

# ARM

CLIMATE RESEARCH FACILITY

## Parsivel2 HANDBOOK

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June 2014



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# **ARM's Handbook for the Parsivel2 Laser Disdrometer**

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## 1.0 General Overview

In order to improve the quantitative description of precipitation processes in climate models, the ARM program has been collecting observations of the drop size spectra of rain events since early in 2006. ARM purchased Parsivel2 laser disdrometers with America Recovery Act funds and they have proven to be robust in the field. They make observations of the particle size distribution over the range of 0.06mm to 24mm and classify precipitation type. To date they have been deployed on board the Spirit Horizon during the MAGIC Field Campaign and one will be permanently deployed at East North Atlantic (ENA). ARM initially deployed impact disdrometers (TWPC1, TWPC3 and SGPC1). Each of the three units deployed was accompanied by a nearby tipping bucket. In 2010, the tipping buckets were upgraded to weighing buckets. Subsequently five video disdrometers were purchased. The purchase of the 6<sup>th</sup> video disdrometer is pending. The video disdrometers are permanently deployed at SGPC1, TWPC1, TWPC3 and in the near future at ENA. One video disdrometer is assigned to the ARM2. What follows is a detailed description of the Parsivel2 laser disdrometers and their datastreams.

## 2.0 Contacts

### 2.1 Mentor

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### 2.2 Vendor / Instrument Developers

Parsivel2 Disdrometers  
OTT Hydromet GmbH  
Ludwigstrasse 16  
87437 Kempten  
Germany  
[www.ott.com](http://www.ott.com)

In USA sold by  
Hach Hydromet  
P.O. Box 389  
Loveland, CO 80539  
[www.hachhydromet.com](http://www.hachhydromet.com)

### 3.0 Deployment Locations and History

Table 1. Deployment Locations

| Serial Number | Property Number | Location             | Date Installed | Date Removed | Status |
|---------------|-----------------|----------------------|----------------|--------------|--------|
|               |                 | MAGIC field campaign | 2012/09/24     | 2013/09/26   |        |
|               |                 | ENA                  | 2014/02/01     | On going     |        |

### 4.0 Near-Real-Time Data Plots

<http://plot.dmf.arm.gov/plotbrowser/>

### 5.0 Data Description and Examples

Data Streams

Xxxpars2Cn.00

Xxxpars2Cn.b1

#### 5.1 Data File Contents

##### 5.1.1 Primary Variables and Expected Uncertainty

The variables for the disdrometer listed in Tables 1 thru 4. The performance of the Parsivel2 disdrometer has not been studied. The performance of an earlier model of Parsivel disdrometer, however, was evaluated in a field study. In this study three different types of disdrometers observed the same rain events for 6 months (Tokai et al., 2013). If the second model's performance is like the first one then, in terms of median volume diameter, the Parsivel showed an absolute % bias of 9.7 and 11.8 in comparison to the 2-dimensional video disdrometer and Joss-Waldvogel impact disdrometer respectively. In terms of liquid water content the absolute % bias values were 17.5 and 21.3 respectively.

The Parsivel2 assigns a precipitation classification whenever precipitation is observed. The precipitation categories are listed below:

- Drizzle
- Drizzle with rain
- Rain
- Rain, drizzle with snow
- Snow
- Snow grains
- Freezing rain
- Hail.

## 5.1.1.1 Primary Variables

Table 2. Parsivel2 Datastream

| Quantity                                 | Variable                      | Measurement Interval  | Units  | Comments   |
|--|-------------------------------|-----------------------|--|--|
| base time in epoch                       | base_time                     | 1 min                 | seconds since<br>YYYY-mm-dd<br>XX:XX:XX X:XX   |  |
| time offset from<br>base_time            | time_offset                   | 1 min                 | seconds since<br>YYYY-mm-dd<br>XX:XX:XX X:XX   |  |
| time offset form<br>midnight             | time                          | 1 min                 | seconds since<br>YYYY-mm-dd<br>XX:XX:XX X:XX   |  |
| north latitude                           | lat                           | constant              | degrees  | permanent<br>deployments have<br>constant latitude;<br>latitude from ship<br>board deployments is<br>contained in separate<br>navigation<br>datastreams      |
| east longitude                           | lon                           | constant/<br>variable | degrees  | Permanent<br>deployments have<br>constant longitude;<br>longitude from<br>ship board<br>deployments is<br>contained in separate<br>navigation<br>datastreams |
| altitude                                 | alt                           | constant/<br>variable | meters above<br>sea level  |  |
| number of<br>drops/particless            | number_detected_<br>particles | 1 min                 | counts   |  |
| weather code                             | weather_code                  | 1 min                 | integer  | SYNOP WaWa Table<br>4680   |
| average diameter<br>of particle class    | particle_size                 | 1 min                 | millimeters  |  |
| precipitation rate                       | precip_rate                   | 1 min                 | millimeters/hour   |  |
| smallest particle                        | diameter_min                  | 1 min                 | millimeters  |  |
| largest particle                         | diameter_max                  | 1 min                 | millimeters  |  |
| moments of particle<br>size distribution | moment1...moment6             | 1 min                 | mm/m <sup>3</sup> ,<br>mm <sup>2</sup> /m <sup>3</sup> ,<br>mm <sup>3</sup> /m <sup>3</sup> ,<br>mm <sup>4</sup> /m <sup>3</sup> ,<br>mm <sup>5</sup> /m <sup>3</sup> ,<br>mm <sup>6</sup> /m <sup>3</sup> |  |
| number density                           | Number_density                | 1 min                 | 1/(m <sup>3</sup> · m)   |  |

| Quantity                       | Variable                          | Measurement Interval | Units                                 | Comments   |
|--------------------------------|-----------------------------------|----------------------|---------------------------------------|--|
| raw fall velocity              | raw_fall_velocity                 | set of 32 constants  | m/s                                   |  |
| fall velocity after Lhermite   | fall_velocity_calculated          | set of 32 constants  | m/s                                   | Lhermite, 2002   |
| raw particle size distribution | raw_spectrum                      |                      | counts                                | matrix (32 x 32) of counts for particles observed in 32 possible particle classes at 32 possible fall velocities |
| class size width               | class_size_width                  |                      | mm                                    |  |
| median volume diameter         | median_volume_diameter            | 1 min                | mm                                    |  |
| liquid water distribution mean | liquid_water_distribution_mean    | 1 min                | millimeters                           |  |
| liquid water content           | liquid_water_content              | 1 min                | mm <sup>3</sup> /m <sup>3</sup>       |  |
| radar reflectivity             | equivalent_radar_reflectivity     | 1 min                | dBZ                                   | S band   |
| radar reflectivity             | equivalent_radar_reflectivity_ott | 1 min                | dBZ                                   | S band reflectivity determined by OTT software   |
| distribution slope             | lambda                            | 1 min                | 1/mm                                  | assumes Marshall-Palmer distribution   |
| distribution intercept         | intercept_parameter               | 1 min                | 1/(meters <sup>3</sup> · millimeters) | assumes Marshall-Palmer distribution   |
| Mor visibility                 | mor_visibility                    | 1 min                | m                                     |  |
| laser band amplitude           | laser_band_amplitude              | 1 min                | counts                                |  |
| sensor temperature             | sensor_temperature                | 1 min                | degrees C                             |  |
| heating current                | heating_current                   | 1 min                | amps                                  |  |
| sensor voltage                 | Sensor_voltage                    | 1 min                | volts DC                              |  |

**Note:** lat/lon/alt refers to the ground where the instrument is sited, NOT the height of the sensor.

### 5.1.1.2 Expected Uncertainty

The performance of the Parsivel2 disdrometer has not been studied. The performance of an earlier model of Parsivel disdrometer, however, was evaluated in a field study. In this study three different types of disdrometers observed the same rain events for 6 months (Tokai et al., 2013). If the second model's performance is like the second one then, in terms of median volume diameter, the Parsivel showed an absolute % bias of 9.7 and 11.8 in comparison to the 2-dimensional video disdrometer and Joss-Waldvogel impact disdrometer respectively. In terms of liquid water content the absolute % bias values were 17.5 and 21.3 respectively.

**Table 3.** Particle Class Specifics for Parsivel2 Disdrometer Observations

| <b>Diameter mm</b> | <b>Width mm</b> | <b>Ott Fall Velocity m/s</b> | <b>Lhermite Velocity m/s</b> |
|--------------------|-----------------|------------------------------|------------------------------|
| 0.0620             | 0.1250          | 0.0500                       | 0.2770                       |
| 0.1870             | 0.1250          | 0.1500                       | 0.8220                       |
| 0.3120             | 0.1250          | 0.2500                       | 1.3510                       |
| 0.4370             | 0.1250          | 0.3500                       | 1.8630                       |
| 0.5620             | 0.1250          | 0.4500                       | 2.3550                       |
| 0.6870             | 0.1250          | 0.5500                       | 2.8280                       |
| 0.8120             | 0.1250          | 0.6500                       | 3.2810                       |
| 0.9370             | 0.1250          | 0.7500                       | 3.7140                       |
| 1.0620             | 0.1250          | 0.8500                       | 4.1250                       |
| 1.1870             | 0.1250          | 0.9500                       | 4.5160                       |
| 1.3750             | 0.2500          | 1.1000                       | 5.0640                       |
| 1.6250             | 0.2500          | 1.3000                       | 5.7210                       |
| 1.8750             | 0.2500          | 1.5000                       | 6.2990                       |
| 2.1250             | 0.2500          | 1.7000                       | 6.8010                       |
| 2.3750             | 0.2500          | 1.9000                       | 7.2330                       |
| 2.7500             | 0.5000          | 2.2000                       | 7.7620                       |
| 3.2500             | 0.5000          | 2.6000                       | 8.2820                       |
| 3.7500             | 0.5000          | 3.0000                       | 8.6330                       |
| 4.2500             | 0.5000          | 3.4000                       | 8.8610                       |
| 4.7500             | 0.5000          | 3.8000                       | 9.0050                       |
| 5.5000             | 1.0000          | 4.4000                       | 9.1200                       |
| 6.5000             | 1.0000          | 5.2000                       | 9.1780                       |
| 7.5000             | 1.0000          | 6.0000                       | 9.1950                       |
| 8.5000             | 1.0000          | 6.8000                       | 9.1990                       |
| 9.5000             | 1.0000          | 7.6000                       | 9.2000                       |
| 11.000             | 2.0000          | 8.8000                       | 9.2000                       |
| 13.000             | 2.0000          | 10.400                       | 9.2000                       |
| 15.000             | 2.0000          | 12.000                       | 9.2000                       |
| 17.000             | 2.0000          | 13.600                       | 9.2000                       |
| 19.000             | 2.0000          | 15.200                       | 9.2000                       |
| 21.500             | 3.0000          | 17.600                       | 9.2000                       |
| 24.000             | 3.0000          | 20.800                       | 9.2000                       |

**5.1.1.3 Definition of Uncertainty**

This section is not applicable to this instrument.

**5.1.2 Secondary / Underlying Variables**

This section is not applicable to this instrument.

**5.1.3 Diagnostic Variables**

This section is not applicable to this instrument.

**5.1.4 Data Quality Flags**

If the data is missing for a sample time, a “missing\_value” value of -999 is assigned to that field.

**Table 4.** Parsivel2 Disdrometer Data Quality Variables

| Quantity            | Variable | Measurement Interval | Min | Max  | Delta |
|---------------------|----------|----------------------|-----|------|-------|
| sample time         | qc_time  | 1 min                |     |      |       |
| number of particles |          | 1 min                | 0   | none | N/A   |
| precip rate         |          | 1 min                | 0   | none | N/A   |
| diameter max        |          | 1 min                | 0   | 24   |       |
| diameter min        |          | 1 min                | 0   | 24   |       |

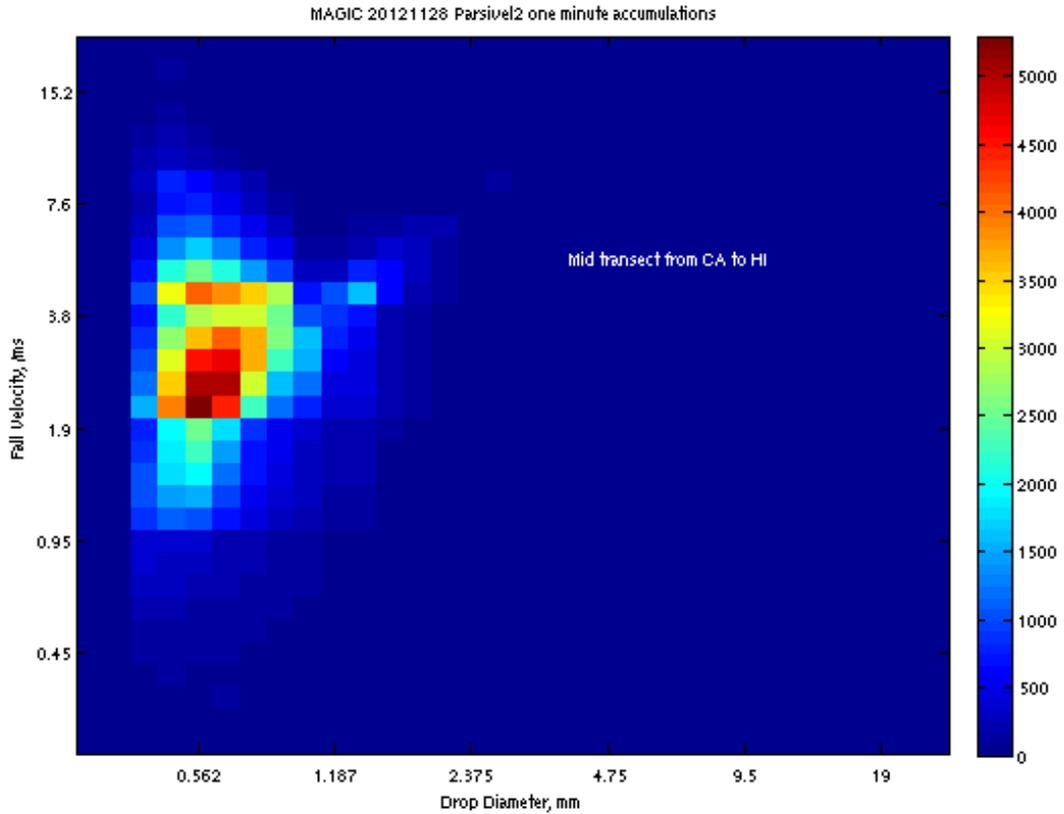
**5.1.5 Dimension Variables**

**Table 5.** Disdrometer Dimension Variables

| Quantity                      | Variable    | Measurement Interval | Unit                                      |
|-------------------------------|-------------|----------------------|---|
| Base time in Epoch            | base_time   | 1 min                | seconds since YYYY-mm-dd<br>XX:XX:XX X:XX |
| Time offset from<br>base_time | time_offset | 1 min                | seconds since YYYY-mm-dd<br>XX:XX:XX X:XX |
| Time offset form<br>midnight  | time        | 1 min                | seconds since YYYY-mm-dd<br>XX:XX:XX X:XX |
| north latitude                | lat         | once                 | degrees                                   |
| east longitude                | lon         | once                 | degrees                                   |
| altitude                      | alt         | once                 | meters above sea level                    |

**Note:** lat/lon/alt refers to the ground where the instrument is sited, NOT the height of the sensor.

## 5.2 Annotated Examples



**Figure 1.** Two dimensional histogram of the drop size distribution observed during MAGIC Field Campaign. This figure shows the sum of all observations over a three hour rain event with rain rates varying from 0 to 10mm/hr. Note that neither the x nor the y axis is linear in this plot.

## 5.3 User Notes and Known Problems

This section is not applicable to this instrument.

## 5.4 Frequently Asked Questions

This section is not applicable to this instrument.

## 6.0 Data Quality

### 6.1 Data Quality Health and Status

The following links go to current data quality health and status results:

- [DQ HandS](#) (Data Quality Health and Status)
- [NCVweb](#) for interactive data plotting using.

The tables and graphs shown contain the techniques used by ARM's data quality analysts, instrument mentors, and site scientists to monitor and diagnose data quality.

### 6.2 Data Reviews by Instrument Mentor

- **QC frequency:** Once or twice a week
- **QC delay:** Three days behind the current day
- **QC type:** DSview plots for instrument operation status, otherwise DQ HandS diagnostic plots
- **Inputs:** None
- **Outputs:** DQPR and DQR as needed
- **Reference:** None.

### 6.3 Data Assessments by Site Scientist / Data Quality Office

All Data Quality Office and most Site Scientist techniques for checking have been incorporated within [DQ HandS](#) and can be viewed there.

### 6.4 Value-Added Procedures and Quality Measurement Experiments

Many of the scientific needs of the ARM Program are met through the analysis and processing of existing data products into "value-added" products or VAPs. Despite extensive instrumentation deployed at the ARM sites, there will always be quantities of interest that are either impractical or impossible to measure directly or routinely. Physical models using ARM instrument data as inputs are implemented as VAPs and can help fill some of the unmet measurement needs of the program. Conversely, ARM produces some VAPs, not in order to fill unmet measurement needs, but to improve the quality of existing measurements. In addition, when more than one measurement is available, ARM also produces "best estimate" VAPs. A special class of VAP, called a Quality Measurement Experiment (QME), does not output geophysical parameters of scientific interest. Rather, a QME adds value to the input datastreams by providing for continuous assessment of the quality of the input data based on internal consistency checks, comparisons between independent similar measurements, or comparisons between mea

## 7.0 Instrument Details

### 7.1 Detailed Description

The OTT Parsivel2 is a laser optical system housed in a metal “Y” shaped structure (Figure 2). A structure at the end of one branch of the “Y” houses the laser. The structure atop the other branch of the “Y” holds the detector. The field of view is midway between the transmitter and detector. The base of the “Y” is recessed to accommodate a vertical mounting pole for instrument deployment. Typically the device is set up at a height of ~6 feet (2 meters). Because the device weighs ~14lbs (6.4kg), a stable base like a concrete pad must be used to support the instrument. The instrument’s physical dimensions are 670mm x 600mm x 114mm.

The laser operates at a wavelength of 780nm with output power of 0.5mW spread out over a beam 30mm wide. Class 1 (21 CFR 1040.10 and 1040.11) also 1 (IEC/EN 60825-1 A2:2001).

#### 7.1.1 List of Components

1. Parsivel2 device with 10m cable
2. RS485 to CAT5 converter (Nport MOXA 5520)
3. Power supply
4. Enclosure for power supply and converter (power supply and converter located indoors)
5. Computer for instrument control and data acquisition
6. Software for instrument control and monitoring, manufacturer’s Application Development System Online (ADSO) software.



**Figure 2.** Parsivel2 Device: The transmitter is located in one housing and the detector is in the other.

#### 7.1.2 System Configuration and Measurement Methods

##### 7.1.2.1 The Data Acquisition Cycle

During normal operation the disdrometer samples for one minute.

#### **7.1.2.2 Firmware Overview**

This section is not applicable to this instrument.

#### **7.1.2.3 Processing Received Signals**

The disdrometer's manufacturer provided software for data acquisition, analysis and inspection. In the case of the Parsivel2, the program is called ADSO and it runs on a personal computer using Windows7. ARM has always a virtual version of ARM's Core PC for this instrument.

#### **7.1.2.4 Siting Requirements**

The disdrometer needs a level firm base and an environment free from local wind distortions. Ideally it should be orientated perpendicular to prevailing winds.

#### **7.1.3 Specifications**

This section is not applicable to this instrument.

### **7.2 Theory of Operation**

The OTT Parsivel2 is a laser optical system that produces a horizontal strip of light. Particles that pass thru the light block a portion of the beam corresponding to their diameter. To determine particle speed, the duration of the diminished signal is measured.

### **7.3 Calibration**

None required

#### **7.3.1 Theory**

This section is not applicable to this instrument.

#### **7.3.2 Procedures**

This section is not applicable to this instrument.

#### **7.3.3 History**

This section is not applicable to this instrument.

## 7.4 Operation and Maintenance

### 7.4.1 User Manual

This section is not applicable to this instrument.

### 7.4.2 Routine and Corrective Maintenance °Documentation

**Frequency:** weekly

**Inspection of site grounds near the instrument:** Visually check the site grounds around the instrument for hazards such as rodent burrows, buried conduit trench settling, and insect nests.

**Checklist response:**

- No Problems Noted
- Problem - Enter any applicable comments for this PM Activity

**Visual inspection of instrument components:**

**Conduit, Cables, and Connectors:** Check that all the conduits on the bottom of the control boxes are secure. Check all conduits from the control boxes to the sensors for damage. Check all sensor wires inside the control box for tightness and damage. Check all the connections at the sensors for damage, water intrusion, and tightness.

**Checklist response:**

- No Problems Noted
- Problem - Enter any applicable comments for this PM Activity

**Check screen for error messages and current weather conditions:**

**Checklist response:**

- No Problems Noted
- Problem - Enter any applicable comments for this PM Activity

**Active maintenance and testing procedures:**

**Disdrometer maintenance:** Keep sensor free of leaves and/or other debris.

**Disdrometer testing:** Precipitation events should show particles accumulating in particle vs velocity plot.

**Checklist response:**

- No problems noted
- Problem - Enter any applicable comments for this PM Activity.

### 7.4.3 Software Documentation

**Disdrometer:** Ingest software.

### 7.4.4 Additional Documentation

This section is not applicable to this instrument.

## 7.5 Glossary

This section is not applicable to this instrument.

## 7.6 Acronyms

Also see the [ARM Acronyms and Abbreviations](#).

## 7.7 Citable References

Tokay, A., W Peterson, P Gatlin, and M Wingo, 2013. "Comparison of raindrop size distribution measurements by collocated disdrometers." *Journal of Atmospheric and Oceanic Technology* 30: 1672-1690. doi:10.1175/JTECH-D-12-00163.1.

## 7.8 Formulas Used in Data Processing

The following quantities are calculated for a distribution with a time interval  $t$ :

R Rainfall rate, [mm/h]

RA Rain amount, [mm]

W Liquid water content, [mm<sup>3</sup>/m<sup>3</sup>]

Z Radar reflectivity factor, [mm<sup>6</sup>/m<sup>3</sup>]

ZdB Radar reflectivity factor, [dB]

Dmax Largest drop registered, [mm]

$N_0$  [1/(m<sup>3</sup>.mm)]

$\Lambda$  Slope, [1/mm]

$N(D_i)$  the number density of drops of the diameter corresponding to size class  $i$  per unit volume, [1/(m<sup>3</sup>.mm)]

Input Data:

$n_i$  number of drops measured in drop size class  $i$  during time interval  $t$

$D_i$  average diameter of the drops in class  $i$  mm

F size of the sensitive surface of the disdrometer m<sup>2</sup>

$F = 0.0054$  m<sup>2</sup>

$t$  time interval for measurement s

$t = 60$  s (standard value)

$v(D_i)$  fall velocity of a drop with diameter  $D_i$  m/s

$\Delta D_i$  diameter interval of drop size class  $i$  mm, see drop size classes below

$$R = \frac{\pi}{6} \cdot \frac{3.6}{10^3} \cdot \frac{1}{F \cdot t} \cdot \sum_{i=1}^{20} (n_i \cdot D_i^3)$$

$$RA = R \cdot t/3600$$

$$RT = \sum RA$$

$$W = \frac{\pi}{6} \cdot \frac{1}{F \cdot t} \cdot \sum_{i=1}^{20} \left( \frac{n_i}{v(D_i)} \cdot D_i^3 \right)$$

$$Wg = W/1000$$

$$Z = \frac{1}{F \cdot t} \cdot \sum_{i=1}^{20} \left( \frac{n_i}{v(D_i)} \cdot D_i^6 \right)$$

$$ZdB = 10 \cdot \log Z$$

$$EK = \frac{\pi}{12} \cdot \frac{1}{F} \cdot \frac{1}{10^6} \cdot \sum_{i=1}^{20} (n_i \cdot D_i^3 \cdot v(D_i)^2)$$

$$EF = EK \cdot 3600/t$$

Dmax

$$N_o = \frac{1}{\pi} \cdot \left( \frac{6!}{\pi} \right)^{\frac{4}{3}} \cdot \left( \frac{W}{Z} \right)^{\frac{4}{3}} \cdot W$$

$$\Lambda = \left( \frac{6!}{\pi} \cdot \frac{W}{Z} \right)^{\frac{1}{3}}$$

$$N(D_i) = \frac{n_i}{F \cdot t \cdot v(D_i) \cdot \Delta D_i}$$



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