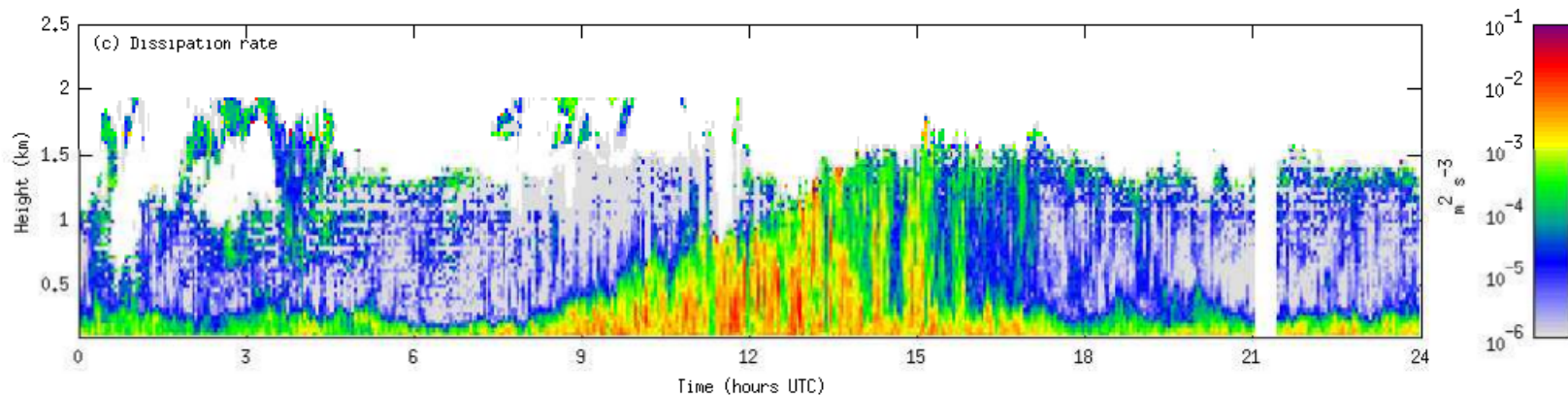




Diagnosing boundary layer properties from remote-sensing observations



Ewan O'Connor

FMI (Finnish Meteorological Institute), Helsinki, Finland

University of Reading, Reading, UK



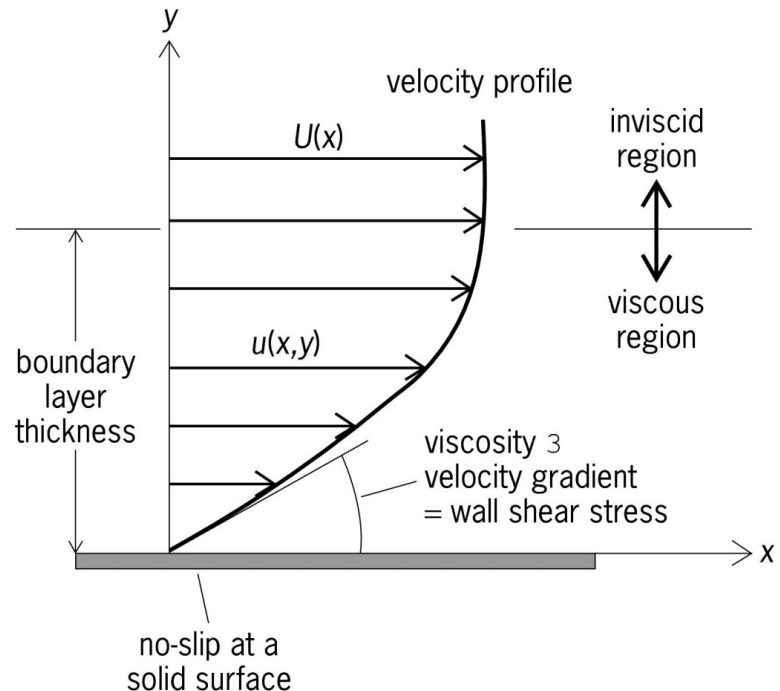
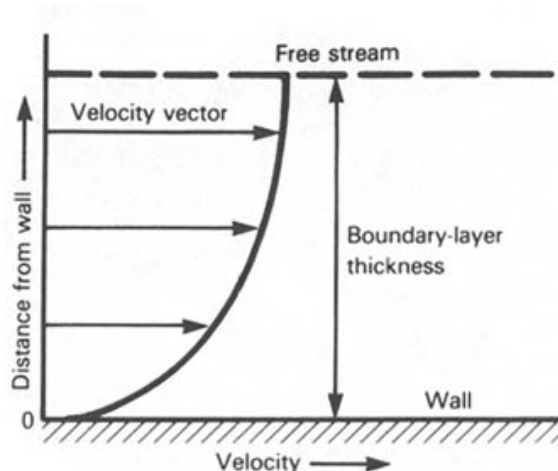
Boundary Layer

- **Friction-only**
 - Classical fluid dynamics
- **Atmospheric stability**
- **Atmospheric**
 - Include convection, cloud
 - Include coast, cities



What is a boundary layer?

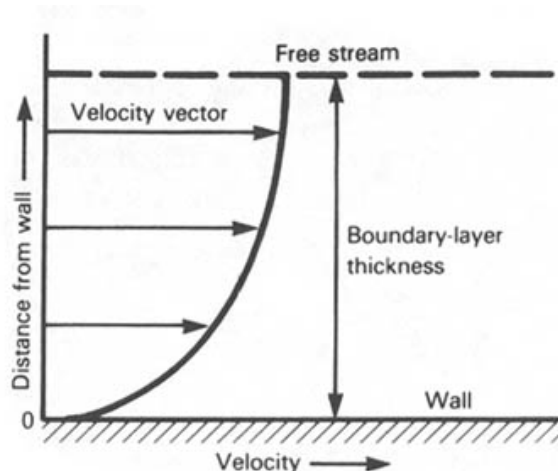
- **Classical fluid dynamics:** the layer in a nearly inviscid fluid next to a surface in which frictional drag associated with that surface is significant (Prandtl, 1905), i.e. no slip-boundary ($v = 0$ at surface),
- Boundary layer can be laminar or turbulent





What is a boundary layer?

- **Classical fluid dynamics:** the layer in a nearly inviscid fluid next to a surface in which frictional drag associated with that surface is significant (Prandtl, 1905), i.e. no slip-boundary ($v = 0$ at surface),
- Boundary layer can be laminar or turbulent



$$u_z = \frac{u_*}{\kappa} \left[\ln \left(\frac{z - d}{z_0} \right) \right]$$

- u_* friction velocity, a measure of shear stress
- κ von Kármán constant (=0.41)
- z distance from surface
- z_0 surface roughness
- d displacement height (for rough surfaces)

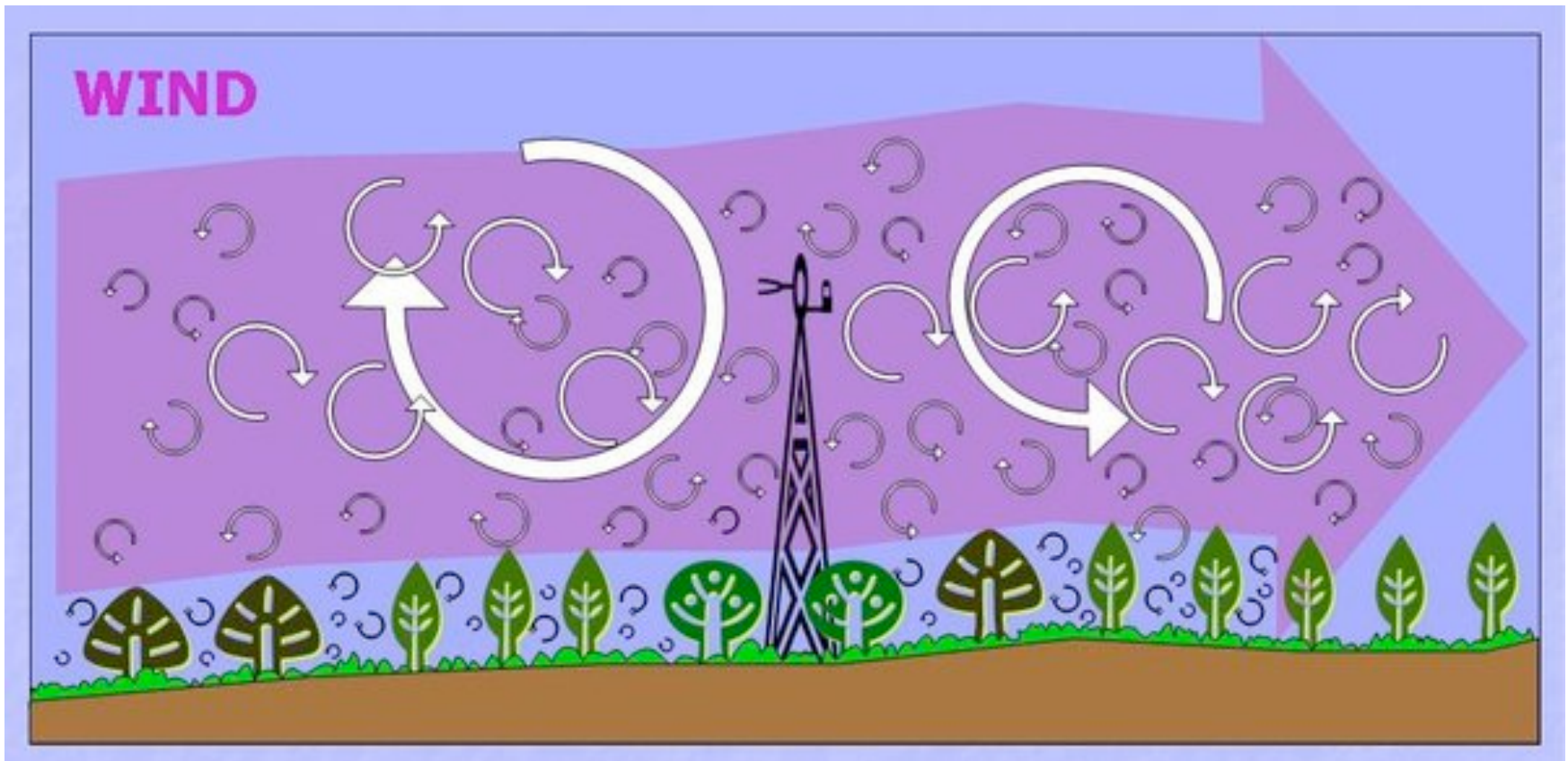


Turbulent motions





Turbulent motions





Atmospheric Boundary Layer?

- Displacement height is where zero wind speed is achieved as a result of flow obstacles such as trees or buildings.
 - Typical value is $2/3$ of the average obstacle height
- Roughness length is between $1/10$ and $1/30$ of the average height of the roughness elements on the ground:

Surface	Roughness length (m)
flat, open grassland	
cropland	
scrub or forest	
cities with skyscrapers	
ice (smooth to rough)	
smooth open water	



Atmospheric Boundary Layer?

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Surface	Roughness length (m)
flat, open grassland	0.03
cropland	
scrub or forest	
cities with skyscrapers	
ice (smooth to rough)	
smooth open water	



Atmospheric Boundary Layer?

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cropland	0.1 – 0.25
scrub or forest	
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ice (smooth to rough)	
smooth open water	



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scrub or forest	0.5 - 1
cities with skyscrapers	
ice (smooth to rough)	
smooth open water	



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flat, open grassland	0.03
cropland	0.1 – 0.25
scrub or forest	0.5 - 1
cities with skyscrapers	2
ice (smooth to rough)	
smooth open water	



Atmospheric Boundary Layer?

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cropland	0.1 – 0.25
scrub or forest	0.5 - 1
cities with skyscrapers	2
ice (smooth to rough)	0.002 – 0.4
smooth open water	



Atmospheric Boundary Layer?

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Surface	Roughness length (m)
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scrub or forest	0.5 - 1
cities with skyscrapers	2
ice (smooth to rough)	0.002 – 0.4
smooth open water	0.0002



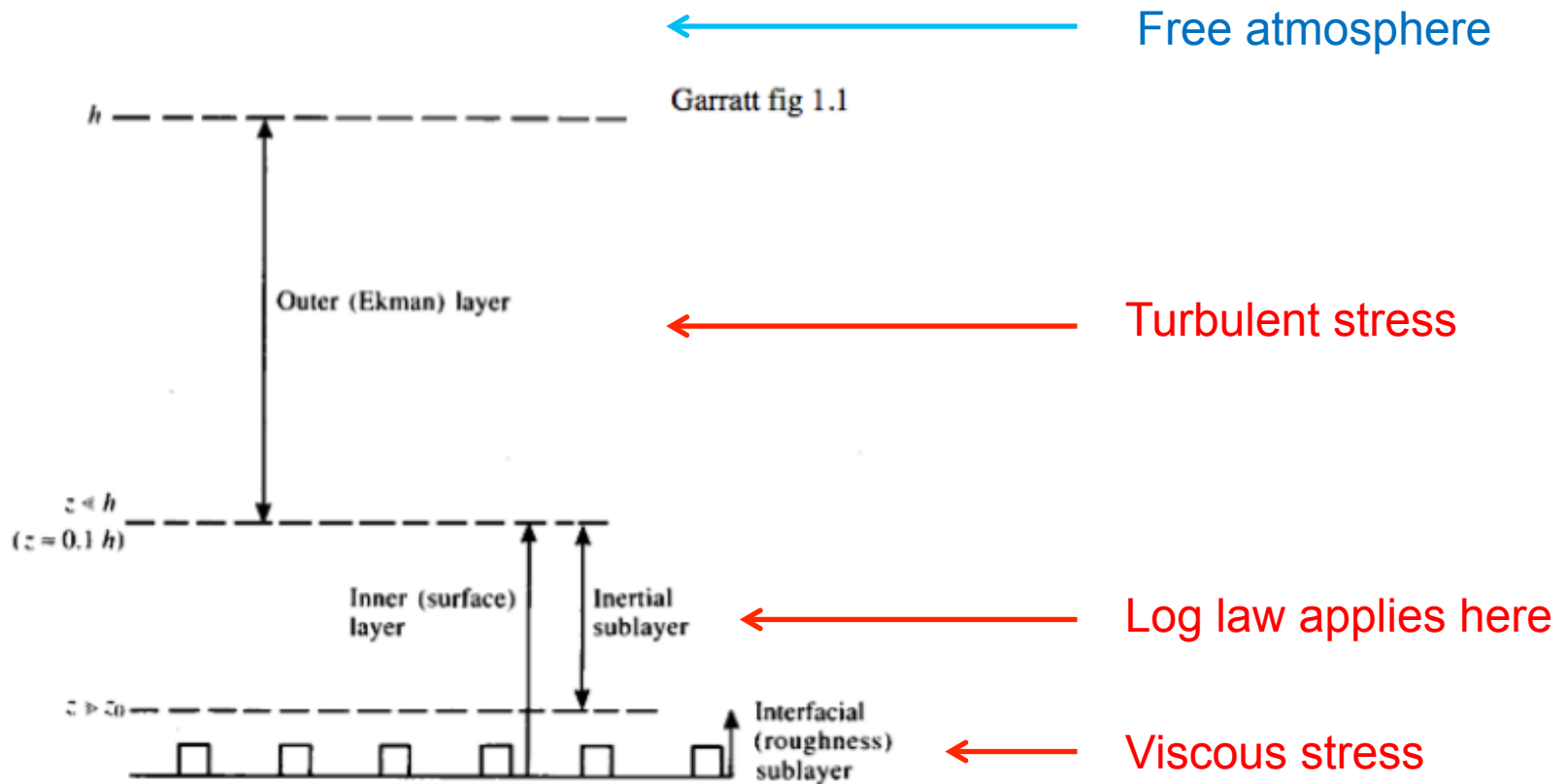
Atmospheric Boundary layer?

- **In addition to friction:**
 - Surface heat exchange (convection)
 - Moisture (and effects on convection)
 - Earth's rotation
 - Complex surface characteristics and topography
- There are significant fluxes of momentum, heat and/or moisture carried by turbulent motions whose horizontal and vertical scales are on the order of the boundary layer depth, and whose circulation timescale is a few hours or less.
- This is similar for the ocean surface, although with different scaling parameters



Atmospheric boundary layer?

- has multiple components





Atmospheric stability – Potential temperature

- **Definition:** θ is the temperature that an air parcel would have if adiabatically brought to a standard reference pressure P_0

$$\theta = T \left(\frac{P_0}{P} \right)^{R/c_p},$$

T current absolute temperature (in K) of the parcel,

R gas constant for air

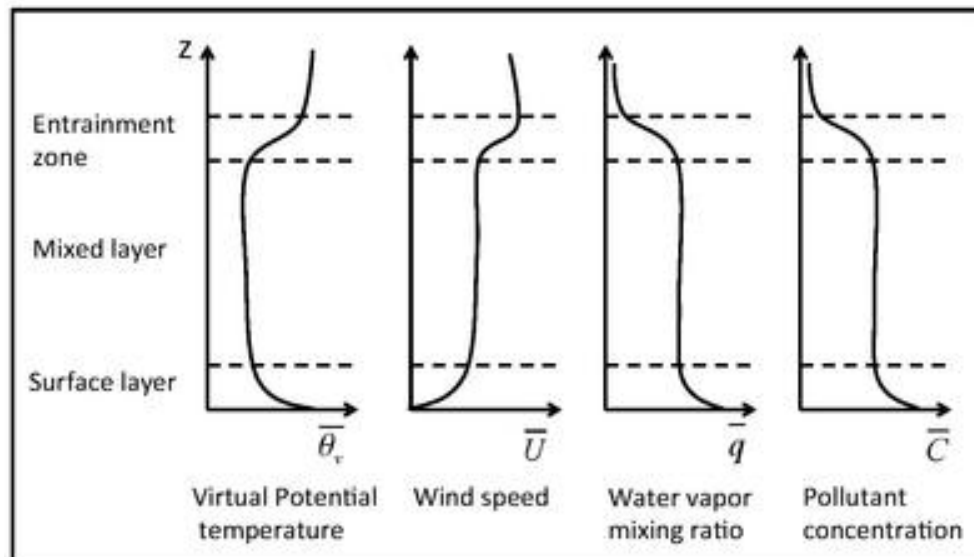
c_p specific heat capacity at constant pressure

$R/c_p = 0.286$ in air



Atmospheric stability – Potential temperature

- θ is conserved under dry adiabatic conditions
- potential temperature will not change in the absence of heating, cooling, evaporation, or condensation
- θ_v (virtual θ) is useful approximation to include moist adiabatic processes





Atmospheric stability – Potential temperature

- In equilibrium: BLH determined by competition between
 - static stability, N^2
 - velocity shear, S^2
- Gradient Richardson number

$$Ri = \frac{N^2}{S^2}$$



Atmospheric stability – Potential temperature

- In equilibrium: BLH determined by competition between
 - static stability, N^2
 - velocity shear, S^2
- Gradient Richardson number

$$Ri = \frac{N^2}{S^2}$$

$$Ri \equiv \frac{\beta(\partial\theta_v/\partial z)}{(\partial u/\partial z)^2 + (\partial v/\partial z)^2} \rightarrow Ri_c = 0.25.$$

$$\beta = g/T_0$$



Atmospheric stability – Potential temperature

- In equilibrium: BLH determined by competition between
 - static stability, N^2
 - velocity shear, S^2
- Bulk Richardson number:

$$\text{Ri} = \frac{N^2}{S^2}$$

$$\text{Ri}_B \equiv \frac{\beta \Delta \theta_v h}{U^2}$$

$$U = \sqrt{u^2(h) + v^2(h)},$$



Monin-Obukhov similarity

Obukhov length: characteristic length scale of surface layer turbulence

$$L = - \frac{u_*^3 \bar{\theta}_v}{kg \overline{(w' \theta'_v)}_s}$$

u_* friction velocity, a measure of shear stress

$\bar{\theta}_v$ mean virtual potential temperature

$\overline{(w' \theta'_v)}_s$ virtual potential temperature flux (at surface)

k von Kármán constant (=0.41)

$$\overline{w' \theta'_v} = \overline{w' \theta'} + 0.61 \bar{T} \overline{w' q'}$$

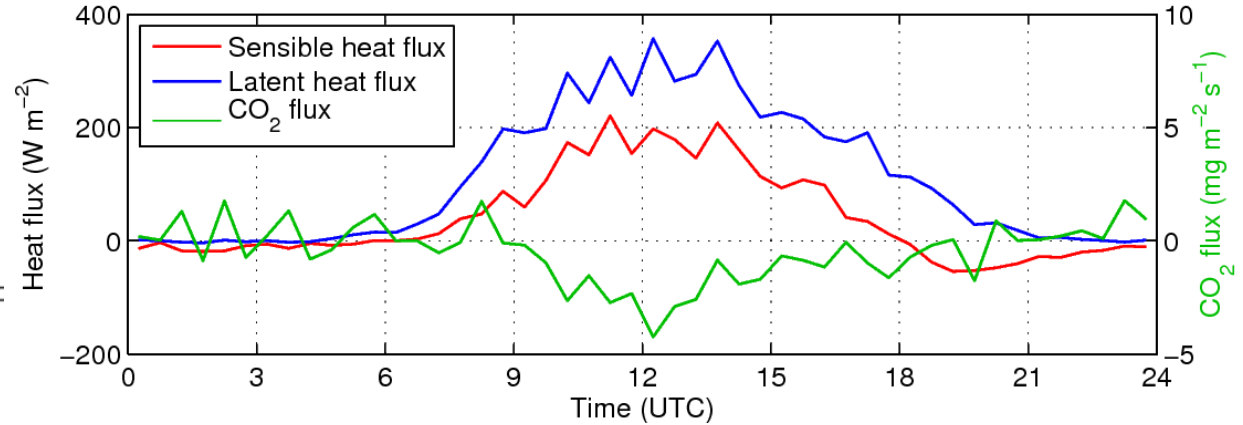
Sensible and latent heat flux



Monin-Obukhov similarity

Obukhov length

$$L =$$



- +ve daytime $L < 0$
- 0 dawn/dusk $L = \infty$
- -ve nighttime $L > 0$

$$\overline{(w'\theta'_v)_s}$$



Monin-Obukhov similarity

Obukhov length

$$L = - \frac{u_*^3 \bar{\theta}_v}{kg(\overline{w'\theta'_v})_s}$$

- | | | | |
|------------------------------|-----------------|--------------|----------|
| | • +ve daytime | $L < 0$ | unstable |
| $(\overline{w'\theta'_v})_s$ | • 0 dawn/dusk | $L = \infty$ | neutral |
| | • -ve nighttime | $L > 0$ | stable |

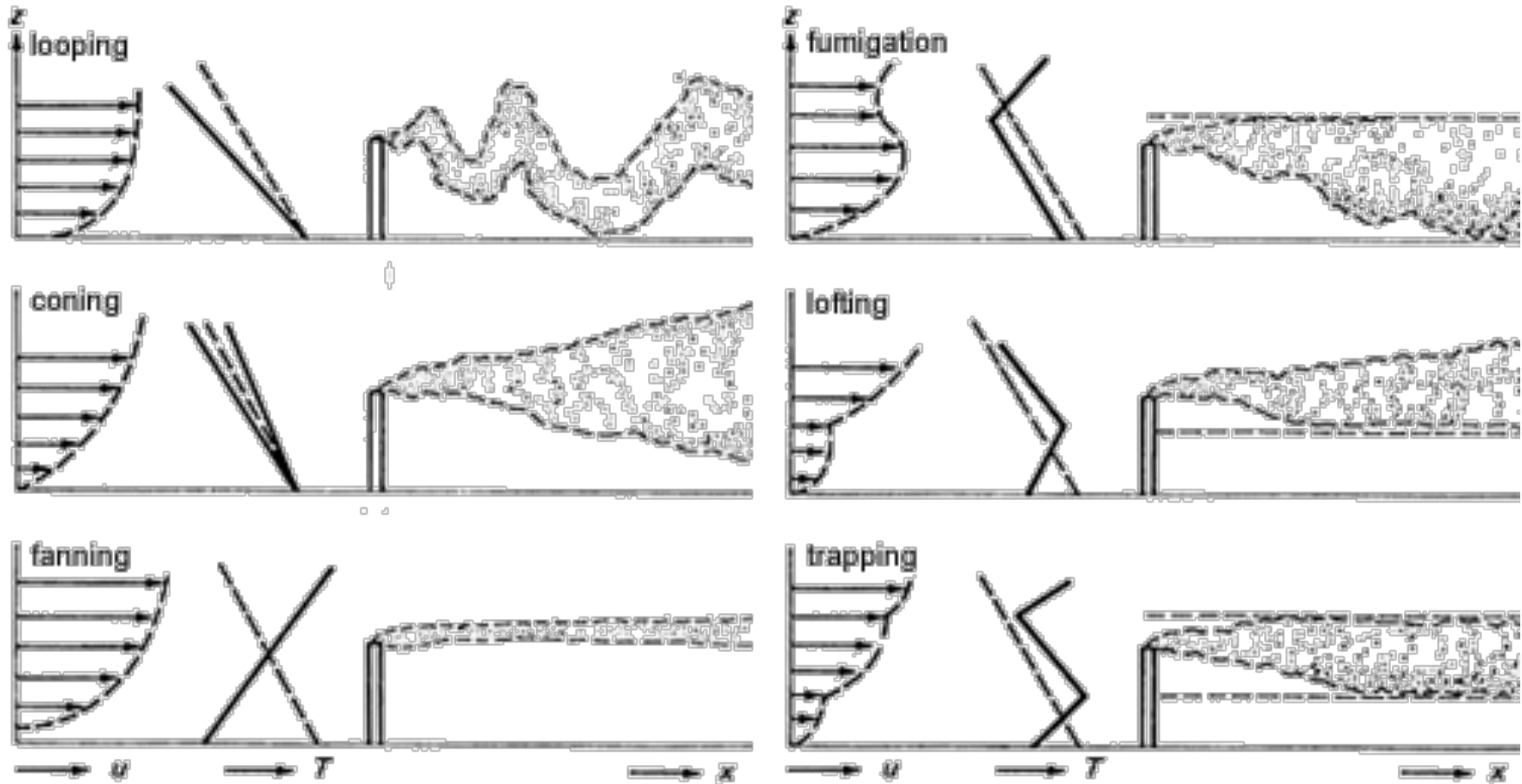
|L| determines whether buoyancy dominates shear



Why is BL height important?



Plume model





Plume model

Different Winds





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Plume observations - Kuopio





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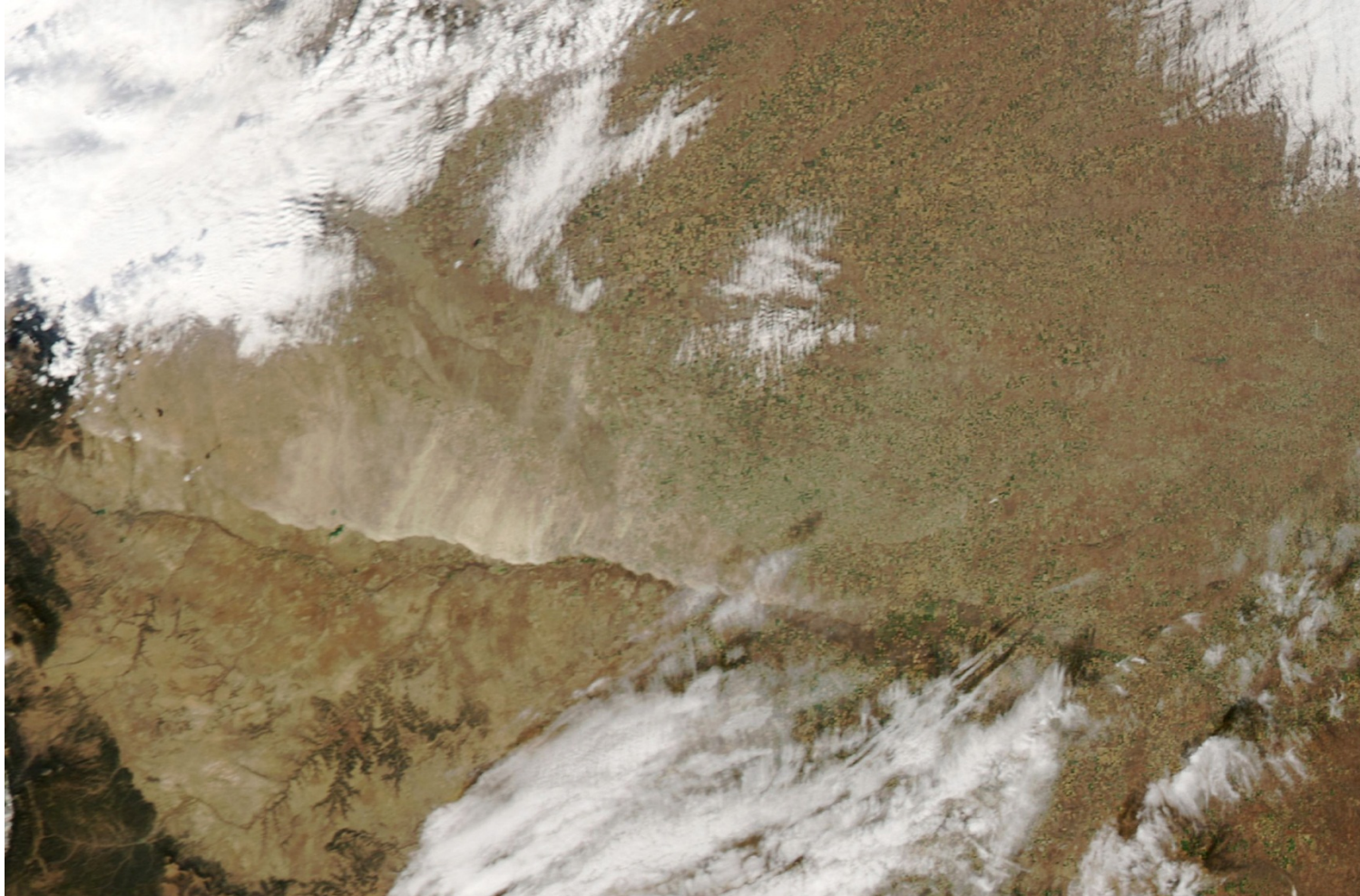


Plume observations - Kuopio





Synoptic scale – dust lofted by front



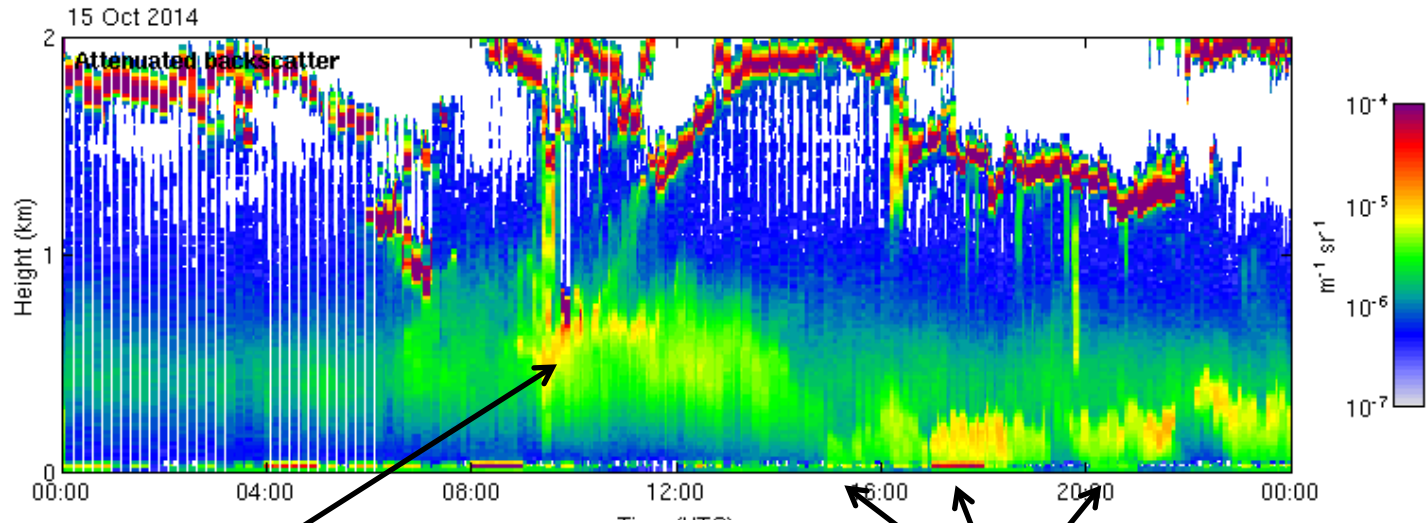


Example from aircraft





Re-suspended ash/dust – NCAS DL at Hatun (Iceland)

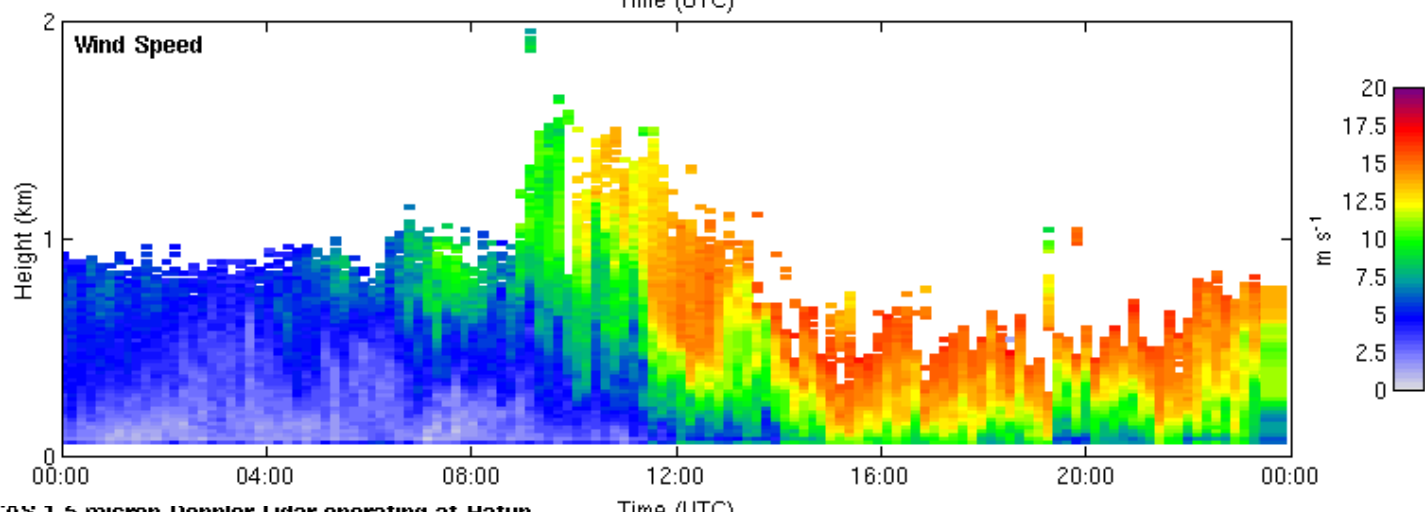
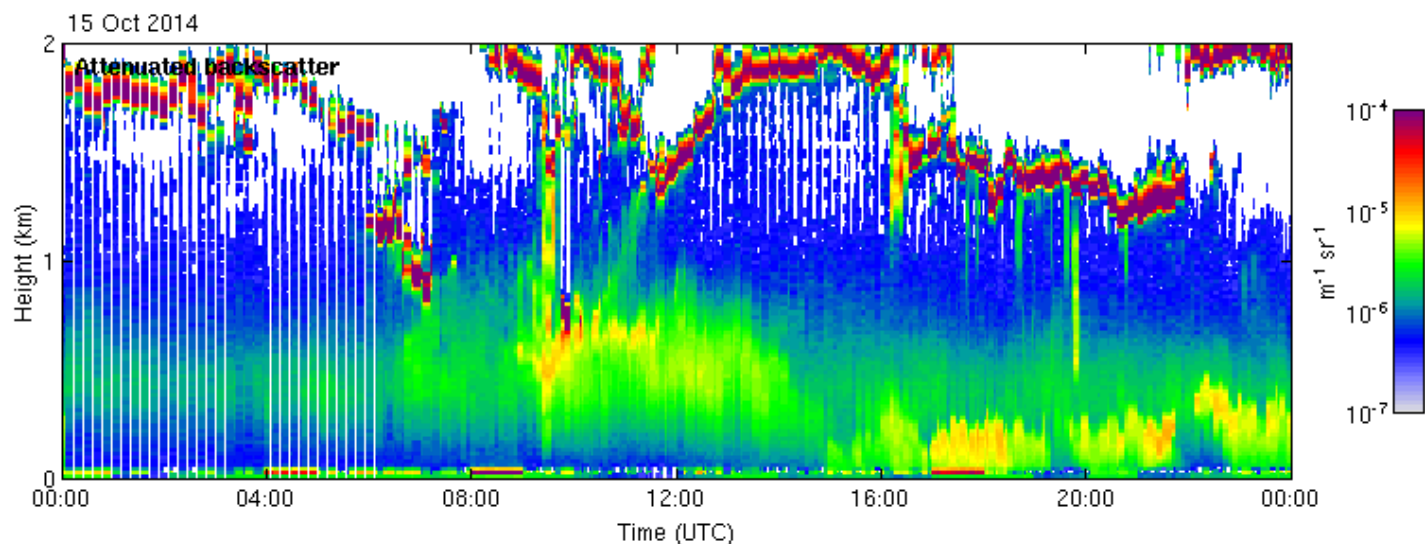


Elevated dust

Local dust being lofted




Re-suspended ash/dust – NCAS DL at Hatun (Iceland)

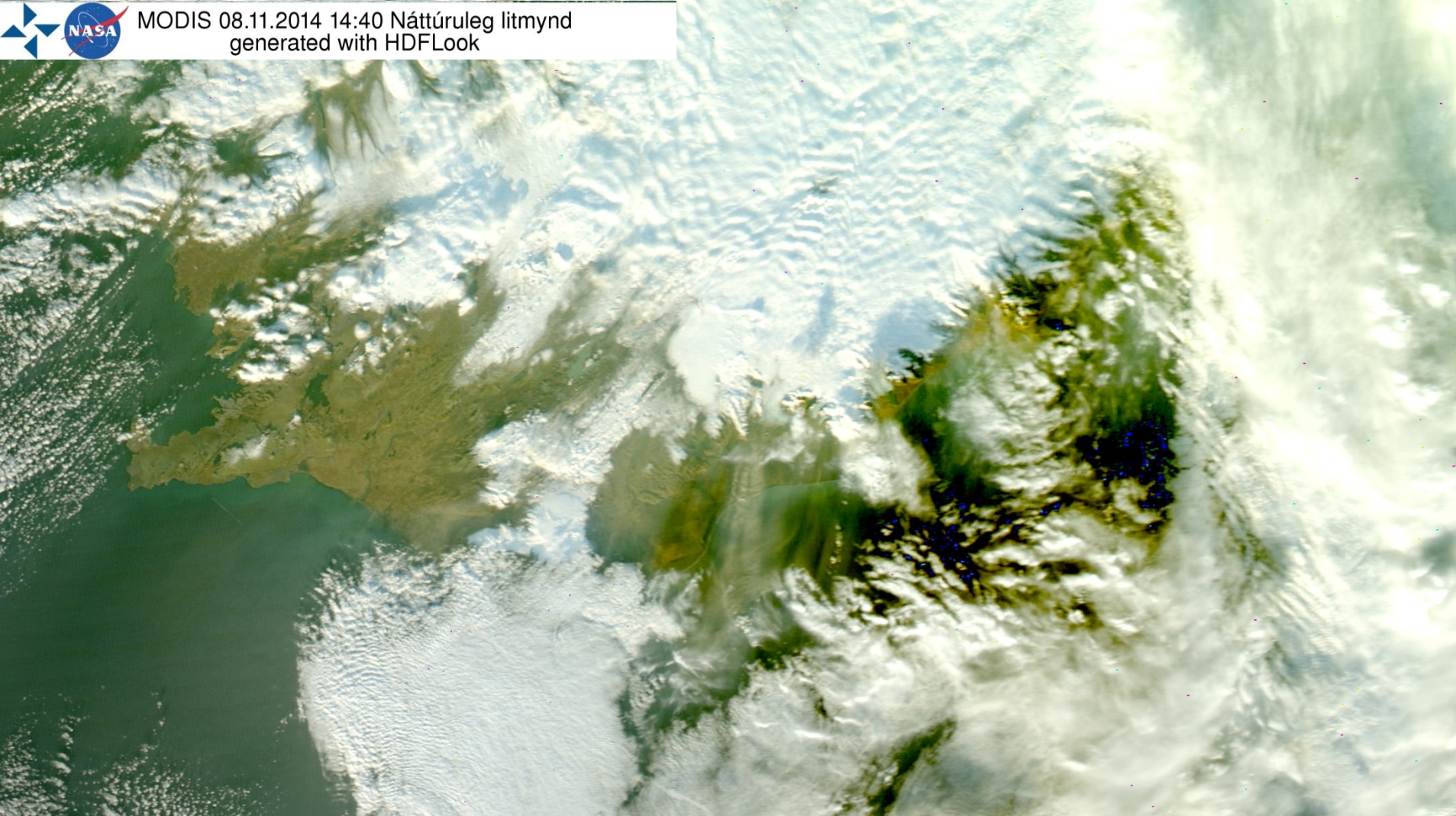




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Re-suspended ash/dust

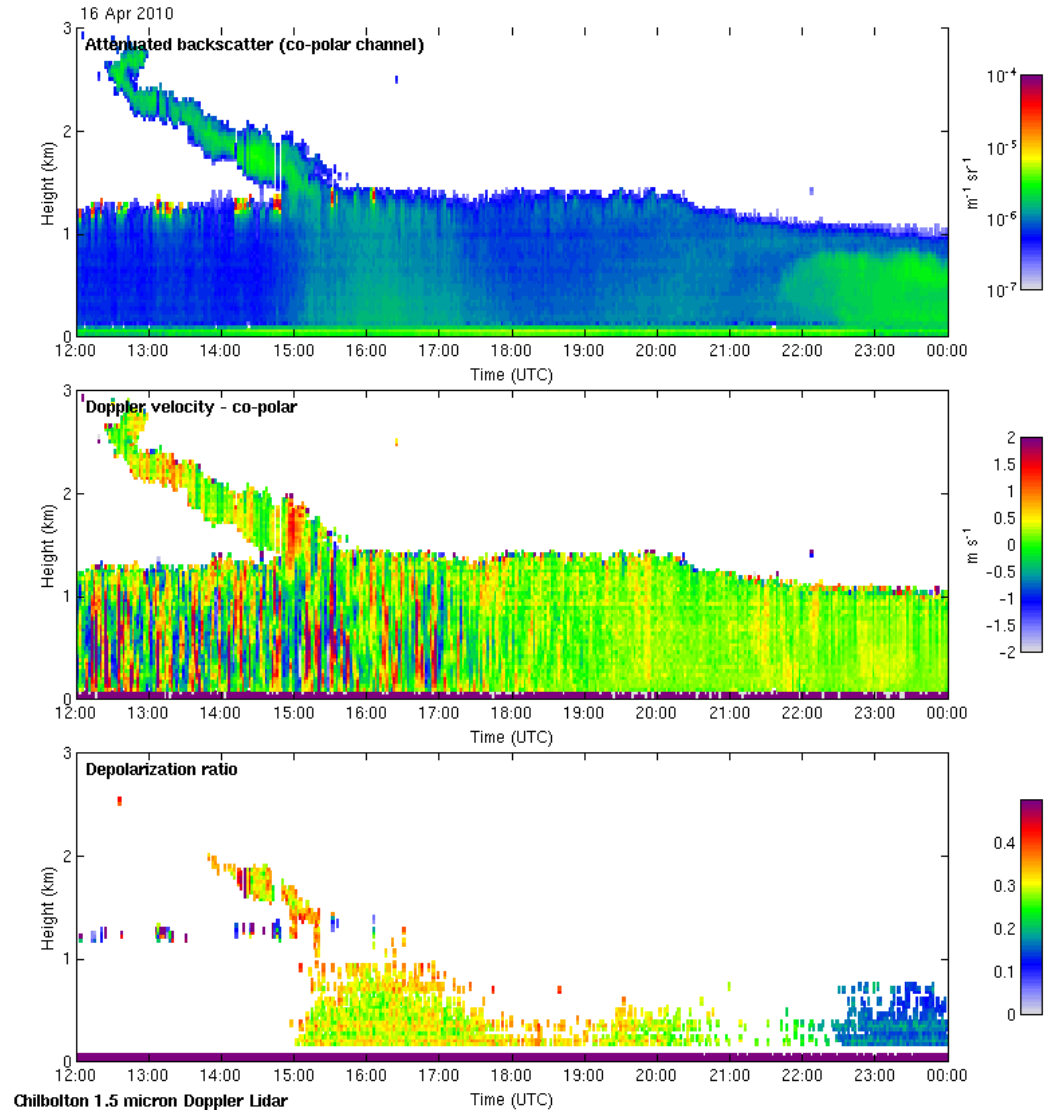
 MODIS 08.11.2014 14:40 Náttúruleg litmynd
generated with HDFLook





Volcanic ash plume from Eyjafjallajökull

Plume over UK 16th April 2010





Atmospheric boundary layer

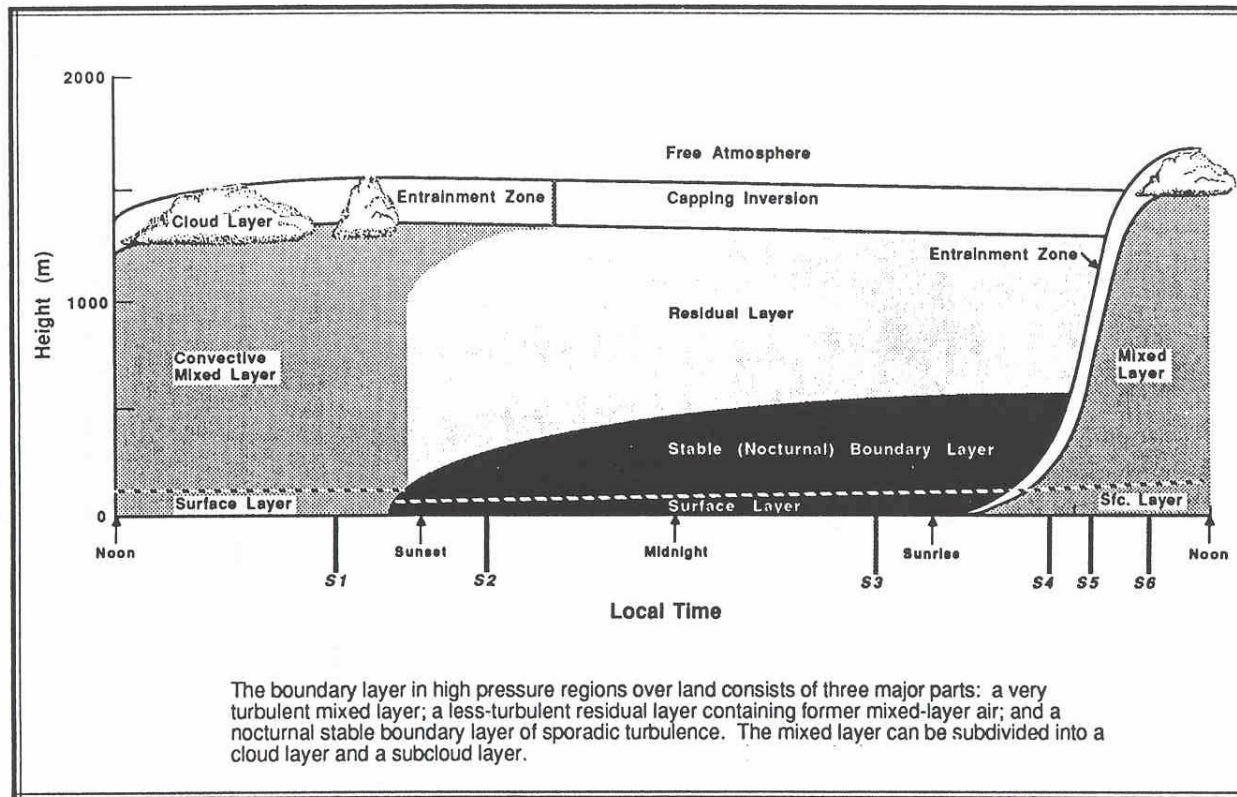
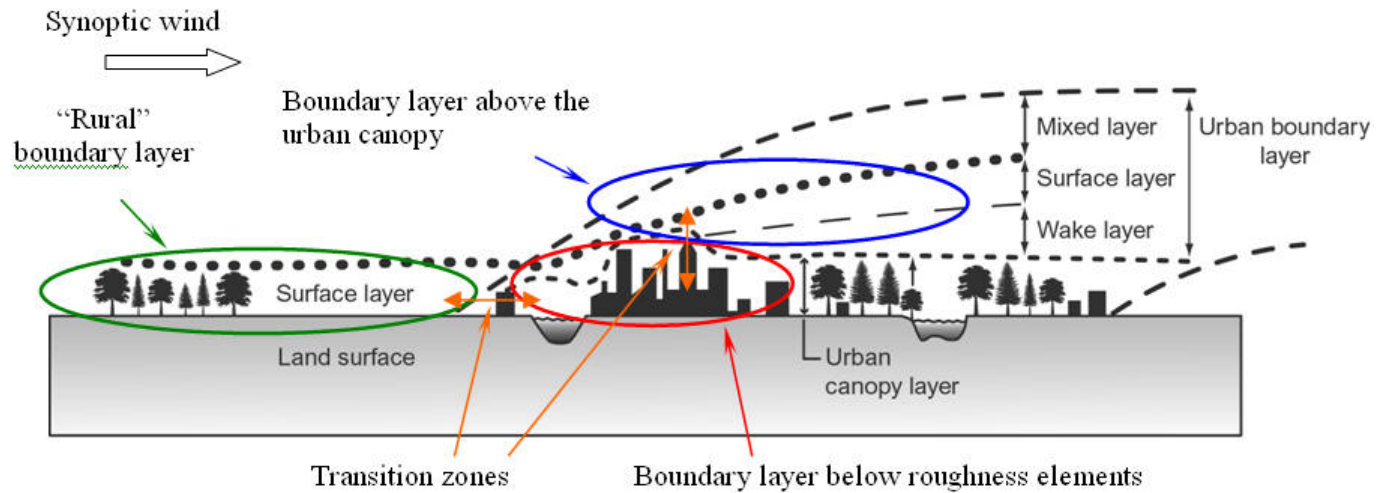


FIGURE 3 (Taken from Stull, 1988)

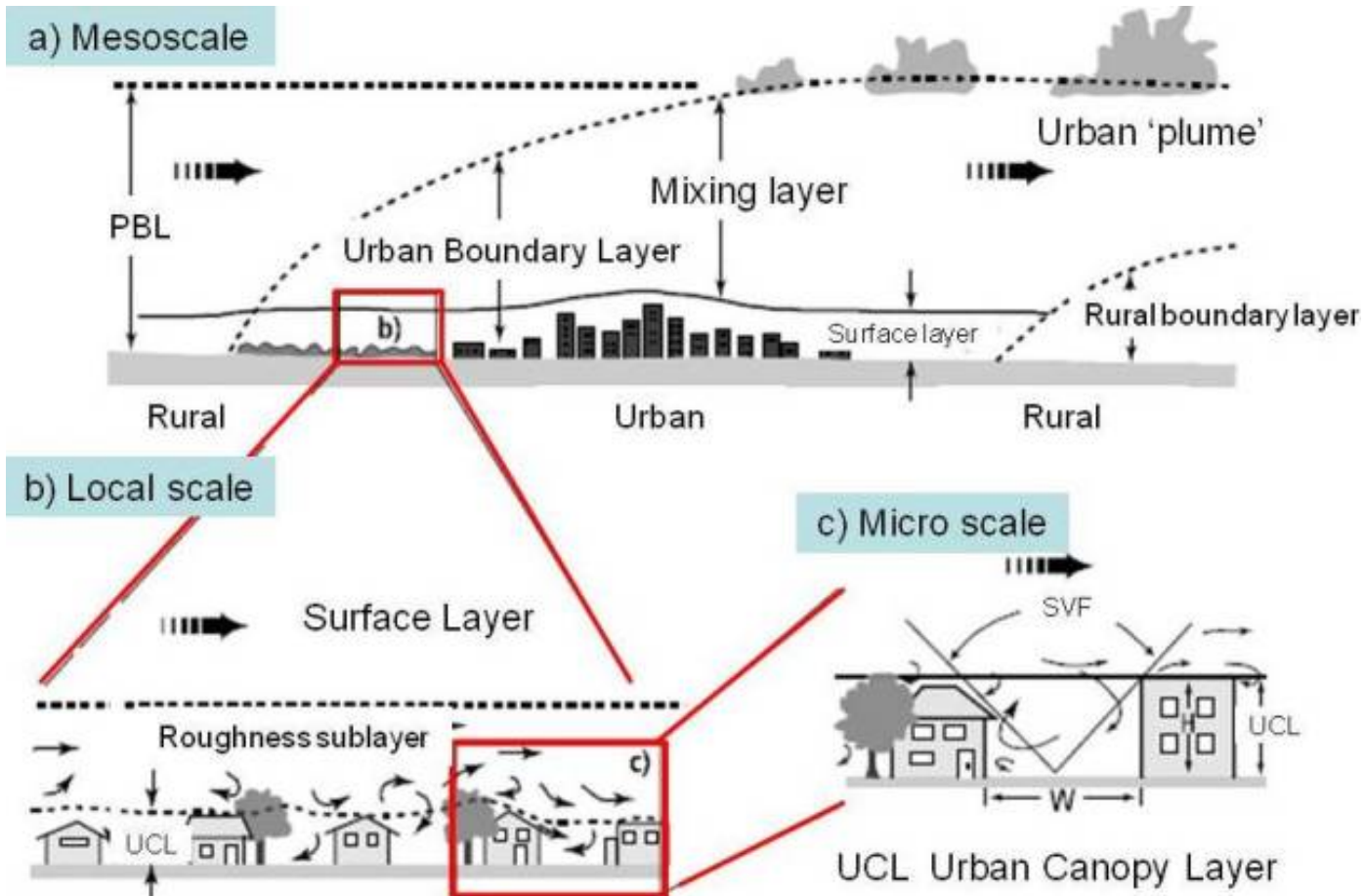


Over cities



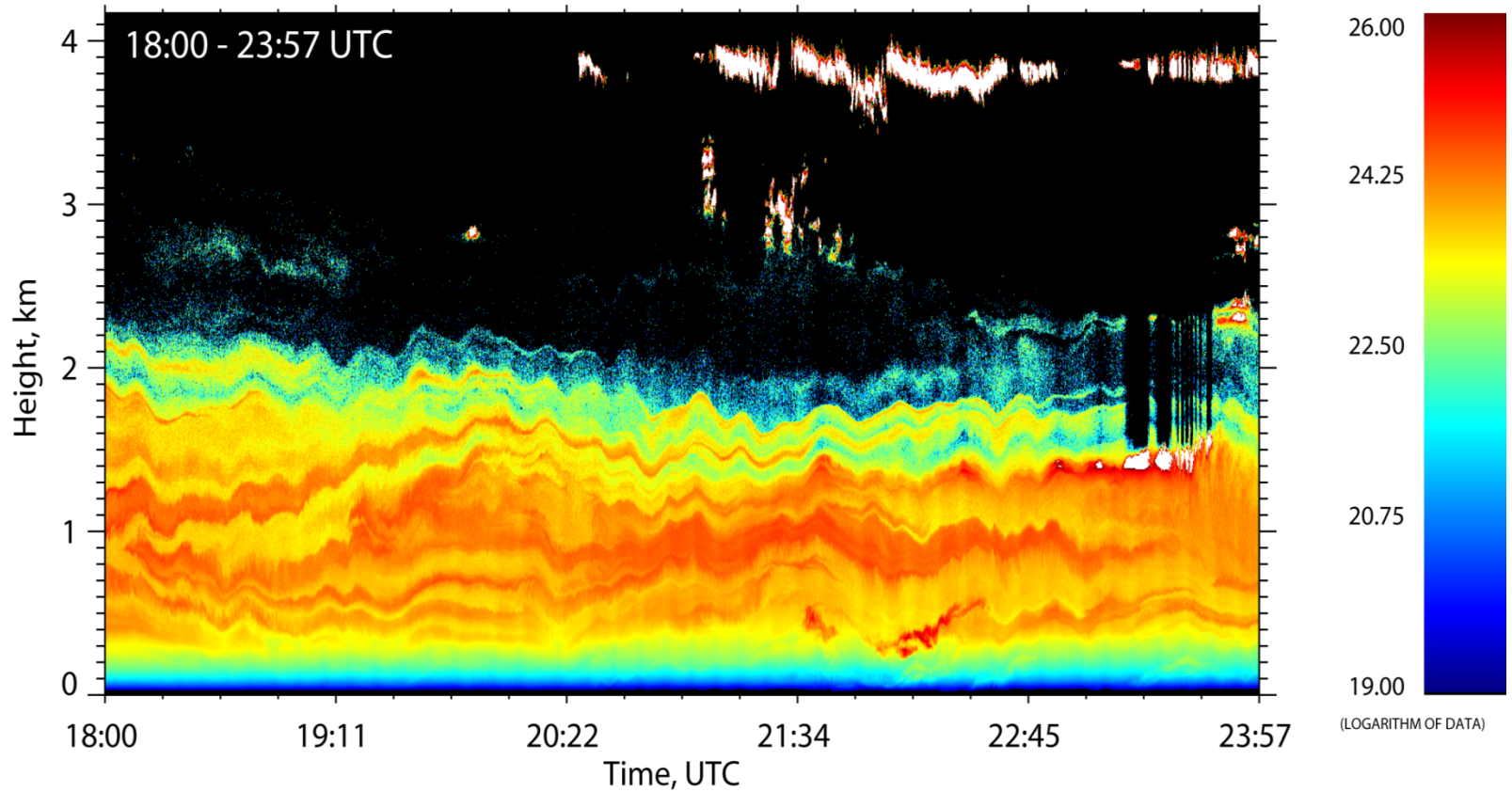


Over cities





PollyXT_FMI, Elandsfontain, 532 nm, 2010_03_25





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How can we diagnose boundary layer properties from remote sensing?



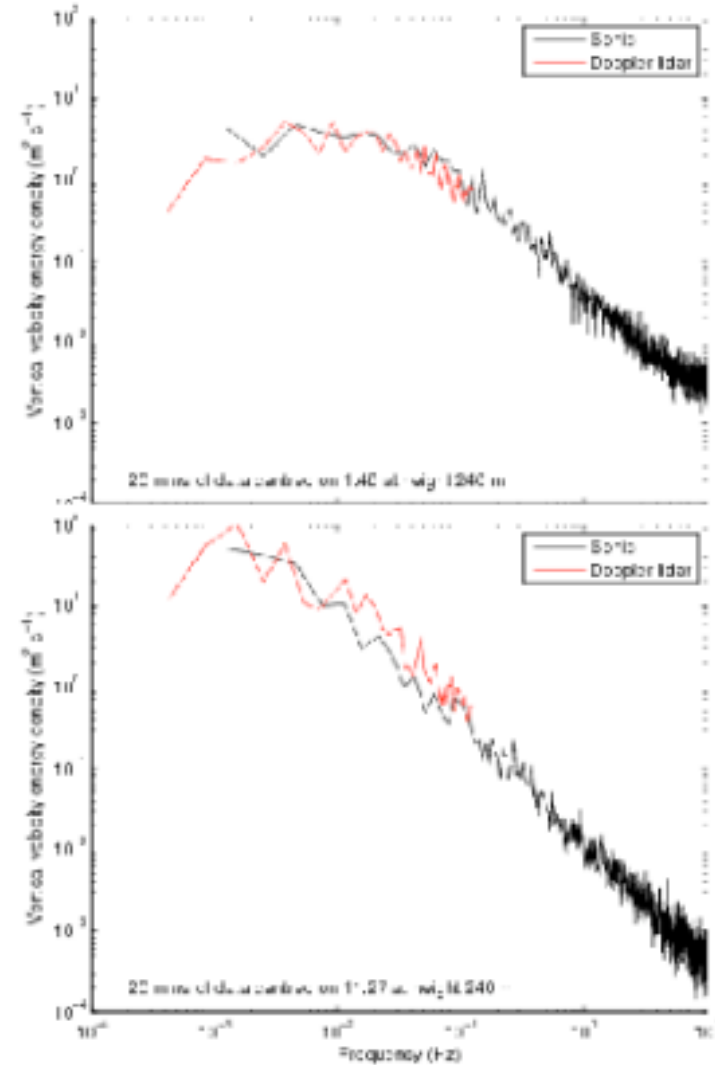
How can we diagnose boundary layer properties from remote sensing?

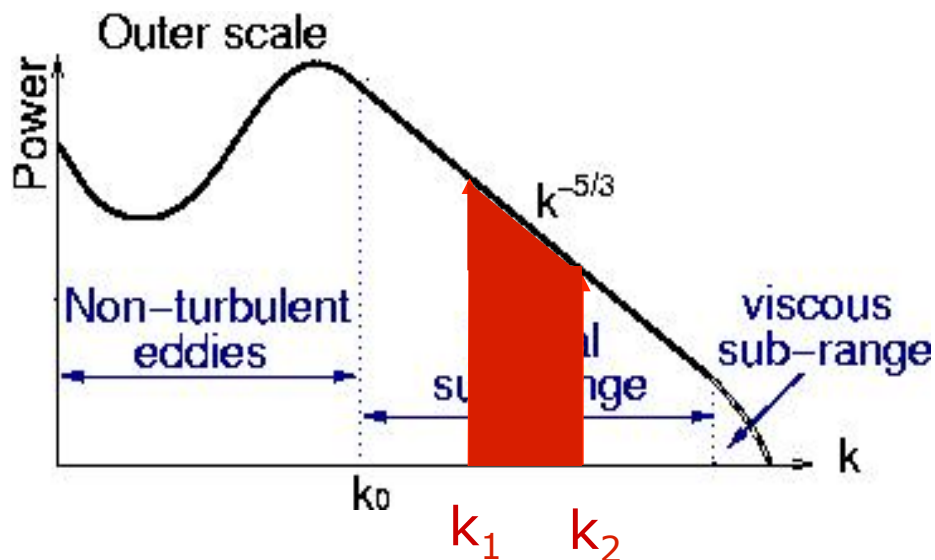
- Possible tracers for turbulent mixing:
 - Velocity variance
 - Temperature
 - Humidity
 - Aerosol
 - Trace gases



Doppler lidar velocity spectra have the expected shape

(if high SNR!)





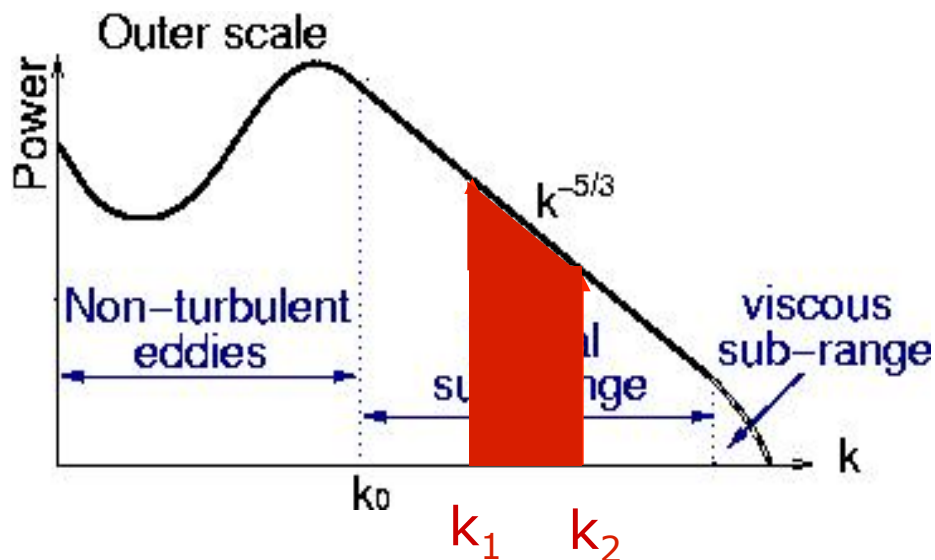
In the inertial sub-range
(Kolmogorov)

$$S(k) = a\varepsilon^{2/3}k^{-5/3}$$

k_1 is min horizontal wavenumber sampled over 300 s (use model winds)
 k_2 is max horizontal wavenumber due to beamwidth of lidar

Part of TKE spectrum can be interpreted in terms of the variance of the mean Doppler velocity:

$$\sigma_v^2 = \int_{k_1}^{k_2} S(k) dk$$



In the inertial sub-range
(Kolmogorov)

$$S(k) = a\varepsilon^{2/3}k^{-5/3}$$

k_1 is min horizontal wavenumber sampled over 300 s (use model winds)
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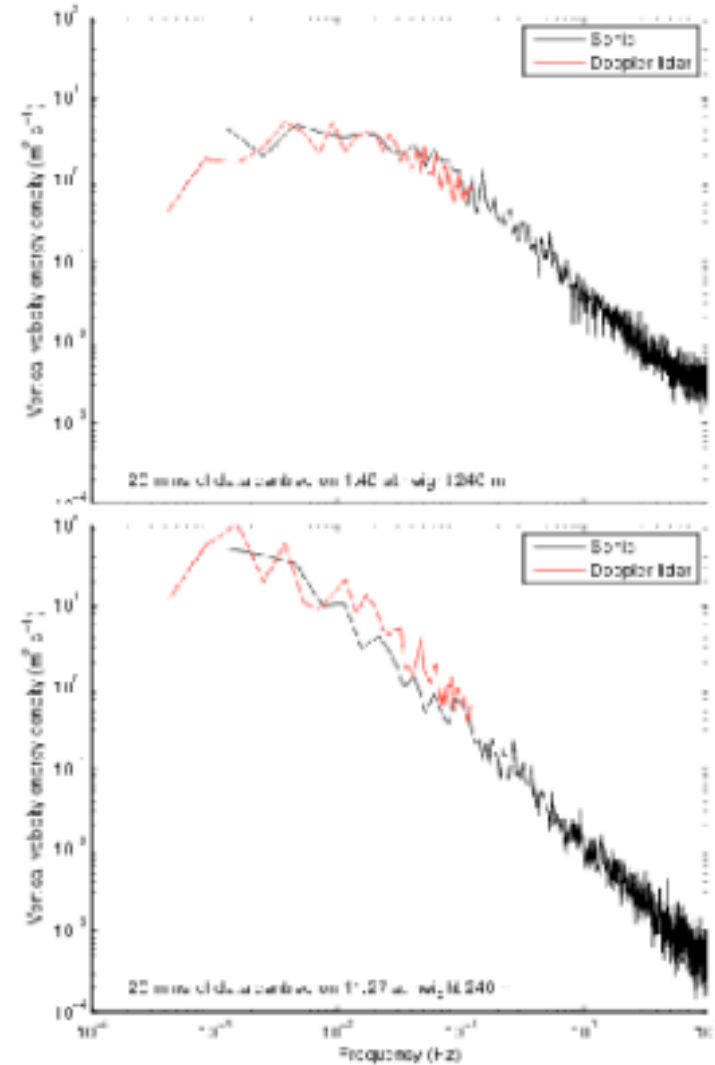
$$\sigma_v^2 = \frac{3a}{2} \varepsilon^{2/3} \left(k_2^{-2/3} - k_1^{-2/3} \right)$$

$$\varepsilon = \left(\frac{2}{3a} \right)^{3/2} \sigma_v^3 \left(k_1^{-2/3} - k_2^{-2/3} \right)^{3/2}$$



Doppler lidar velocity spectra have the expected shape

(if high SNR!)





Doppler lidar velocity uncertainty

$$\sigma_e = \left(\frac{\Delta v^2 \sqrt{2}}{\alpha N_p} (1 + 1.6\alpha + 0.4\alpha^2) \right)^{1/2},$$

Δv , signal spectral width

B receiver bandwidth

α Ratio of detector photon count
to speckle count

$$\alpha = \frac{\text{SNR}}{(2\pi)^{1/2} (\Delta v / B)},$$

N_p Accumulated photon count

$$N_p = \text{SNR } n M,$$



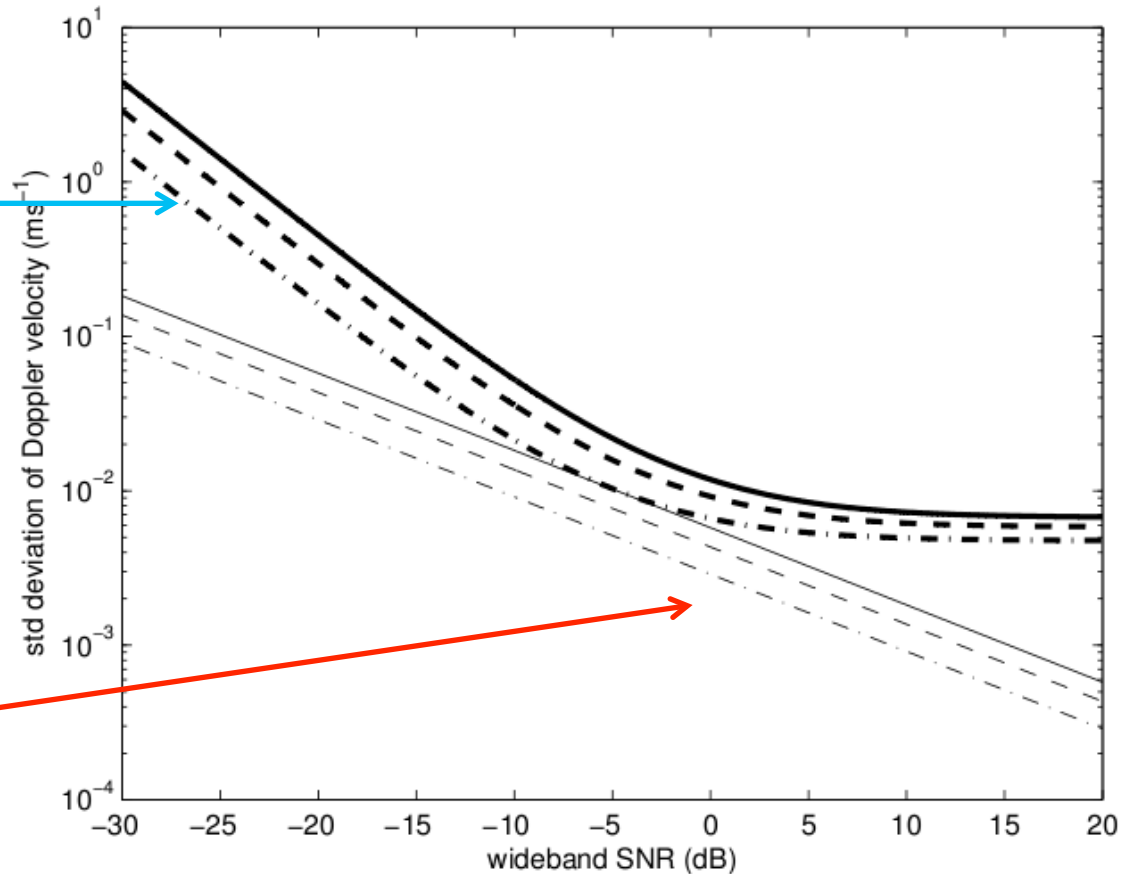
Doppler lidar velocity uncertainty

Heterodyne detection

Lines indicate choice of Δv ,
(signal spectral width)

Direct detection

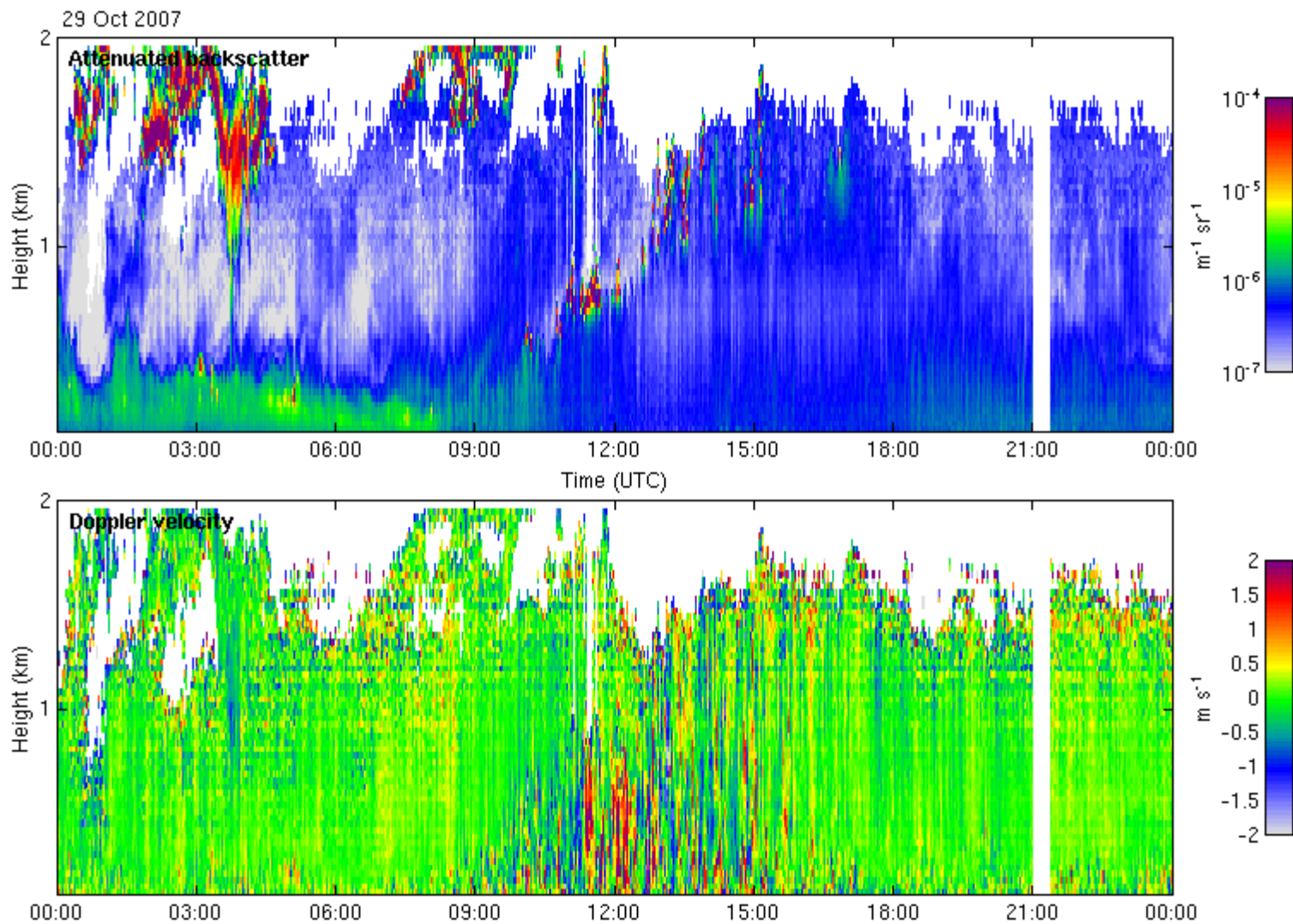
$$\sigma_e = \Delta v / (N_p^{0.5}),$$



Measurements



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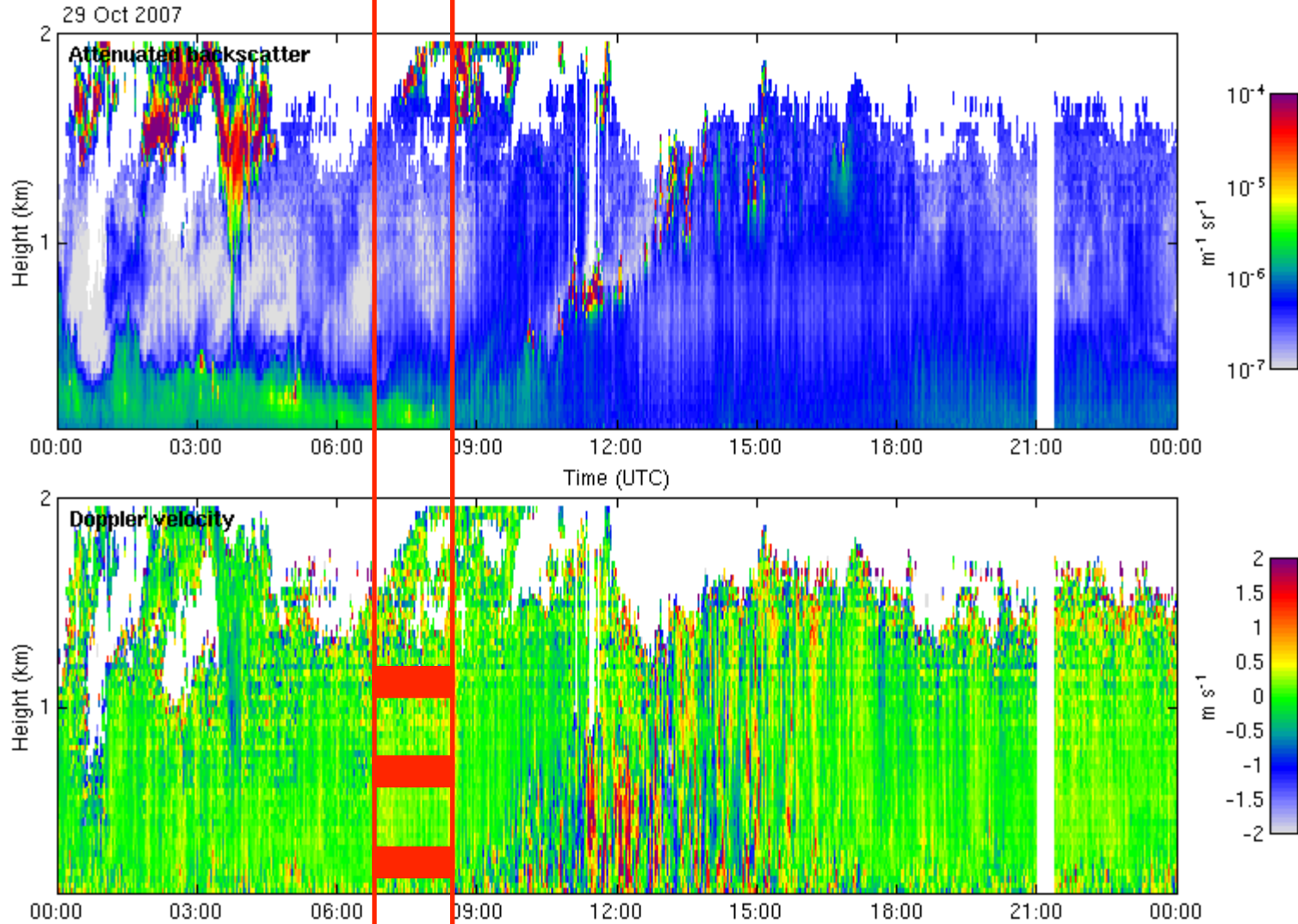


Salford 1.5 micron Doppler Lidar operating at REPARTEE Time (UTC)

Measurements



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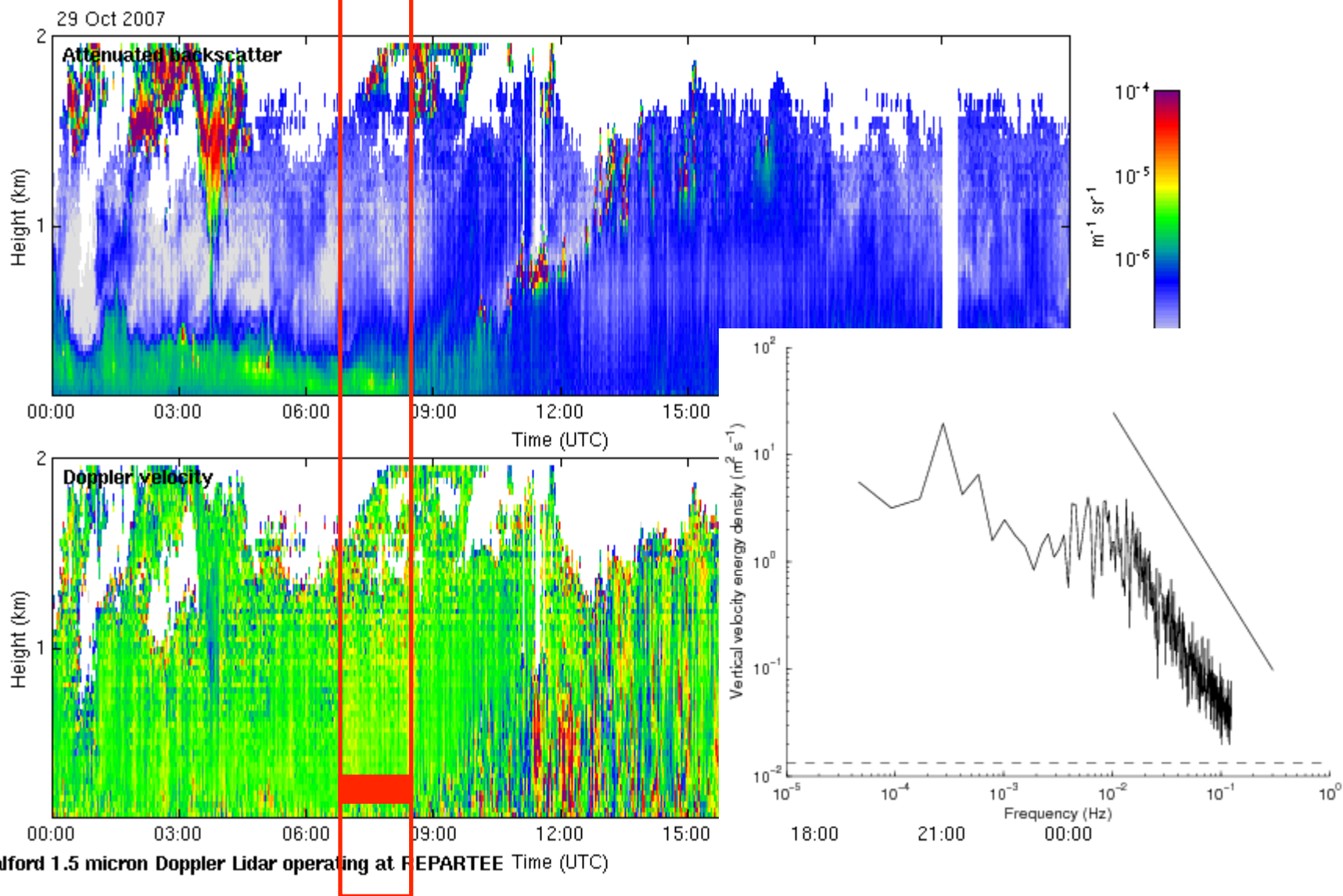


Salford 1.5 micron Doppler Lidar operating at FEPARTEE Time (UTC)

Measurements



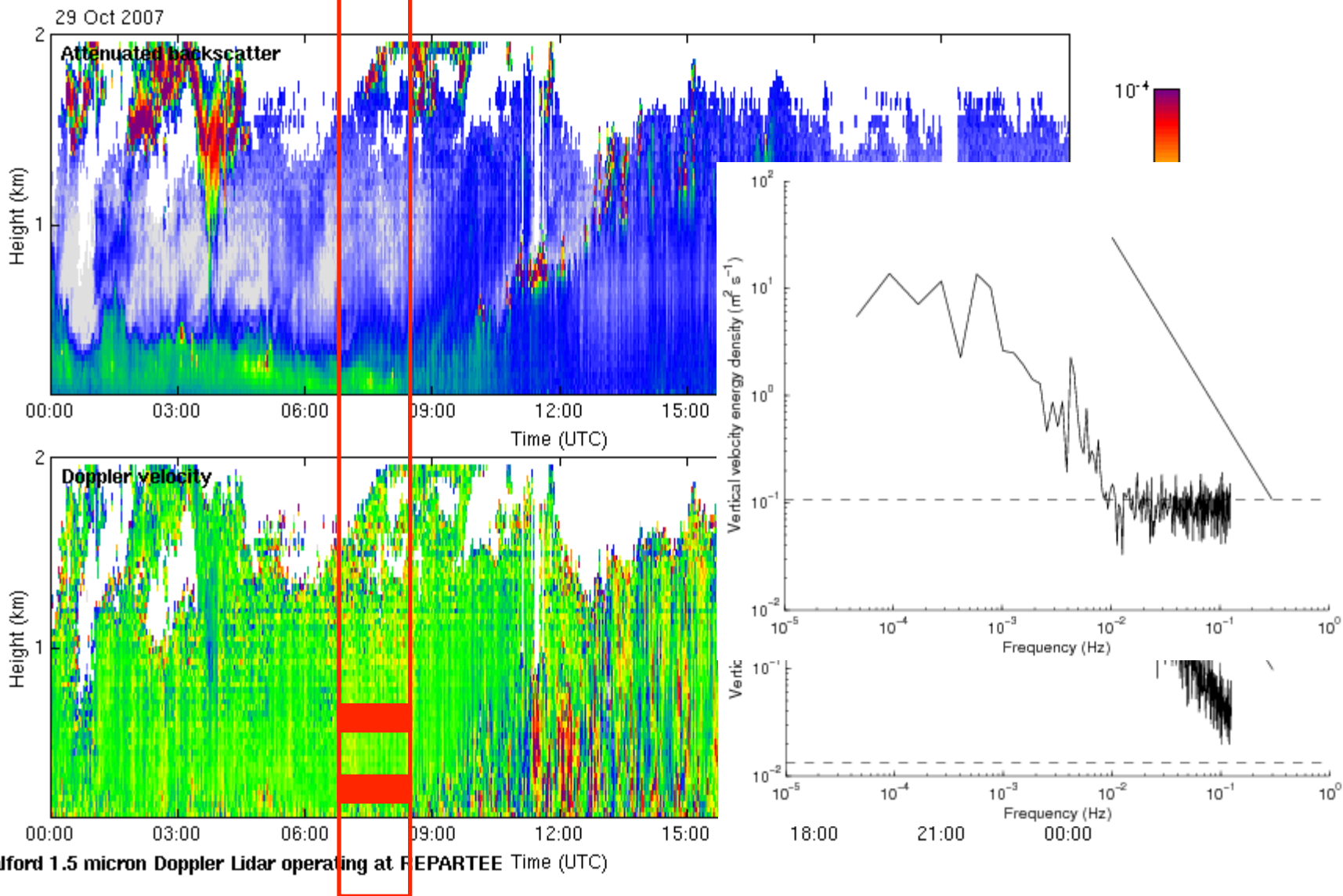
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Measurements



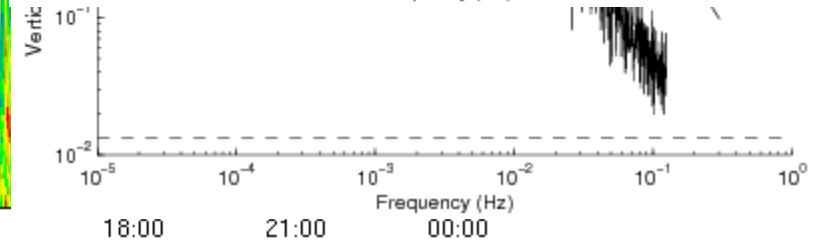
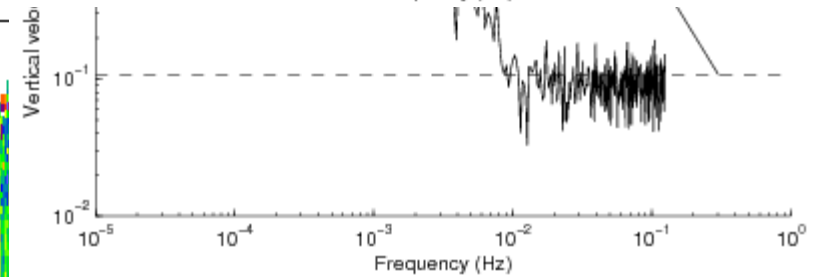
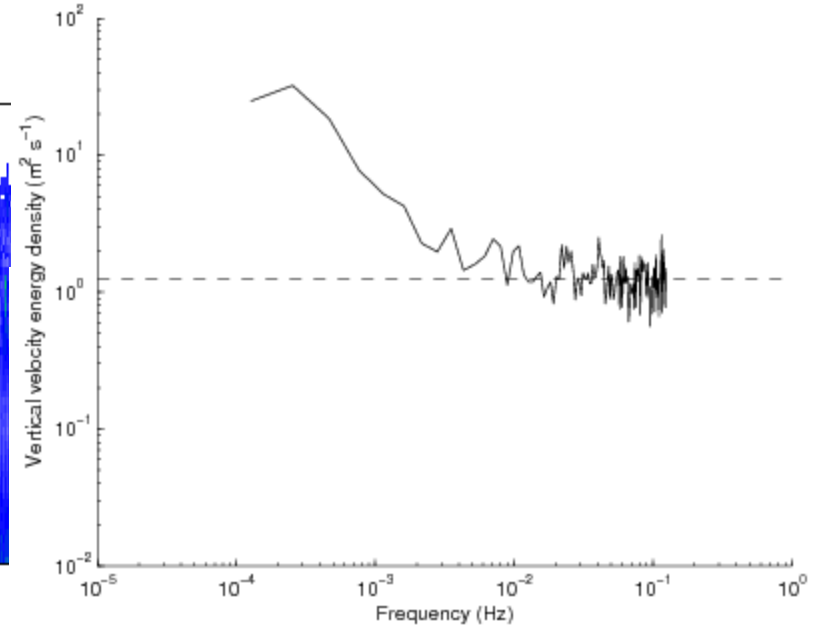
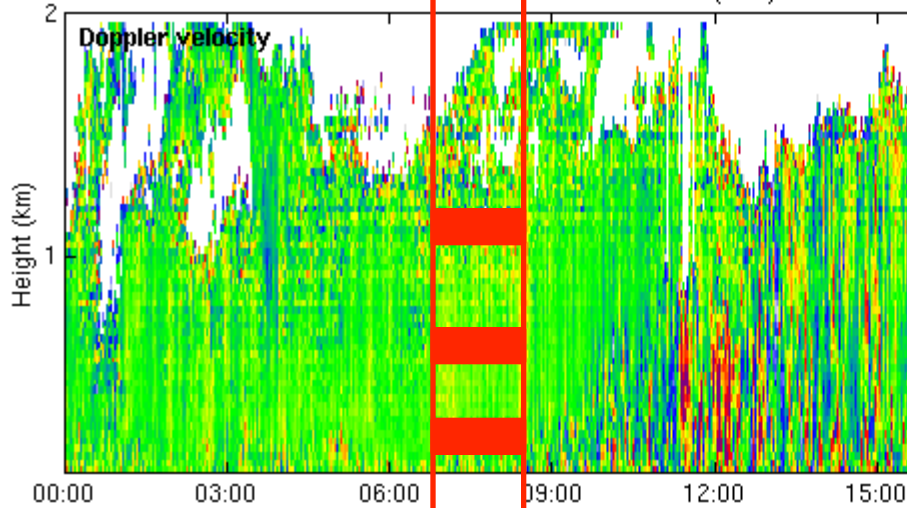
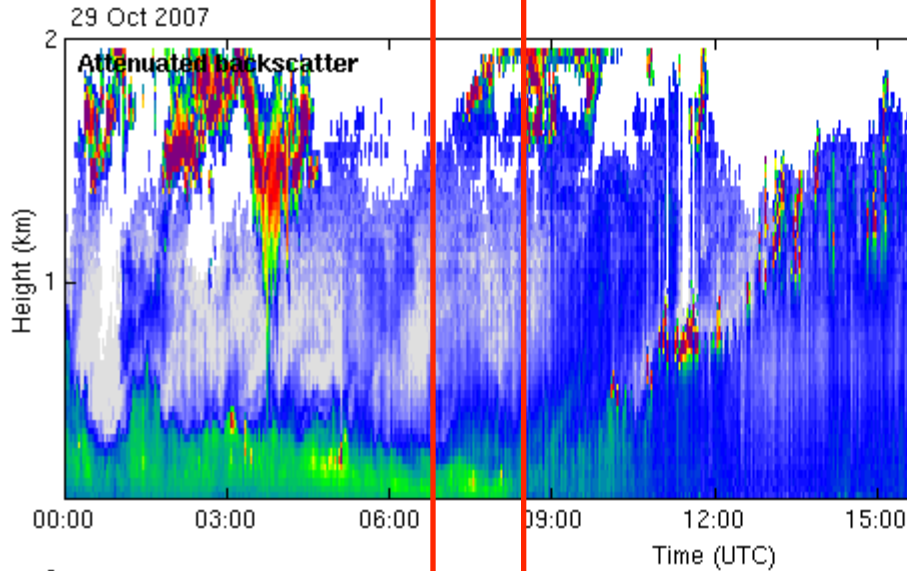
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Measurements



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Salford 1.5 micron Doppler Lidar operating at REPARTEE Time (UTC)



Calculate dissipation rate (after correcting variance)

$$\sigma_{\bar{v}}^2 = \sigma_{\bar{w}}^2 + \sigma_e^2 + \sigma_d^2,$$

Observed variance

Turbulent term

Measurement uncertainty

Droplet fall speed distribution

$$\Delta\sigma_{\bar{w}}^2 \approx \sigma_{\bar{w}}^2 \sqrt{\frac{4}{N} \frac{\sigma_e^2}{\sigma_{\bar{w}}^2}},$$

Uncertainty in variance



Fractional error in epsilon

$$\frac{\Delta\epsilon}{\epsilon} = \frac{3\Delta\sigma_{\bar{w}}}{\sigma_{\bar{w}}} + \frac{\Delta L}{L}.$$

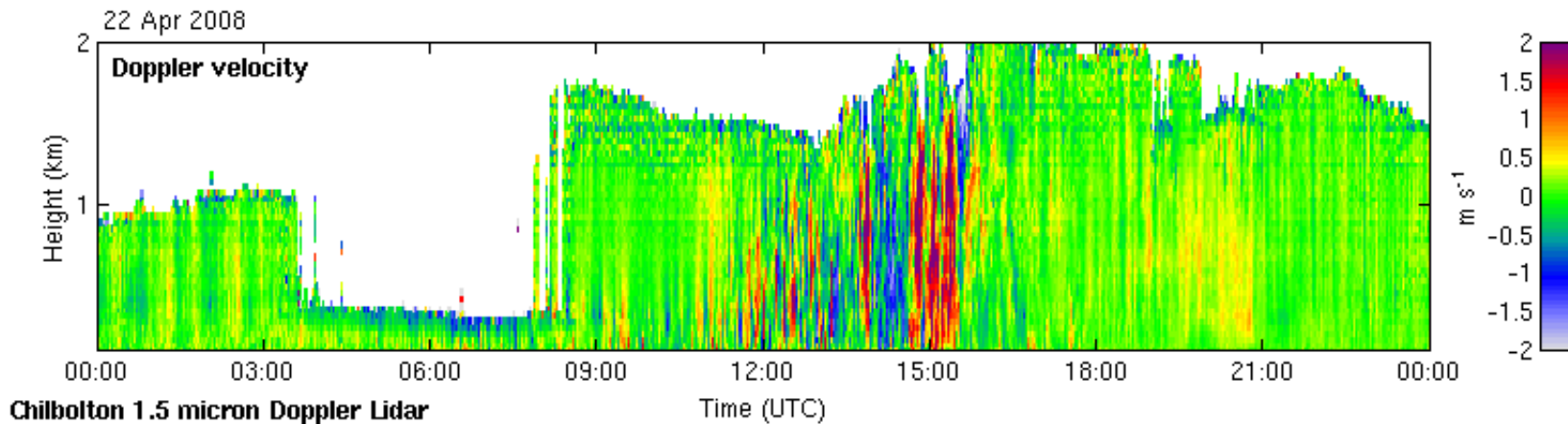
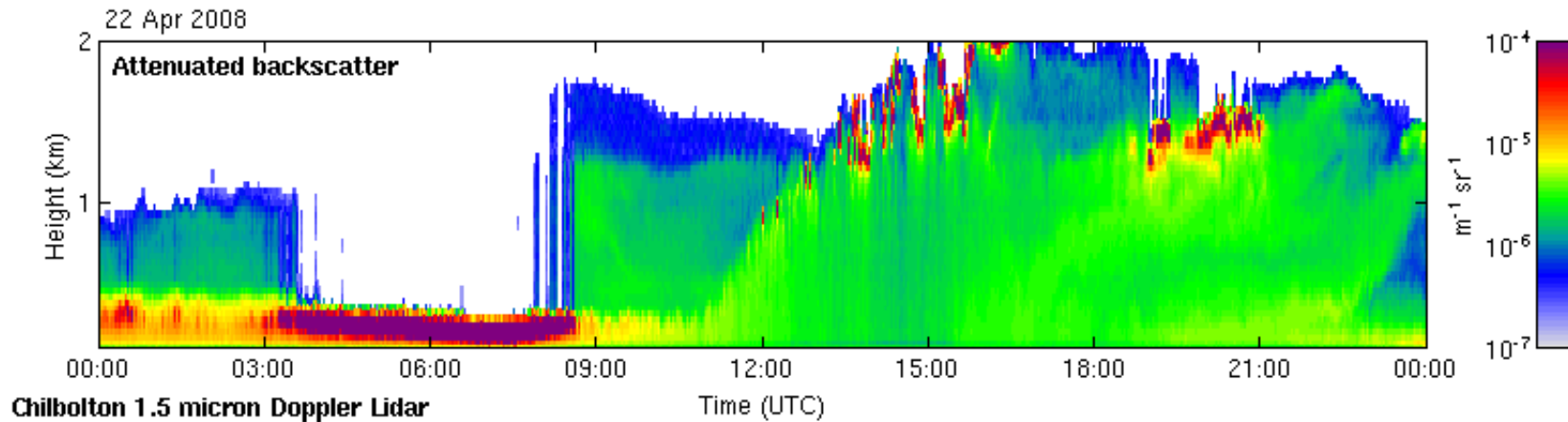
$$L = Ut + 2z \sin\left(\frac{\theta}{2}\right),$$

Uncertainty in length scales
derived from horizontal winds

$$\Delta\sigma_{\bar{w}}^2 \approx \sigma_{\bar{w}}^2 \sqrt{\frac{4}{N} \frac{\sigma_e^2}{\sigma_{\bar{w}}^2}},$$

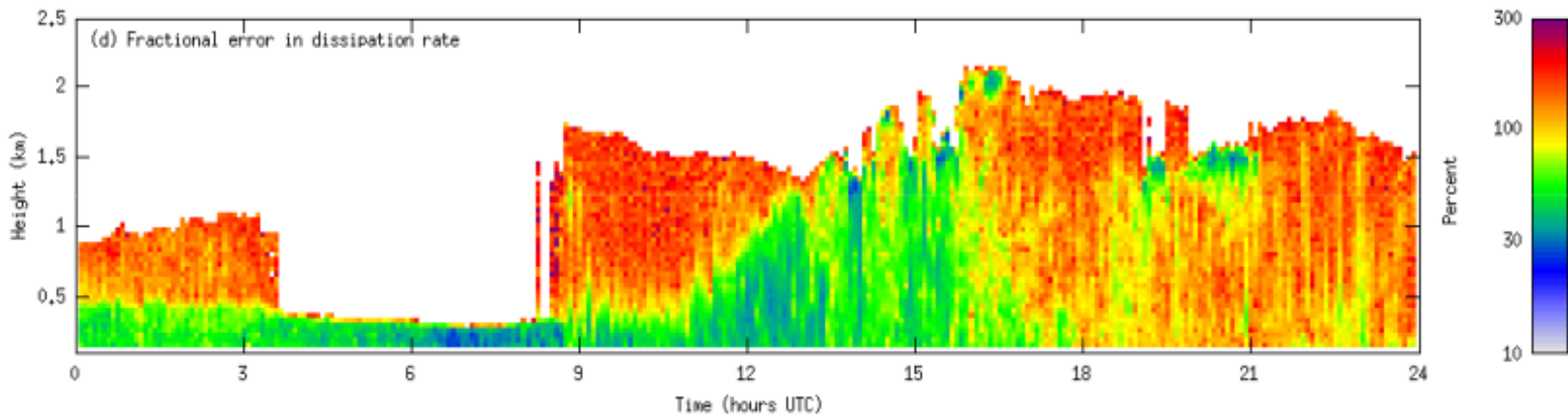
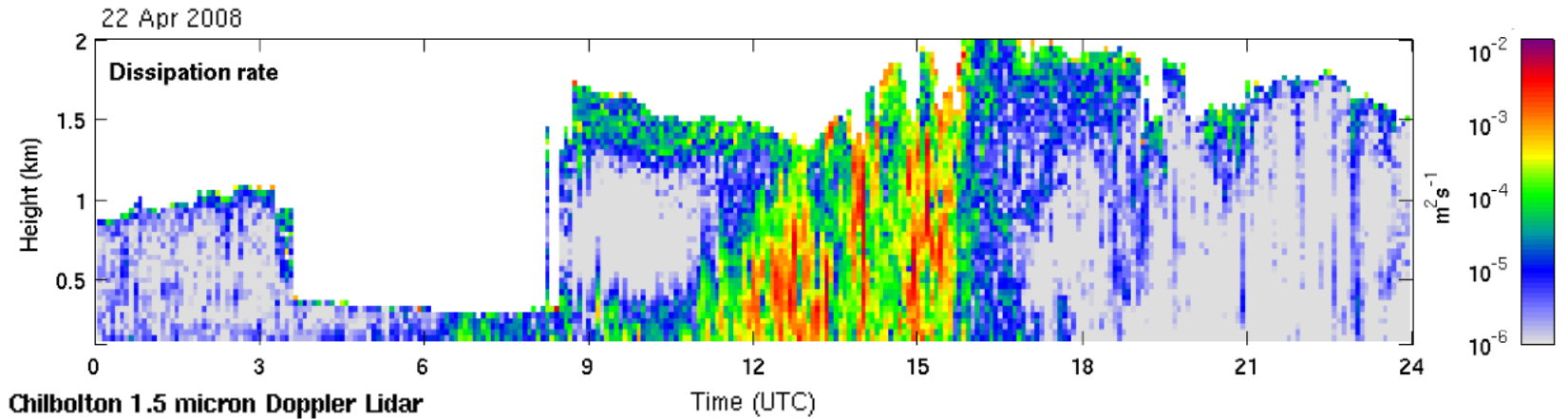


Doppler Lidar data for 22 April 2008



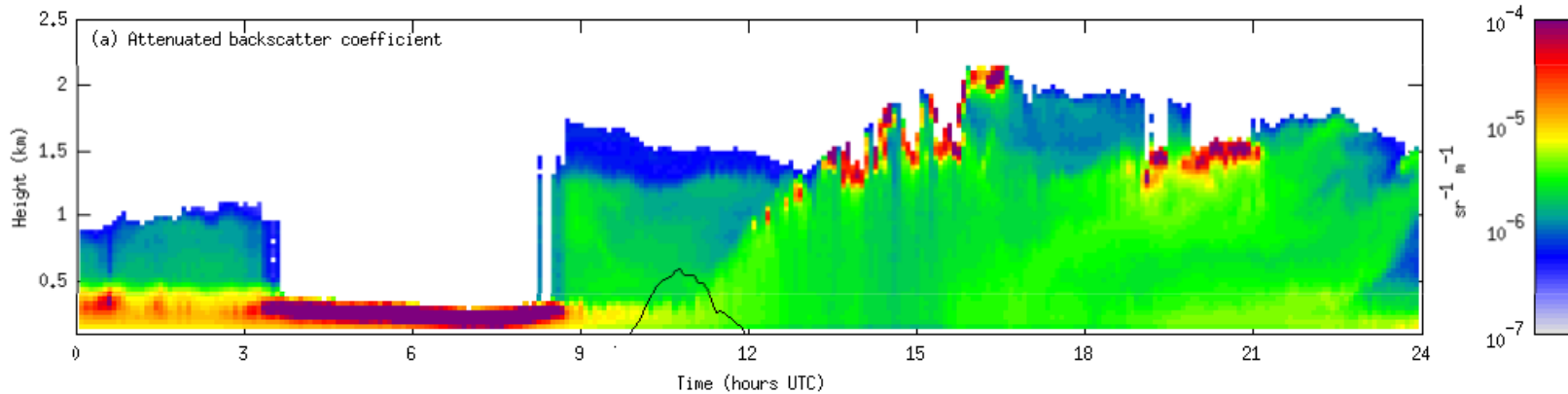


Turbulence

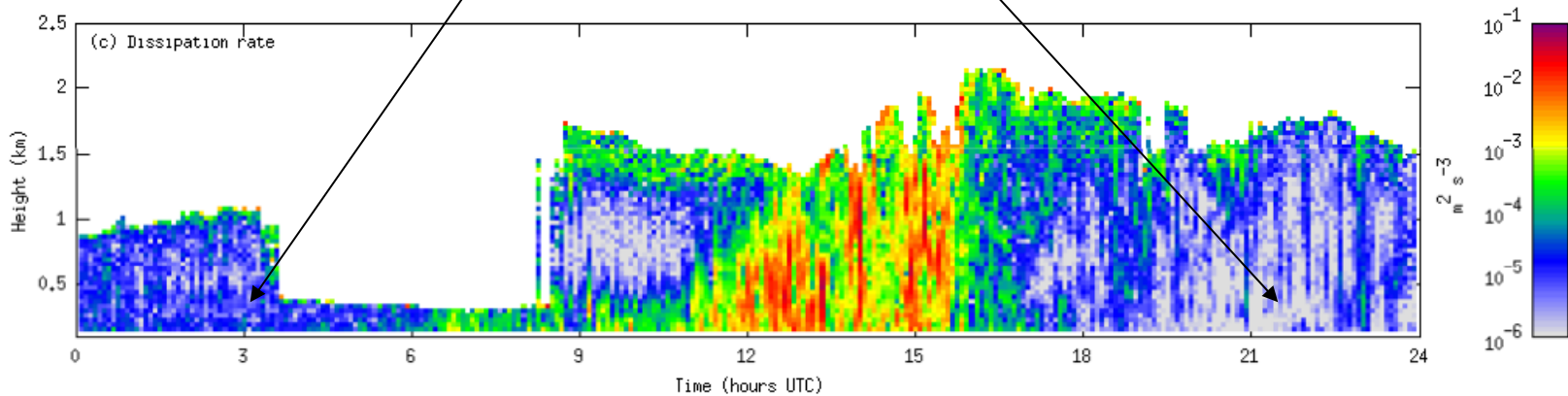




Chilbolton (*Rural*): 20080422



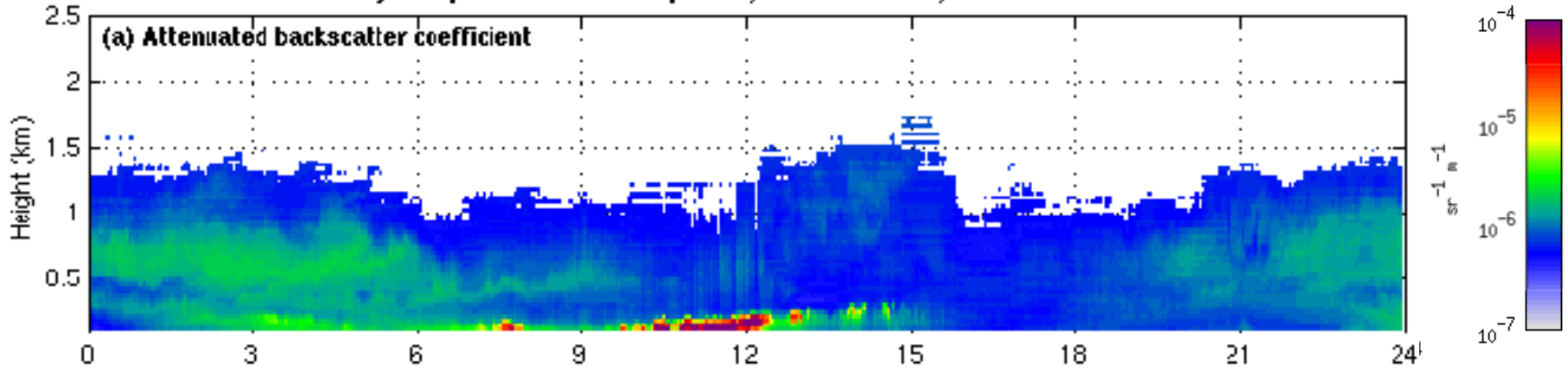
No turbulent layer at night





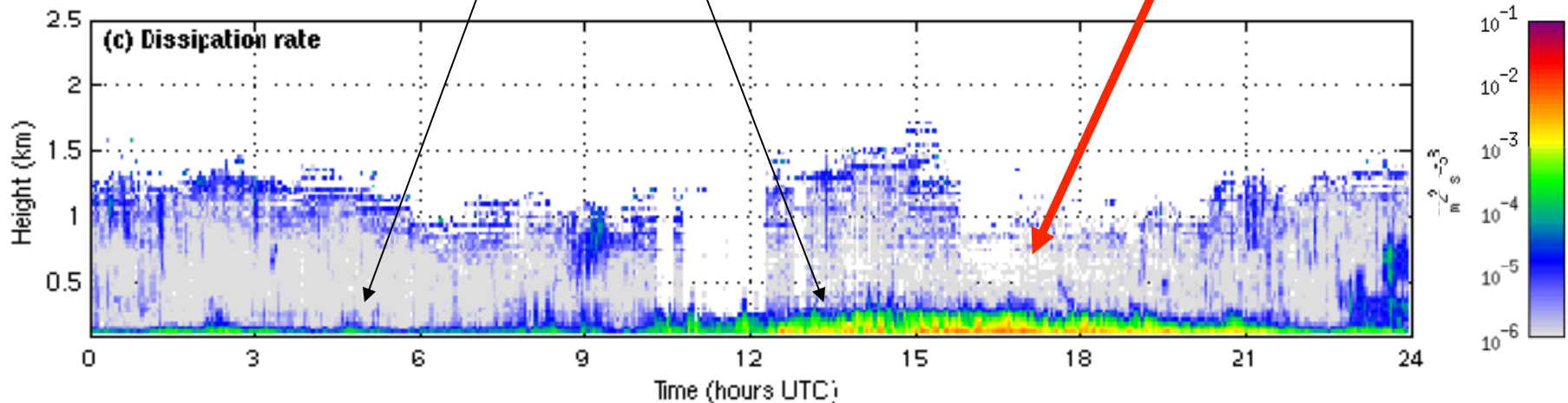
Cape Cod (Marine): 20120803

20120803 Turbulent eddy dissipation rate from Cape Cod, Massachusetts, US



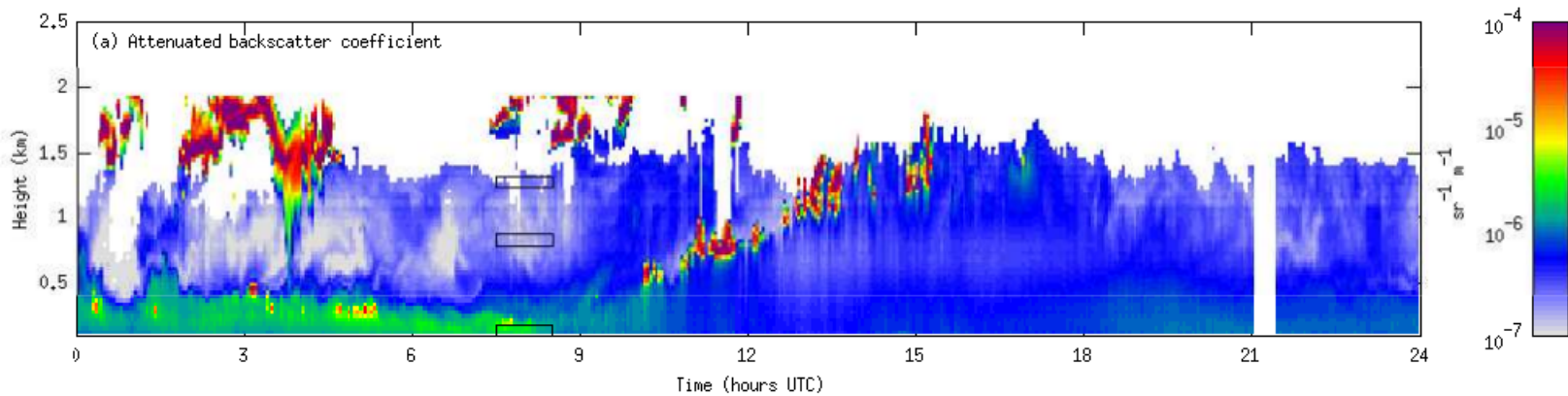
Turbulent layer at surface throughout diurnal cycle

Solar noon

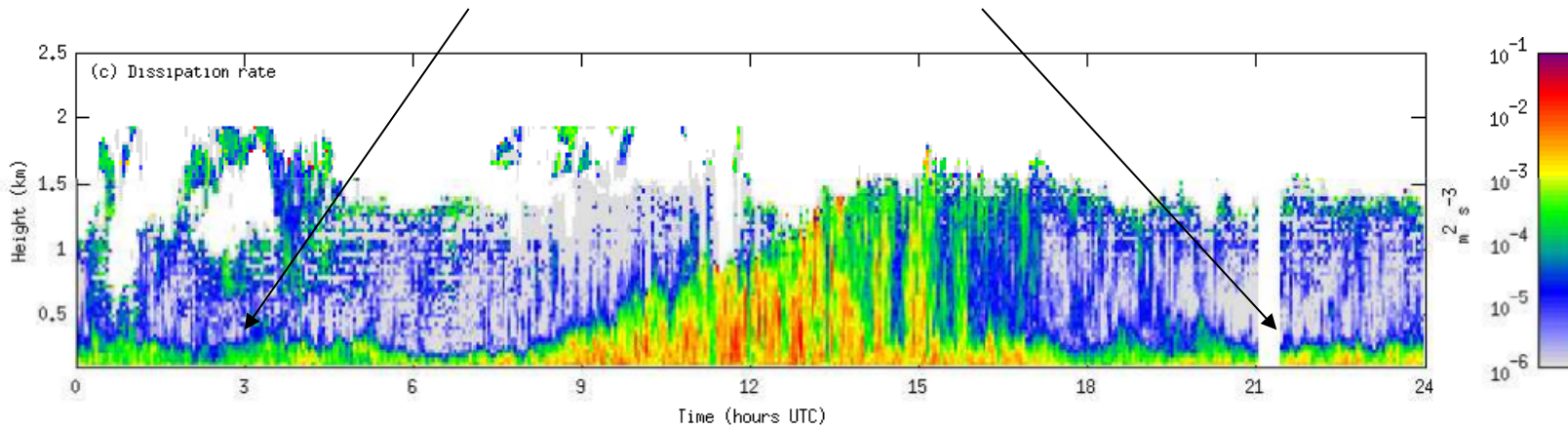




London (Urban): 20071029

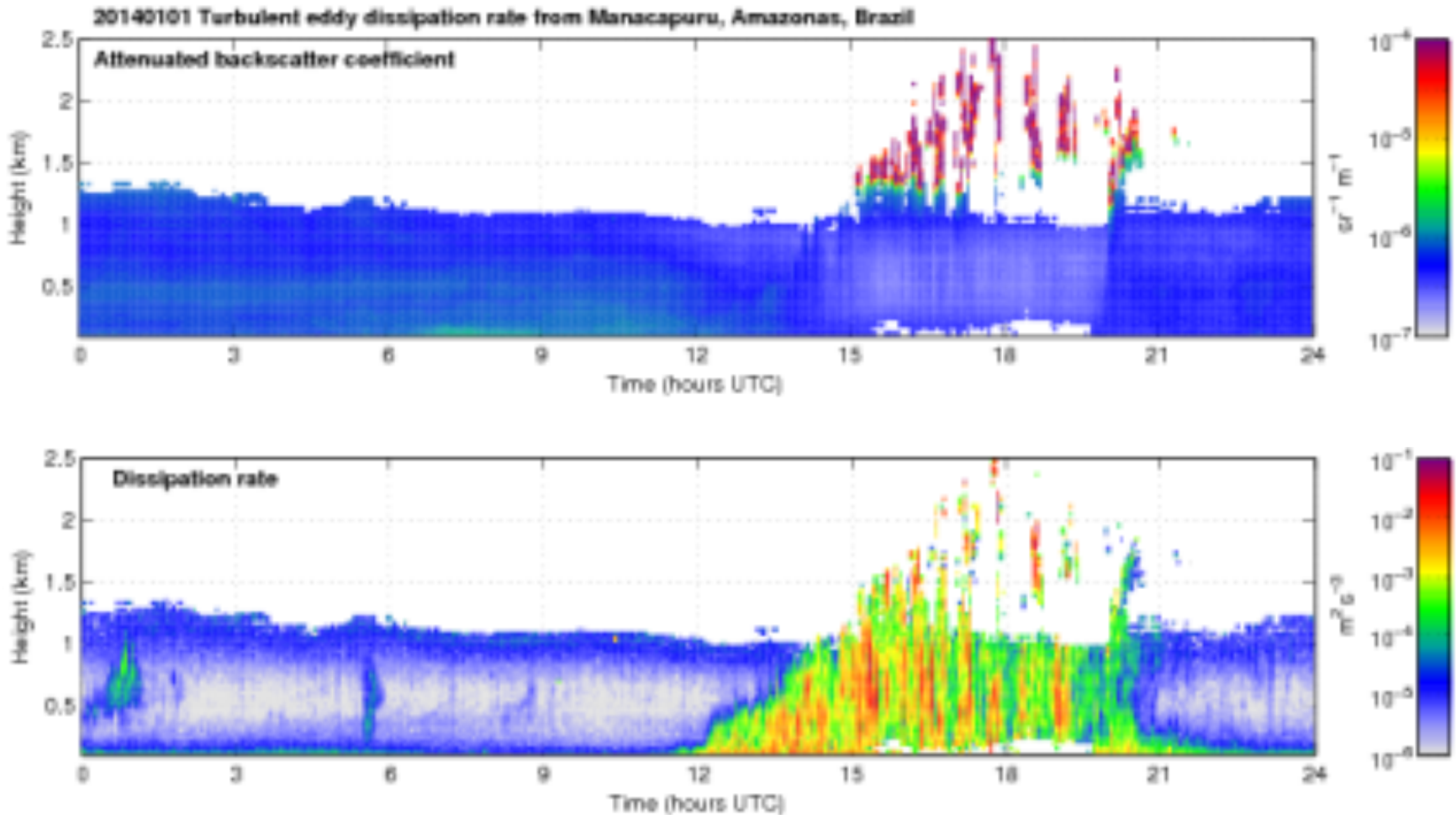


Turbulent layer at surface throughout diurnal cycle



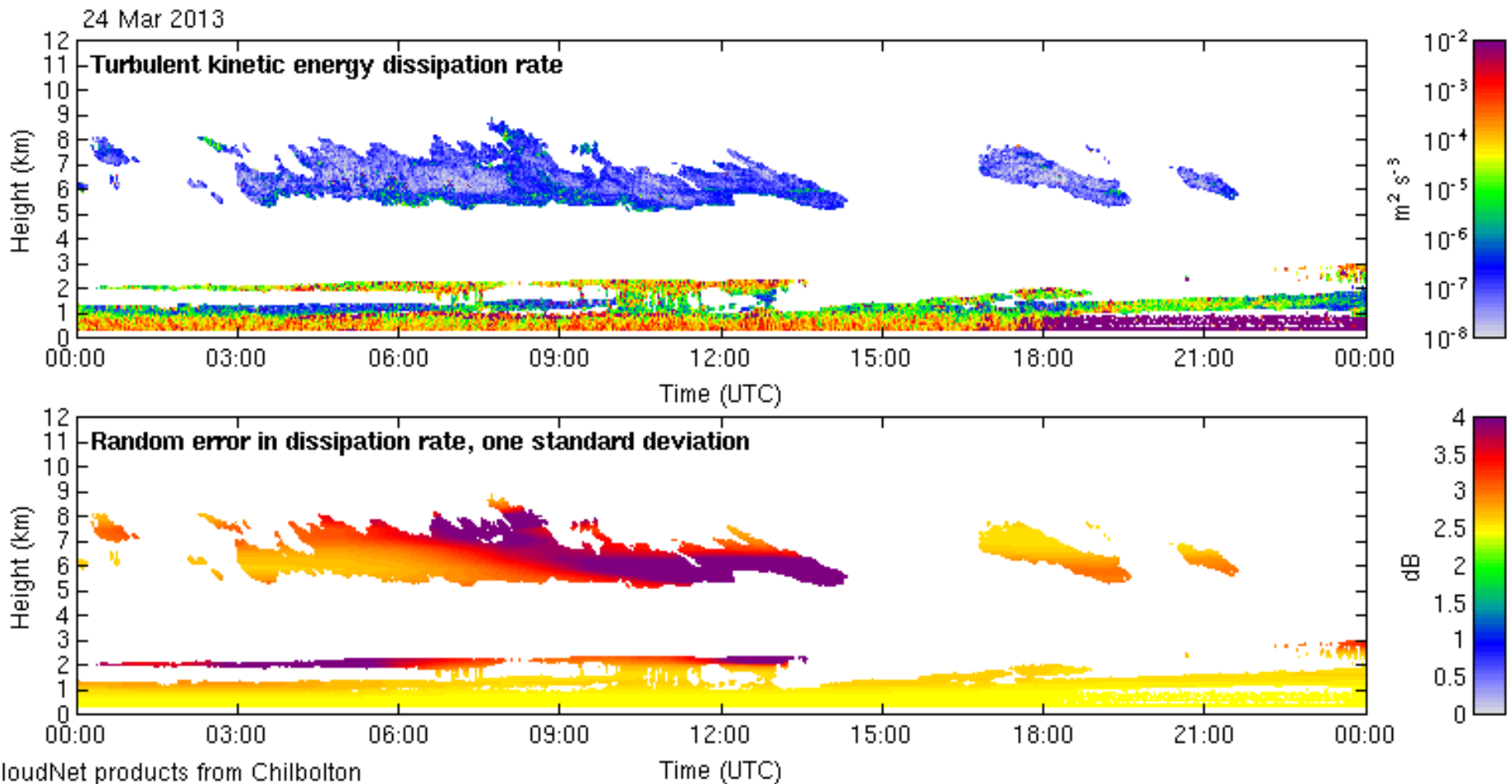


Amazon (rainforest): 20140101





Similar technique for cloud radar





SoDAR (Sonic Detection and Ranging)

- **Sodar operating principles**
 - Sound propagation
 - Pulse type
- **Sodar measures turbulence**
- **Sodar measures radial velocity**
 - How do we get horizontal wind?
 - DBS scans
 - Instrument type
 - Multi-beam
 - Phased-array



Operating principles – sound propagation

- **Sodar emits a pulse of sound**
- Energy is scattered by localised fluctuations in refractive index for acoustic waves (in all directions)
 - Fluctuations may be in temperature, humidity, velocity
- Backscattered energy from the transmitted pulse measured
 - Signal strength gives measure of turbulence
 - Doppler shift in signal gives radial velocity
- For monostatic sodar system, backscattered energy is caused by thermally-induced turbulence only



Operating principles – sound propagation

Backscatter at arbitrary angle (θ)

$$\sigma(\theta) = 0.03k^{1/3} \cos^2 \theta \left[\sin\left(\frac{\theta}{2}\right) \right]^{-11/3} \left[\frac{C_V^2}{c^2} \cos^2\left(\frac{\theta}{2}\right) + 0.13 \frac{C_T^2}{T^2} \right]$$

$$k = 2\pi/\lambda,$$

T is temperature in K,

C_V = structure function constant for velocity,

C_T = structure function constant for temperature



Operating principles – sound propagation

Backscatter at 180 degrees

$$\sigma(\pi) = (0.03k^{1/3}) \left(0.13 \frac{C_T^2}{T^2} \right) = 0.0039k^{1/3} \frac{C_T^2}{T^2}$$

$$k = 2\pi/\lambda,$$

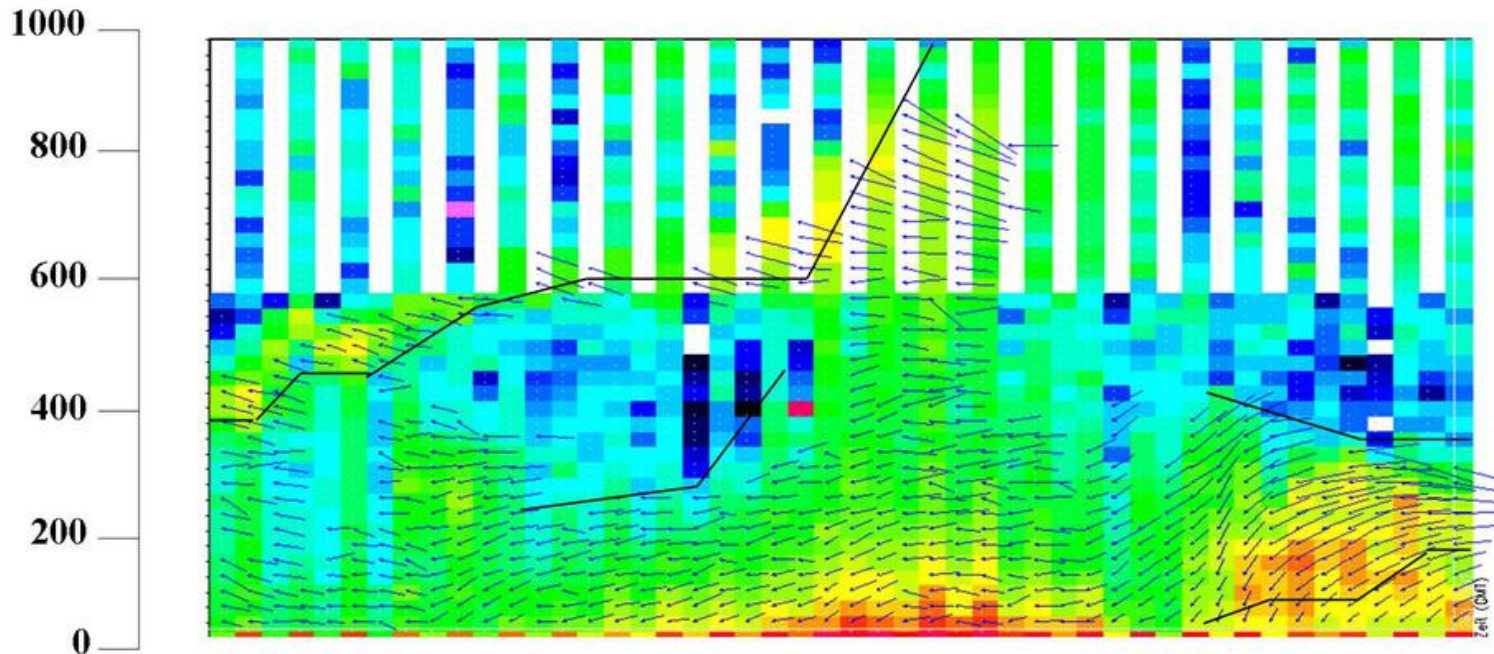
T is temperature in K,

C_T = structure function constant for temperature



Operating principles – sound propagation

Backscatter is a measure of turbulence



Courtesy: Stefan Emeis



Operating principles – velocity

The speed of sound in an ideal gas is

$$v_{sound} = \sqrt{\frac{\gamma RT}{M}} \quad \text{where}$$

γ = adiabatic constant
 R = gas constant
 M = molecular mass of gas
 T = absolute temperature

For air, $\gamma = 1.4$ and average M (DRY) = 28.95 gm/mol.

$$v_{sound} = \sqrt{\frac{1.4(8.314 \text{ J / mol} \cdot \text{K})}{.02895 \text{ kg / mol}}} \sqrt{T} = 20.05 \sqrt{T} \text{ m/s}$$

At $T = 273 \text{ K}$, $v_{sound} \sim 330 \text{ m s}^{-1}$ in dry air.



- **Consider a target at a range, R , from a sodar**
- **Total distance the pulse travels is $2R$**
- **Corresponding to:**
 - $2R/\lambda$ wavelengths, or
 - $4\pi R/\lambda$ radians of phase
- **Consider a target at range R , moving with velocity v , towards the sodar**
- **Change in phase due to the motion of the target between returned signals is**

$$\phi_2 - \phi_1 = \frac{4\pi R_2}{\lambda} - \frac{4\pi R_1}{\lambda}$$



- **The rate of change in phase detected at sodar**

$$\frac{d\phi}{dt} = \frac{4\pi v}{\lambda}$$

- **This can be described as a frequency shift since**

$$\frac{d\phi}{dt} = 2\pi\nu$$

- **The Doppler frequency shift**

$$\nu_D = \frac{2v}{\lambda}$$

- **Doppler frequency shift tells us the speed that the target is moving**
- **For a given wavelength the frequency shift is dependent only on the velocity of the target**



- **Since $\lambda = c/f$, the Doppler frequency shift**

$$v_{\downarrow D} = 2fV/c$$

- **For a wind of 15 m s^{-1}**
 - Operating frequency = 1500 Hz
 - $v_D = 135 \text{ Hz}$
 - Operating frequency 5 kHz
 - $v_D = 455 \text{ Hz}$



Time between pulses?

Require no signal from 1st pulse contaminating 2nd pulse

$$R = ct/2,$$

Choice depends on sensitivity:

assume 6 s

gives $R \sim 990$ m



Range resolution?

Typical operating pulse lengths are about 0.01 s

Potential resolution is therefore 6.6 m

However, may use a coded pulse to improve sensitivity:

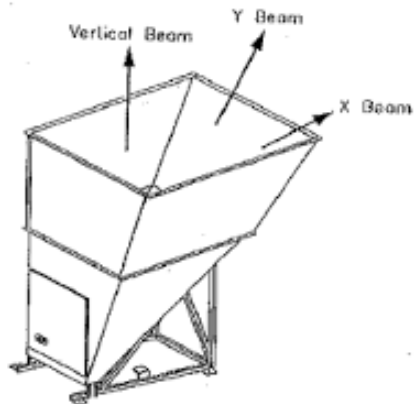
If this is 16 bits, pulse length = 0.16 s

First gate is >100 m

Resolution is theoretically similar to above but in practice smoother



Instrument configurations – 3 beam



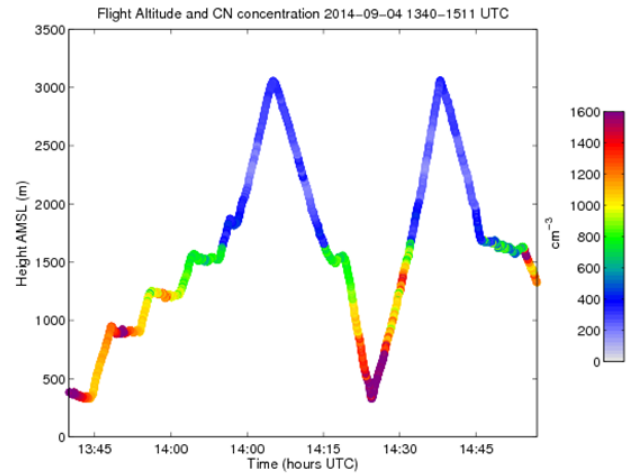
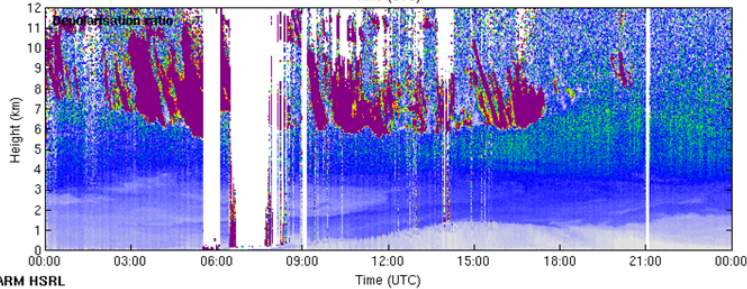
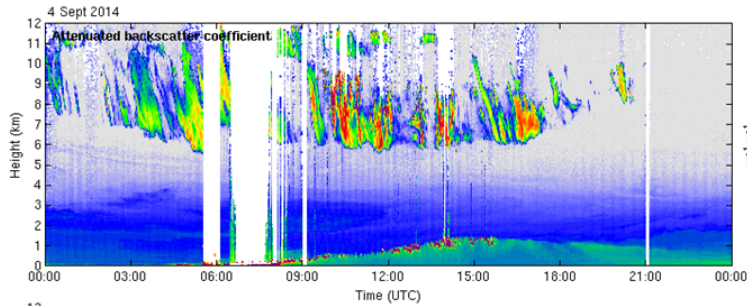
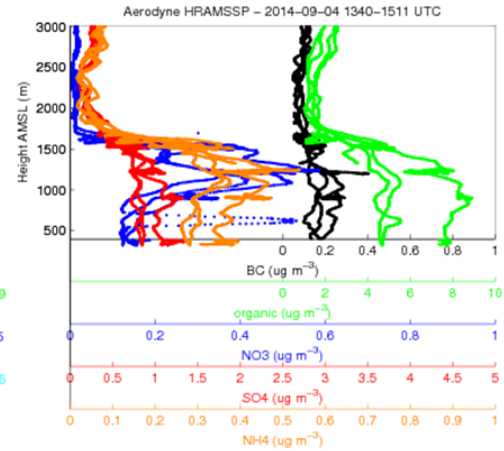
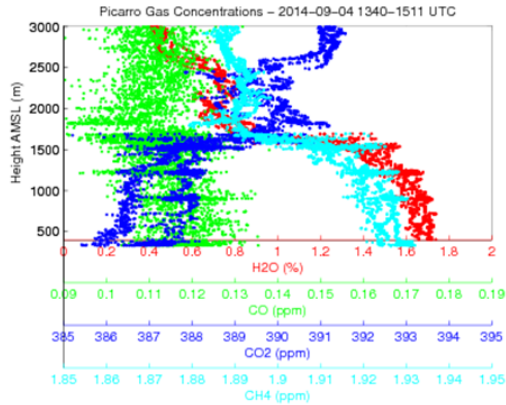
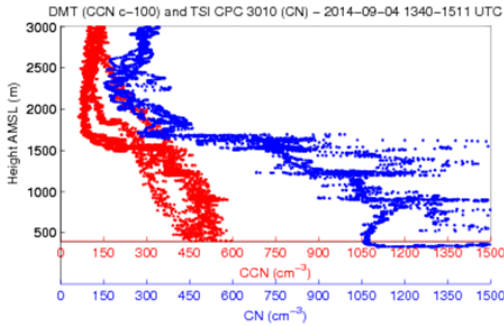


Instrument configurations – Phased array





Aerosol and trace gases





Aerosol as a tracer

- **mixing layer height (MLH) is important for many applications**
- **Most of current Retrievals are based on proxies:**
 - Potential Temperature determines how far up a parcel may rise
 - but starting temperature is often not well defined
 - t
 - Trace aerosol backscatter (gradient) is a proxy
 - S
 - t vertical wind is direct measure of mixing
 - Aerosol => Compare to validate MLH(aerosol)
 - Is a tracer with strongest source at the surface (see above)
 - But is also influenced by relative humidity
- **Mixing itself is vertical movement of air**
 - => vertical staring Doppler lidar measures mixing directly and instantenously



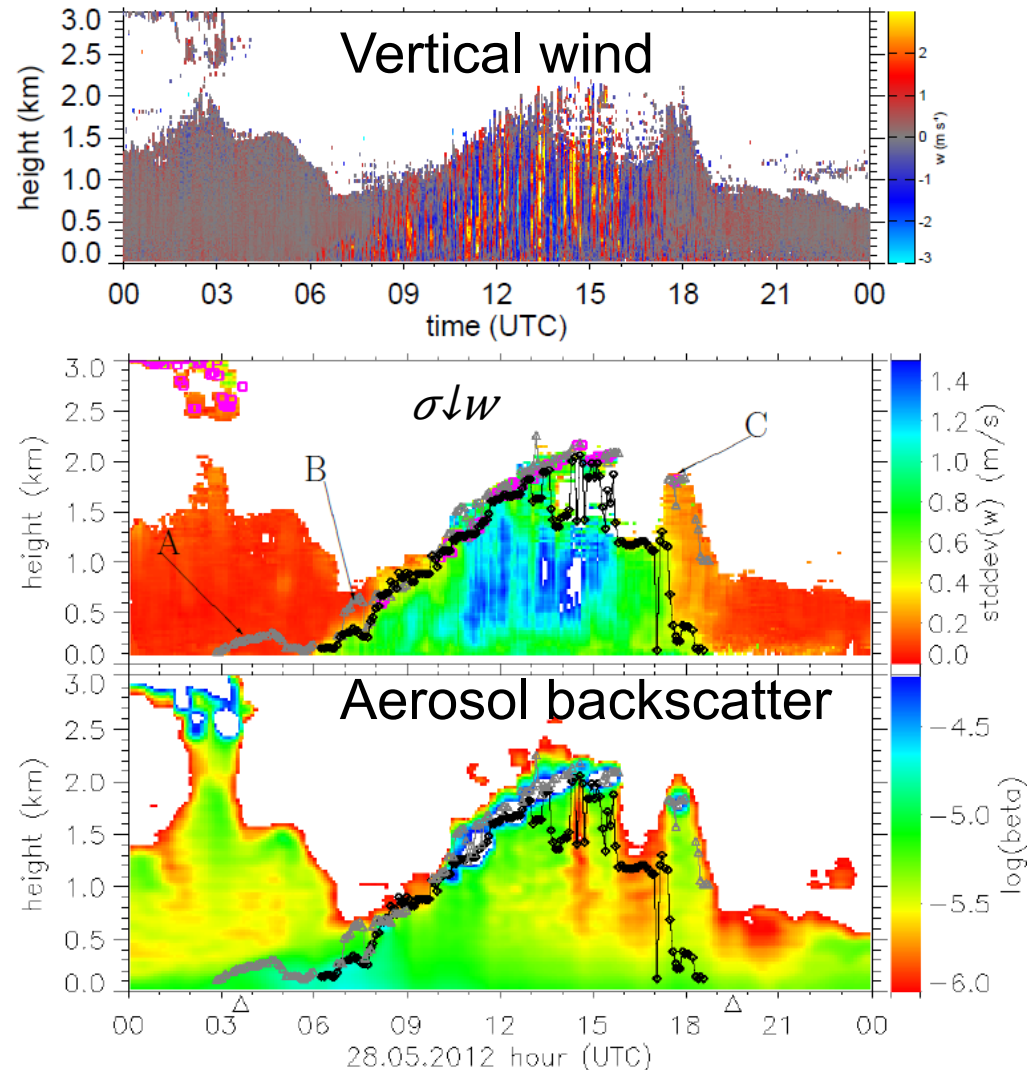
Compare in case study

- MLH_{wind} from $\sigma \downarrow w$ in black
- MLH_{aero} from aerosol in gray
- **General good agreement – but three periods where they disagree:**

A: late night: strong inversion, strong aerosol gradient due to high Rel.Humidity

B: morning: growth of MLH into RL with no clear gradient in aerosol backscatter between both layers

C: late afternoon decay of turbulence, aerosol reflects history but not current state of ML



Jan Schween (Köln, Germany)



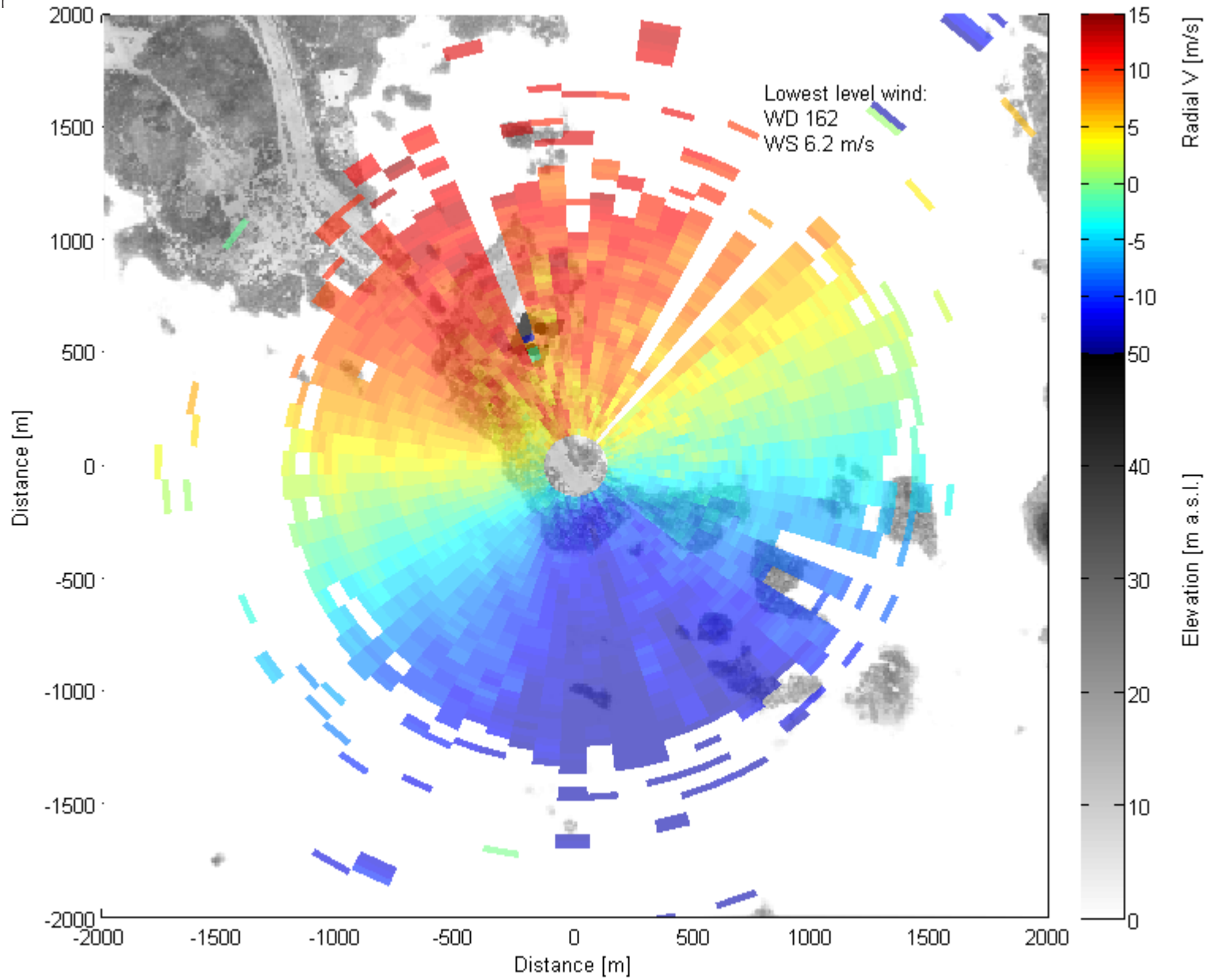
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METEOROLOGISKA INSTITUTET
FINNISH METEOROLOGICAL INSTITUTE



More complicated situations

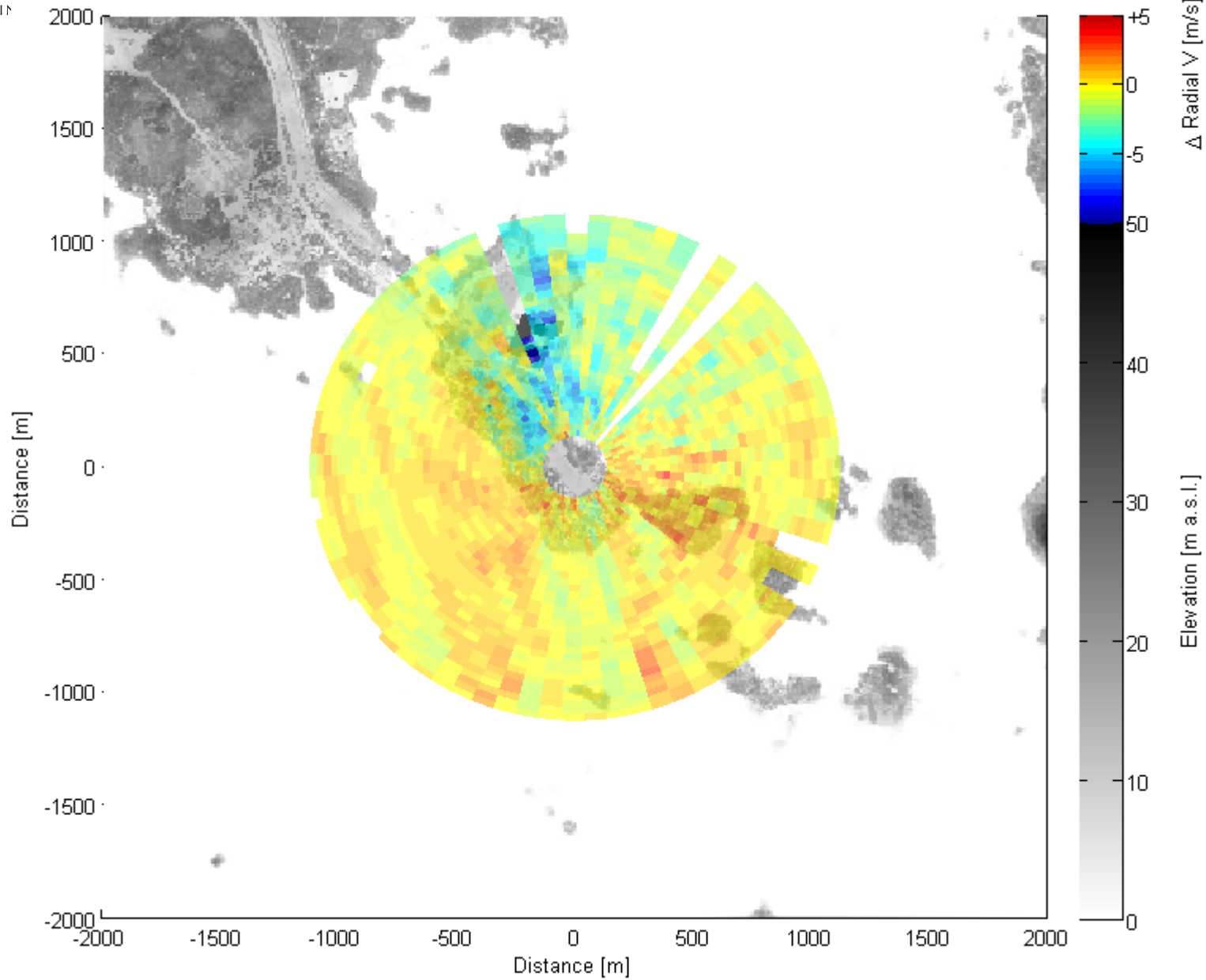


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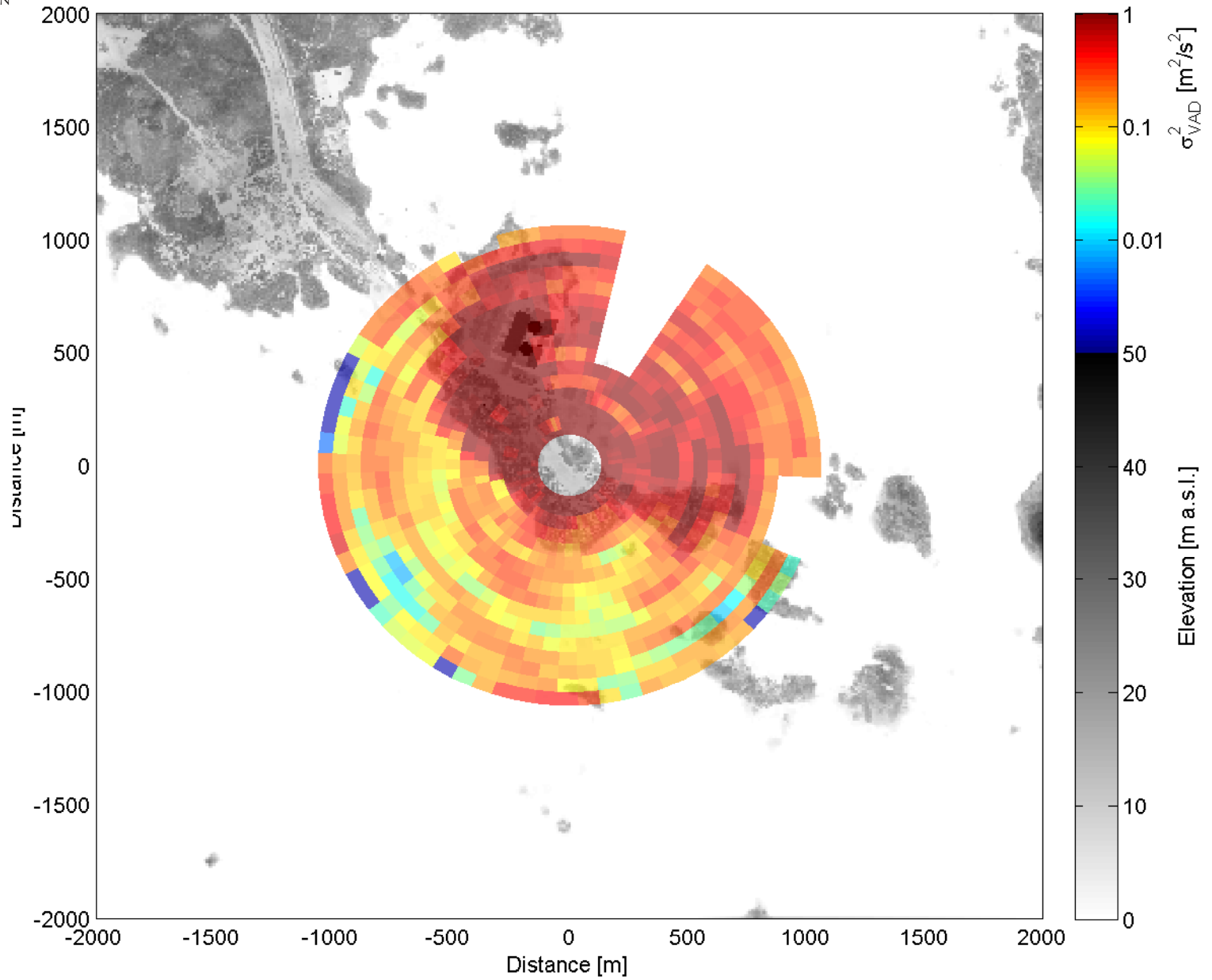


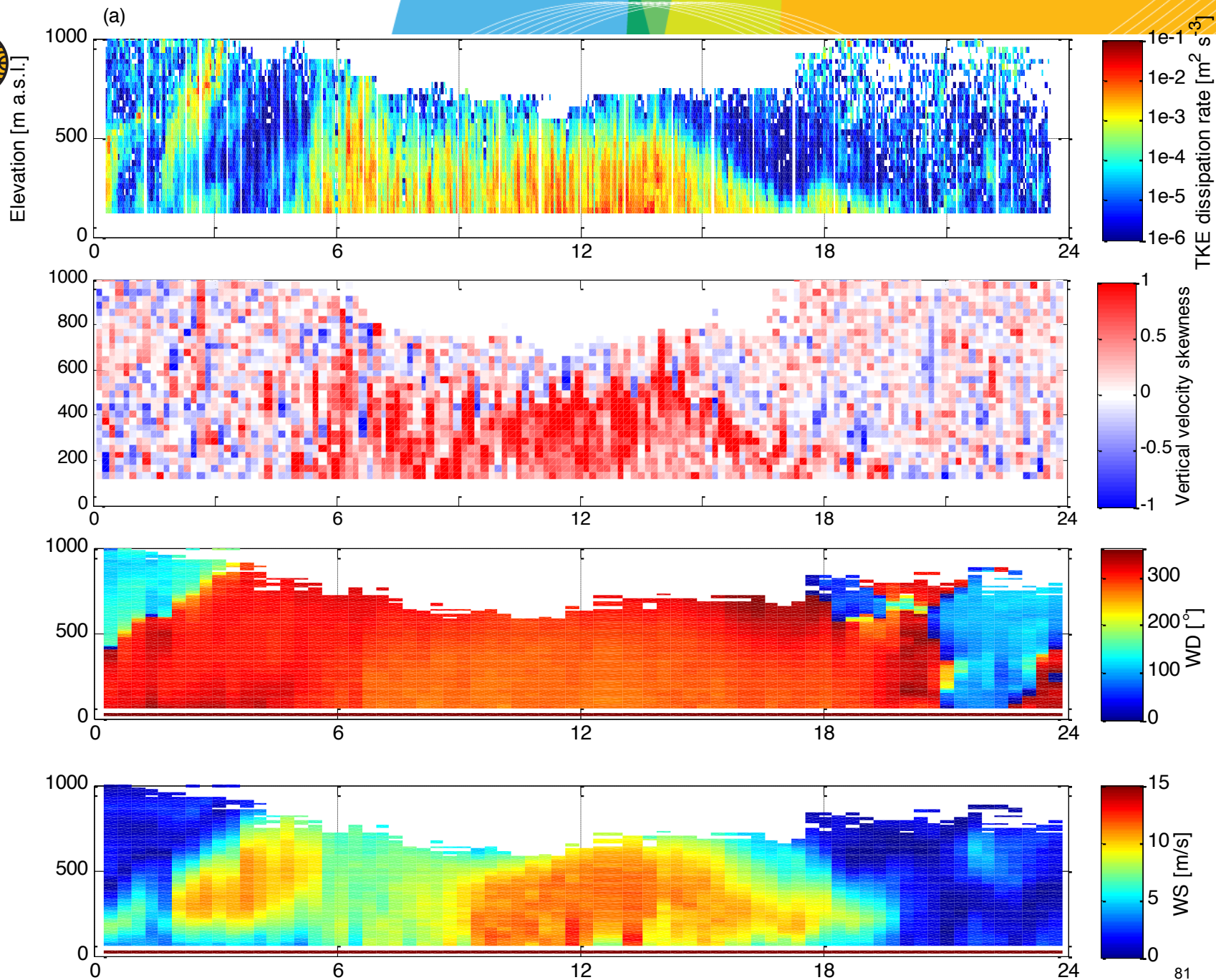
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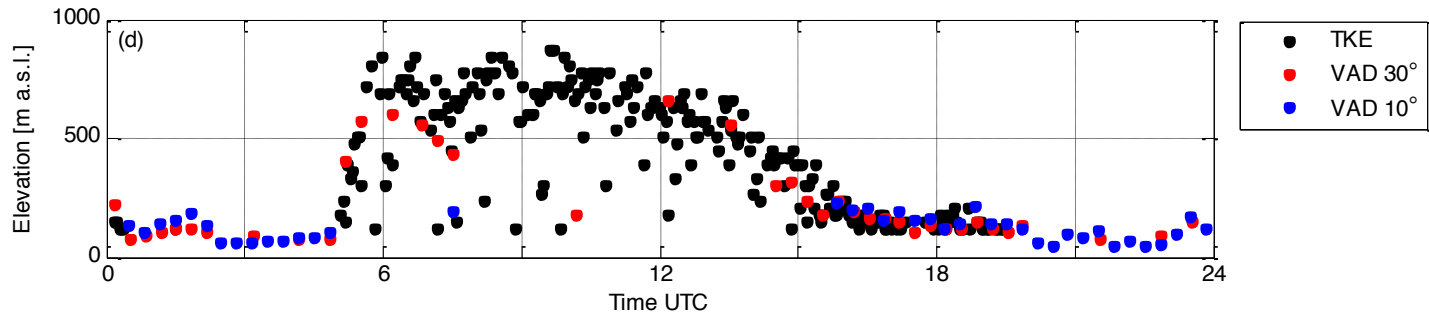
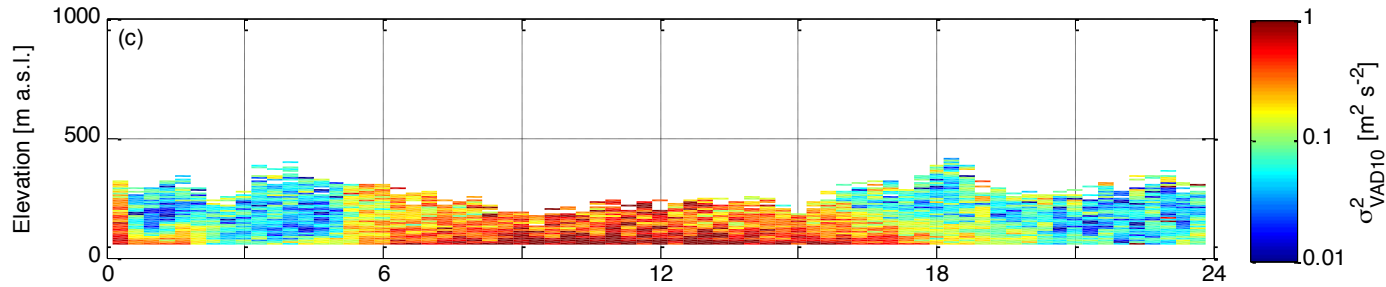
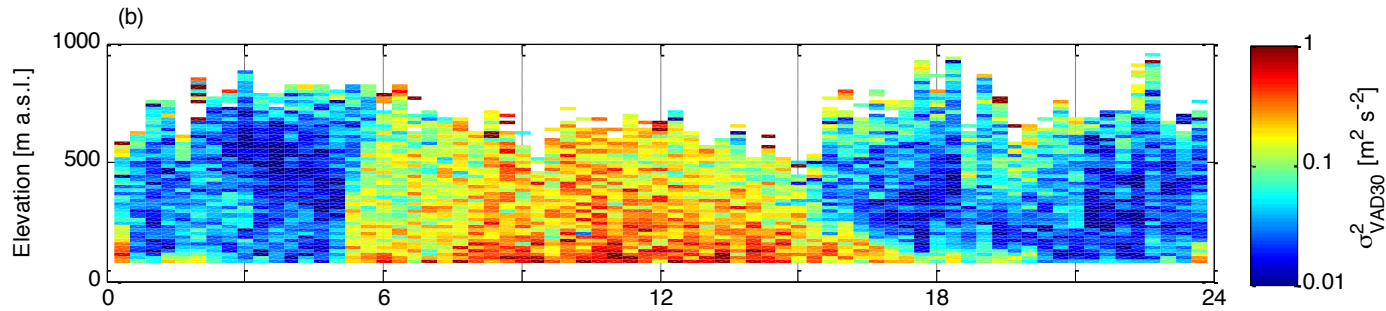
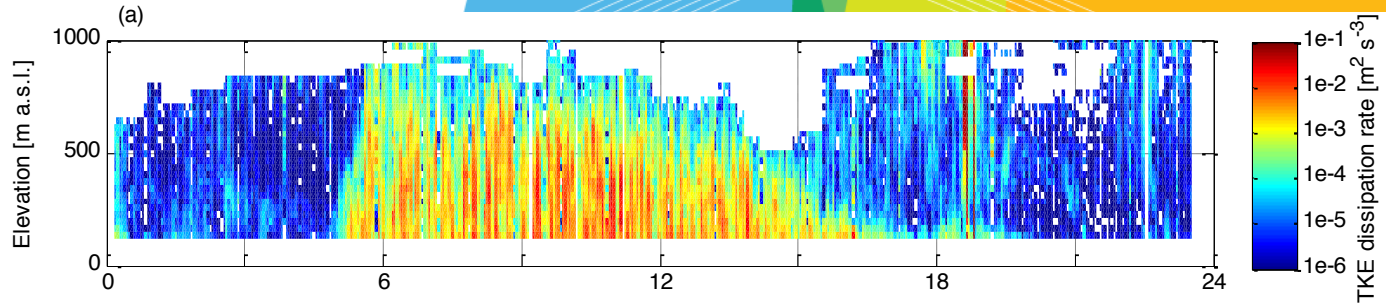




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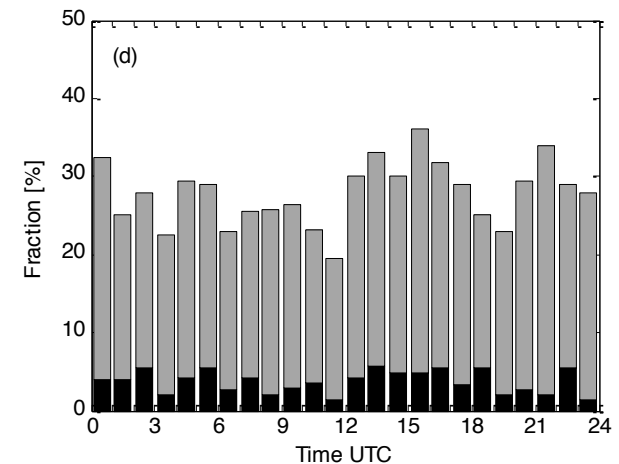
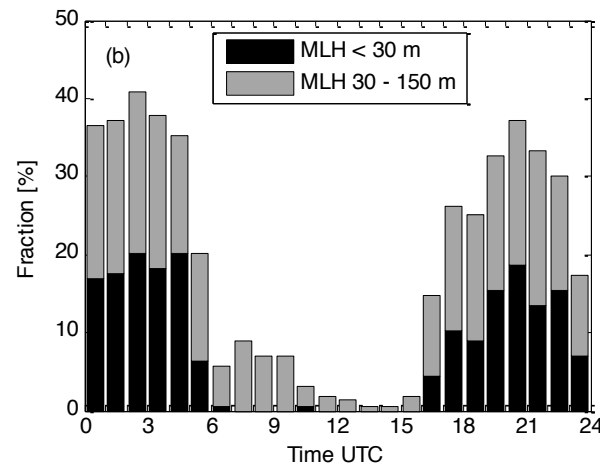
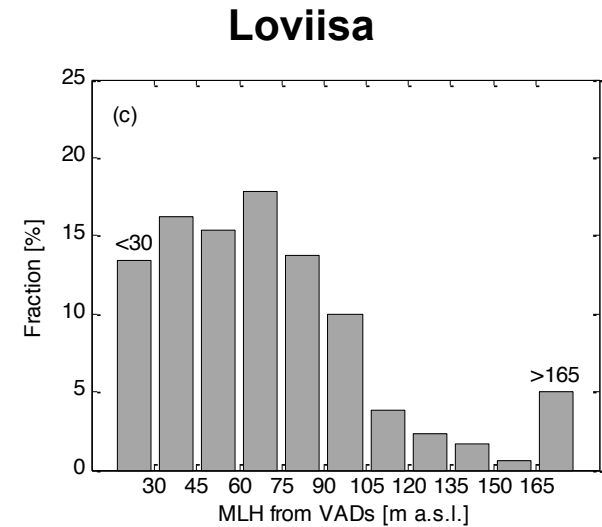
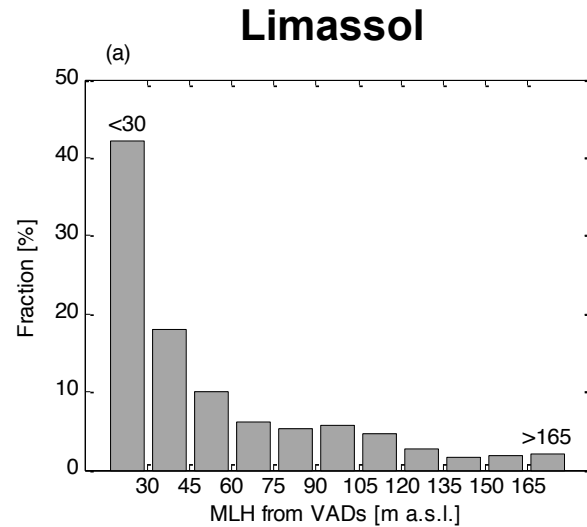


MLH
TKE $1e-4$
VADs 0.05



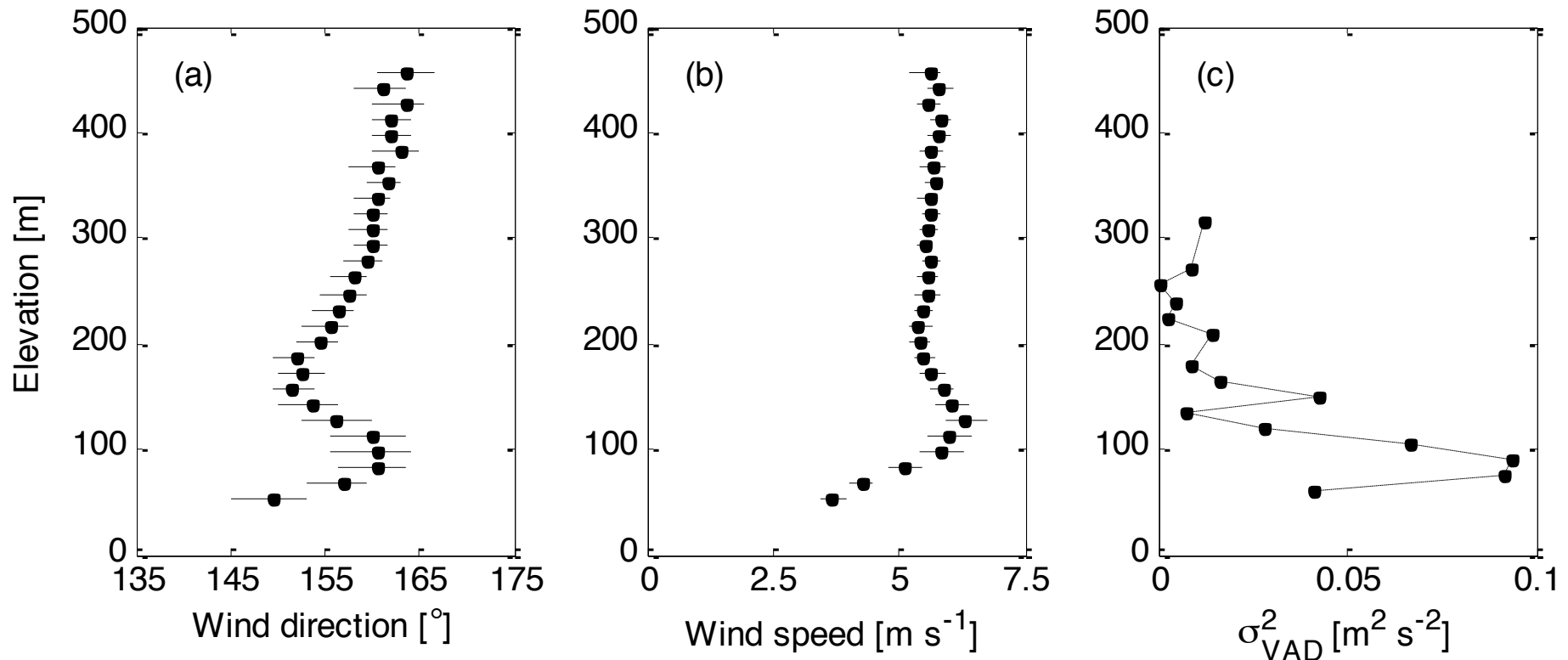
VADs identify frequently low MLH

No mixing in vertically-pointing:



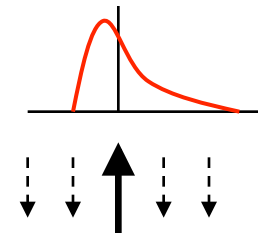
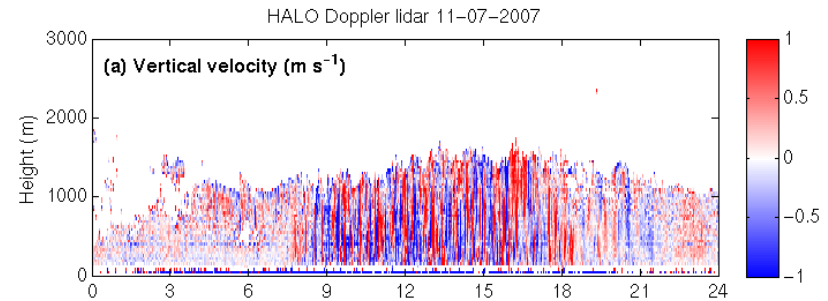
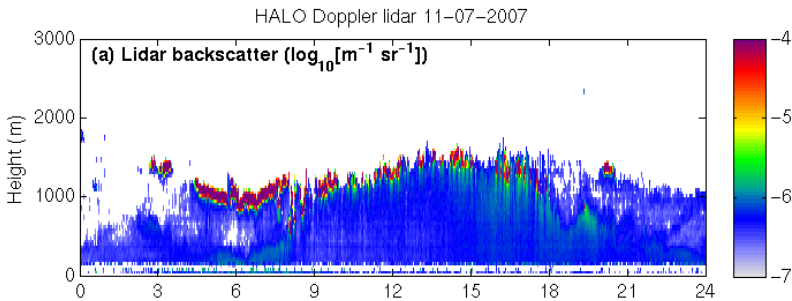
Hyytiälä, Finland, 3 August 2014 at 04:00 UTC

- “Continental” boreal forest
- Night-time turbulent mixing by a low level jet
 - Observed on 70% of nights in August 2014
 - 30° VAD





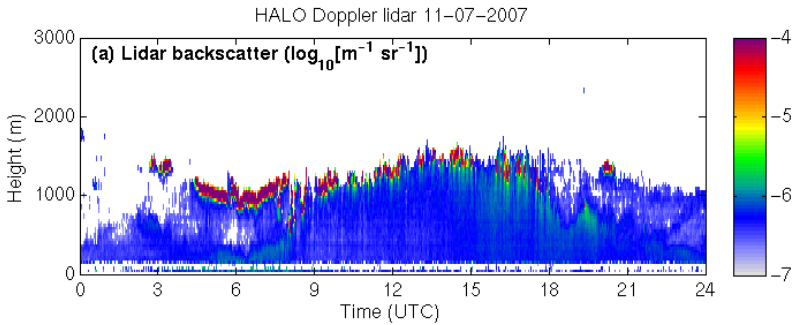
Vertical velocities



- Skewness defined as $s = \overline{w'^3} / \overline{w'^2}^{3/2}$
 - Positive in convective daytime boundary layers
 - Agrees with aircraft observations of LeMone (1990) when plotted versus the fraction of distance into the boundary layer
- Useful for diagnosing source of turbulence

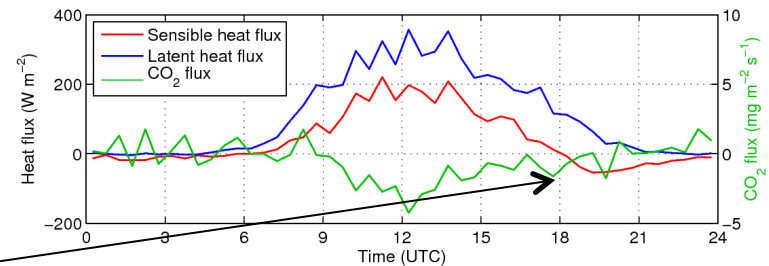
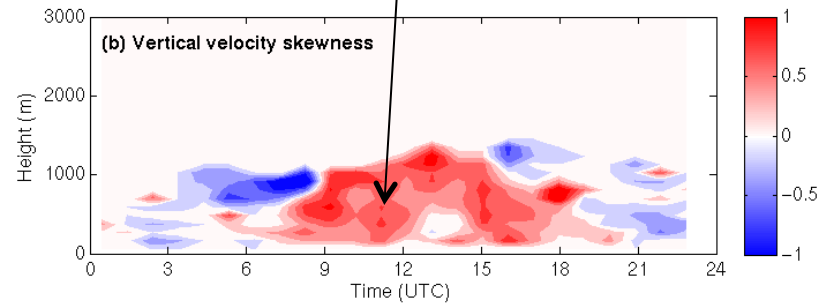
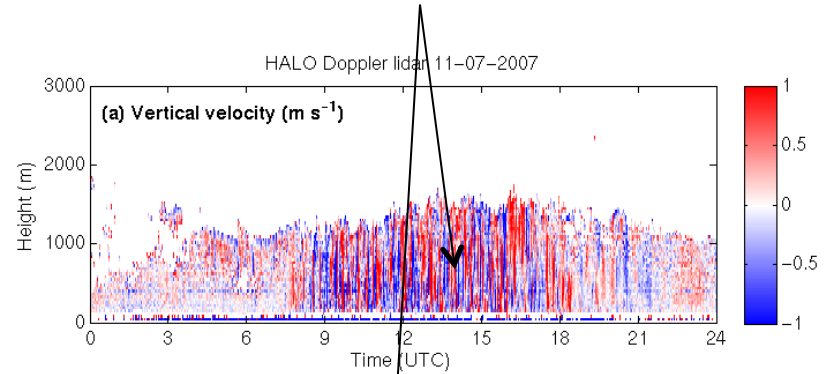


Vertical velocities

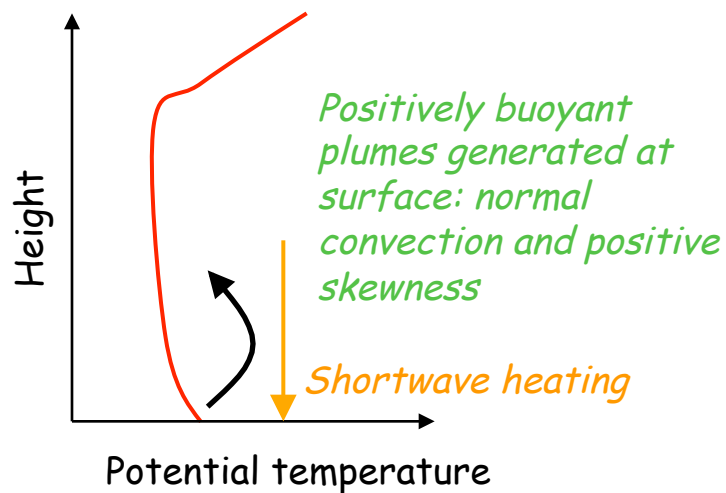
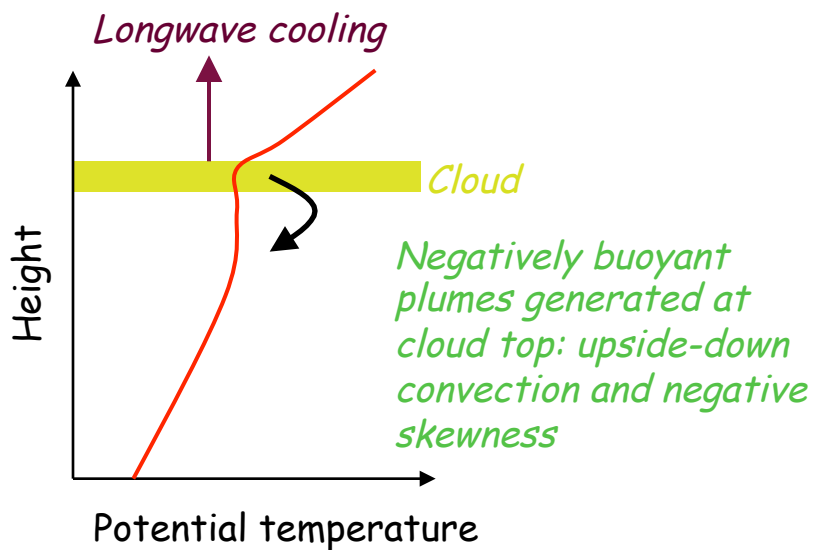
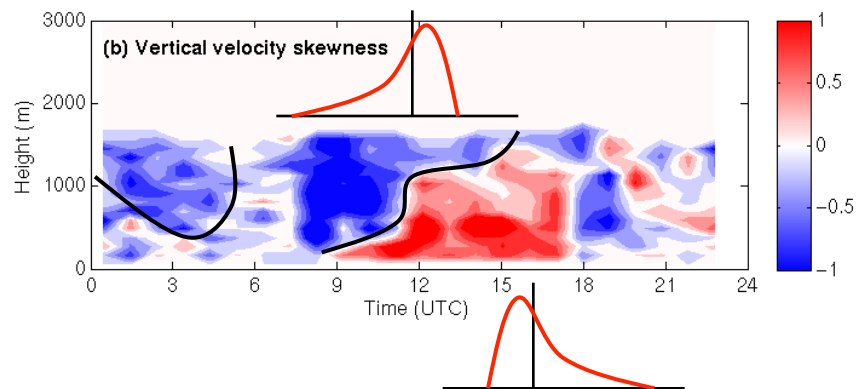
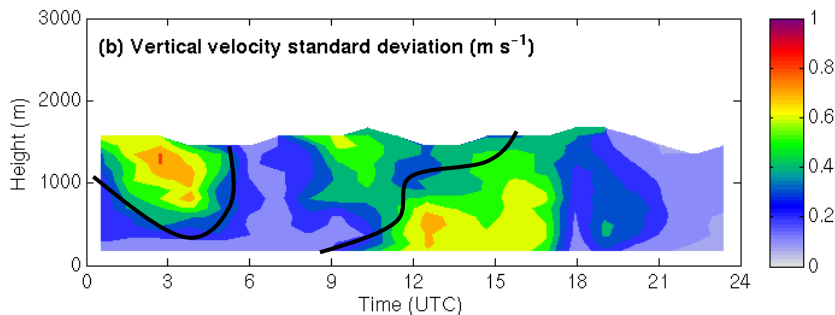
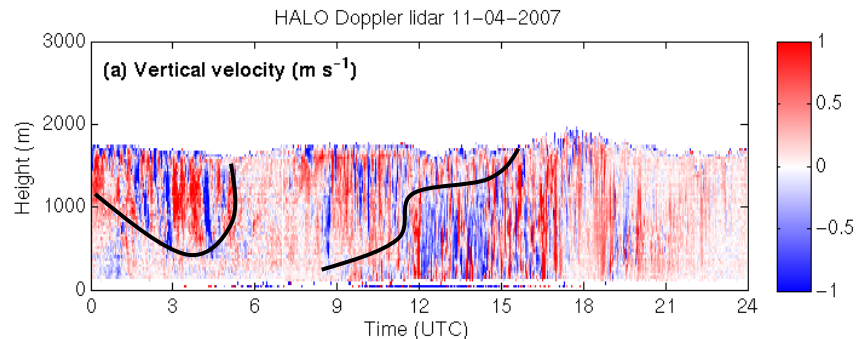
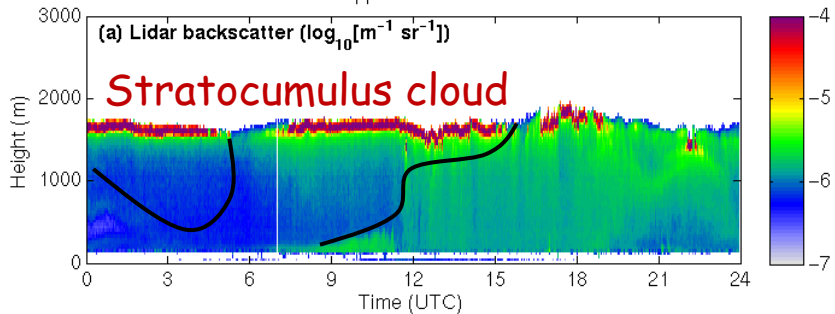


Input of sensible heat “grows” a new cumulus-capped boundary layer during the day (small amount of stratocumulus in early morning)

Surface heating leads to convectively generated turbulence

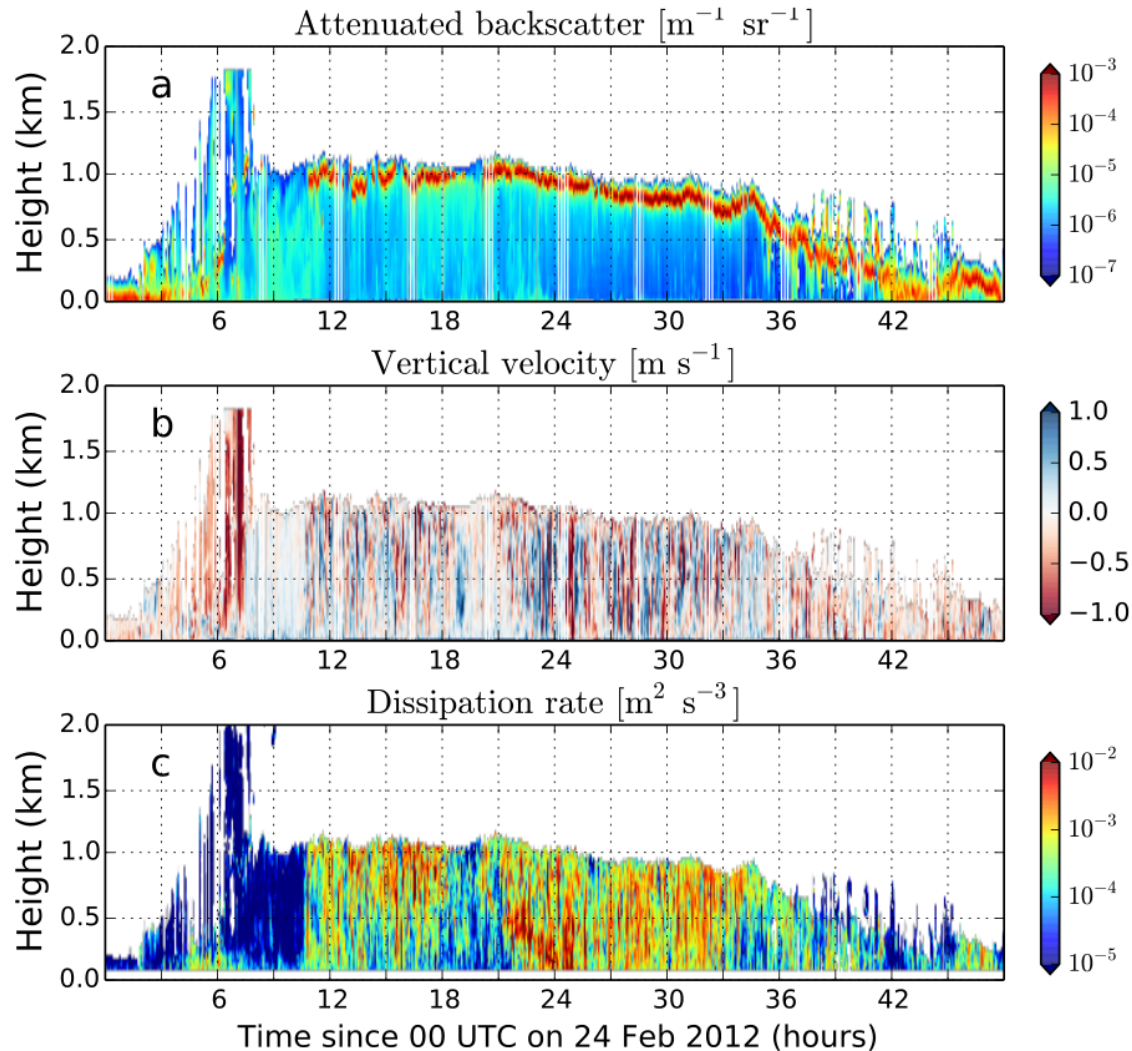


Convection is “switched off” when sensible heat flux goes negative at 1800



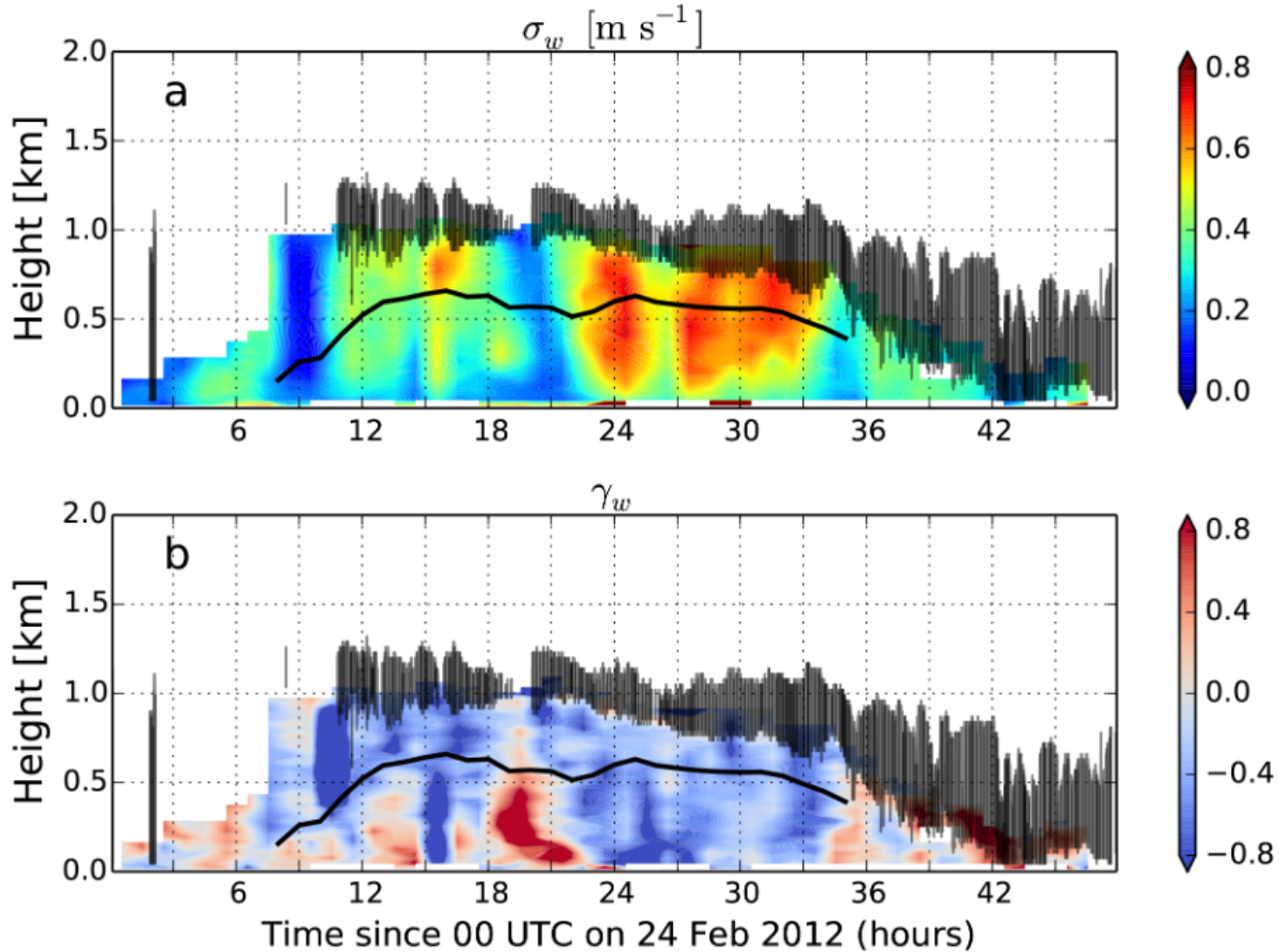


Marine Stratocumulus





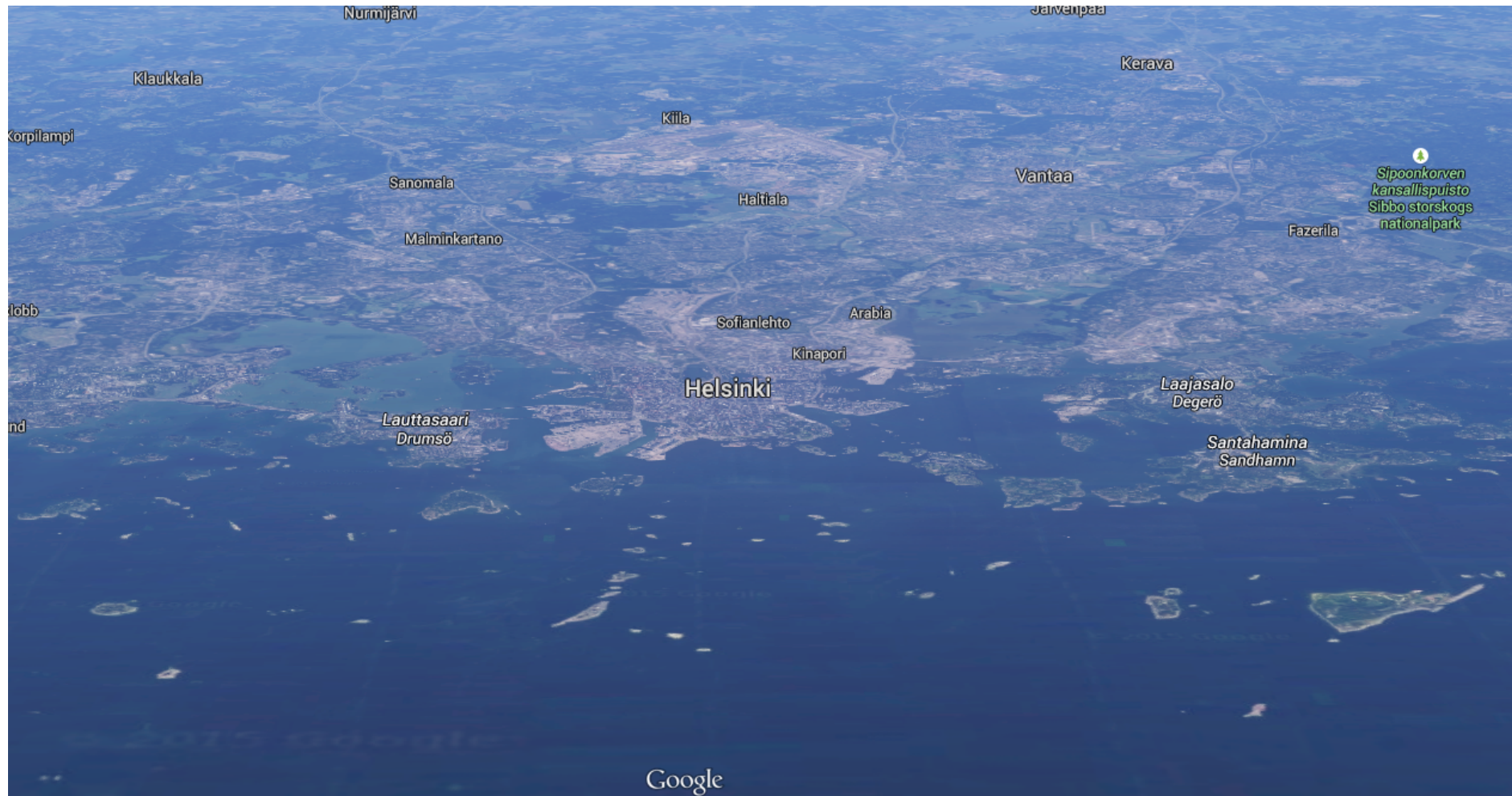
Marine Stratocumulus





Advection of mixed layers in coastal regions

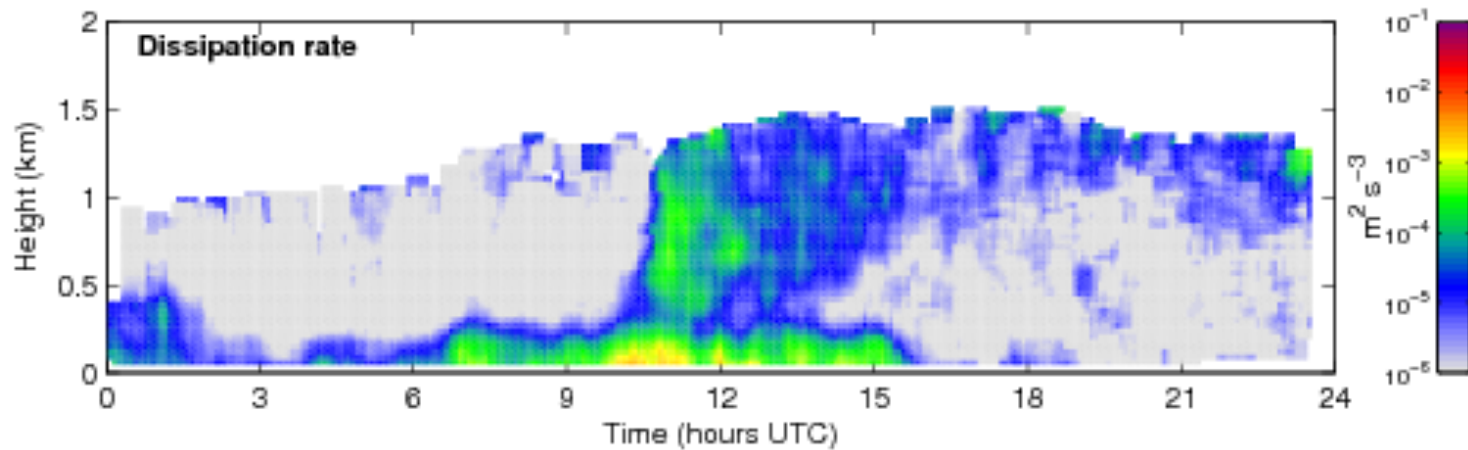
Example from Helsinki





Advection of mixed layers in coastal regions

Example from Helsinki





Advection of mixed layers in coastal regions

Example from Helsinki

