

# Passive Longwave Remote Sensing of Thermodynamics and Clouds

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NOAA / National Severe Storms Laboratory

ARM Summer Workshop  
University of Oklahoma  
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# My Goal

I don't want ~~passive~~ remote sensing be this!



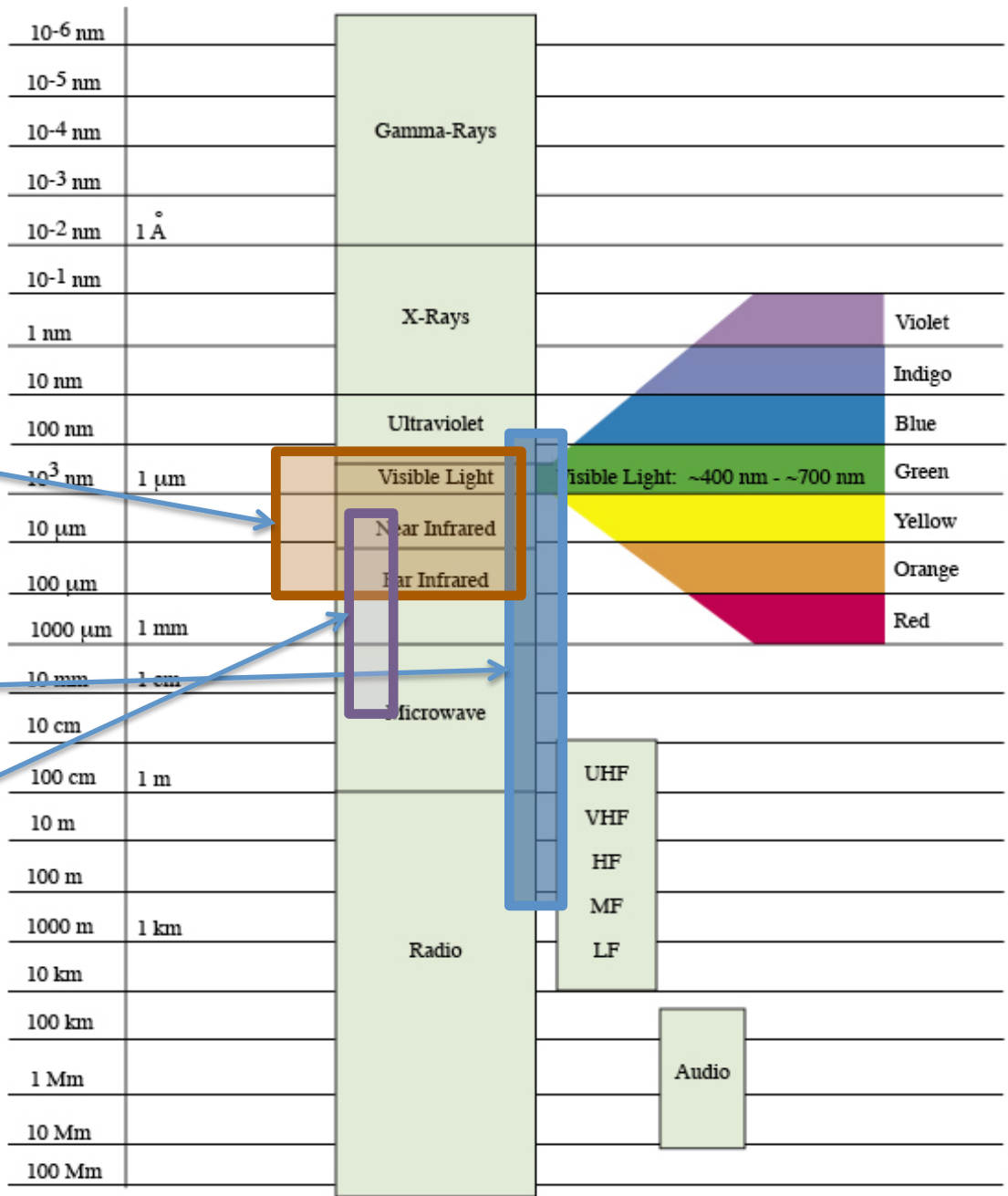
# The Electromagnetic Spectrum

Chart by LASP/University of Colorado, Boulder

Important for Earth's Energy Balance

Important for Remote Sensing

My talk



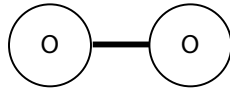
nm=nanometer, Å=angstrom, μm=micrometer, mm=millimeter, cm=centimeter, m=meter, km=kilometer, Mm=Megameter

## Molecule

## Structure

## Permanent Electric Dipole Moment?

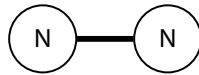
Oxygen



linear

No  
(magnetic dipole)

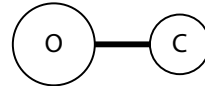
Nitrogen



linear

No

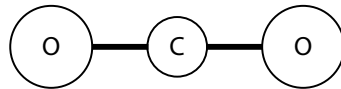
Carbon Monoxide



linear

Yes

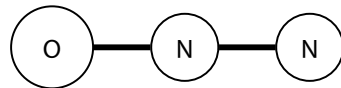
Carbon Dioxide



linear

No

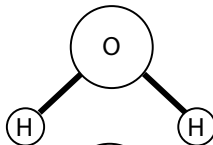
Nitrous Oxide



linear

Yes

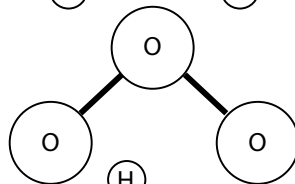
Water



asymmetric top

Yes

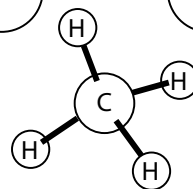
Ozone



asymmetric top

Yes

Methane



spherical top

Yes

# Vibration Modes

Diatomic ( $\text{N}_2$ ,  $\text{O}_2$ ,  $\text{CO}$ )

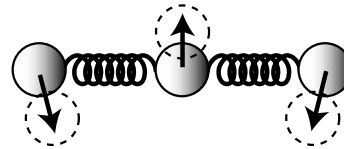


Linear triatomic ( $\text{CO}_2$ ,  $\text{N}_2\text{O}$ )



*Symmetric stretch*

$\nu_1$



*Bending*

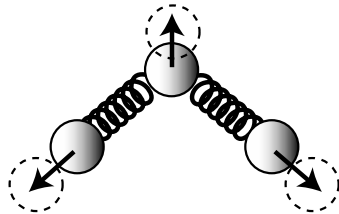
$\nu_2$



*Asymmetric stretch*

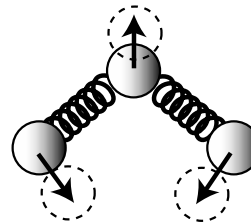
$\nu_3$

Nonlinear Triatomic ( $\text{H}_2\text{O}$ ,  $\text{O}_3$ )



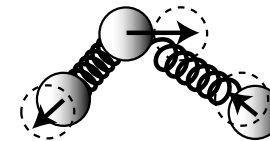
*Symmetric stretch*

$\nu_1$



*Bending*

$\nu_2$



*Asymmetric stretch*

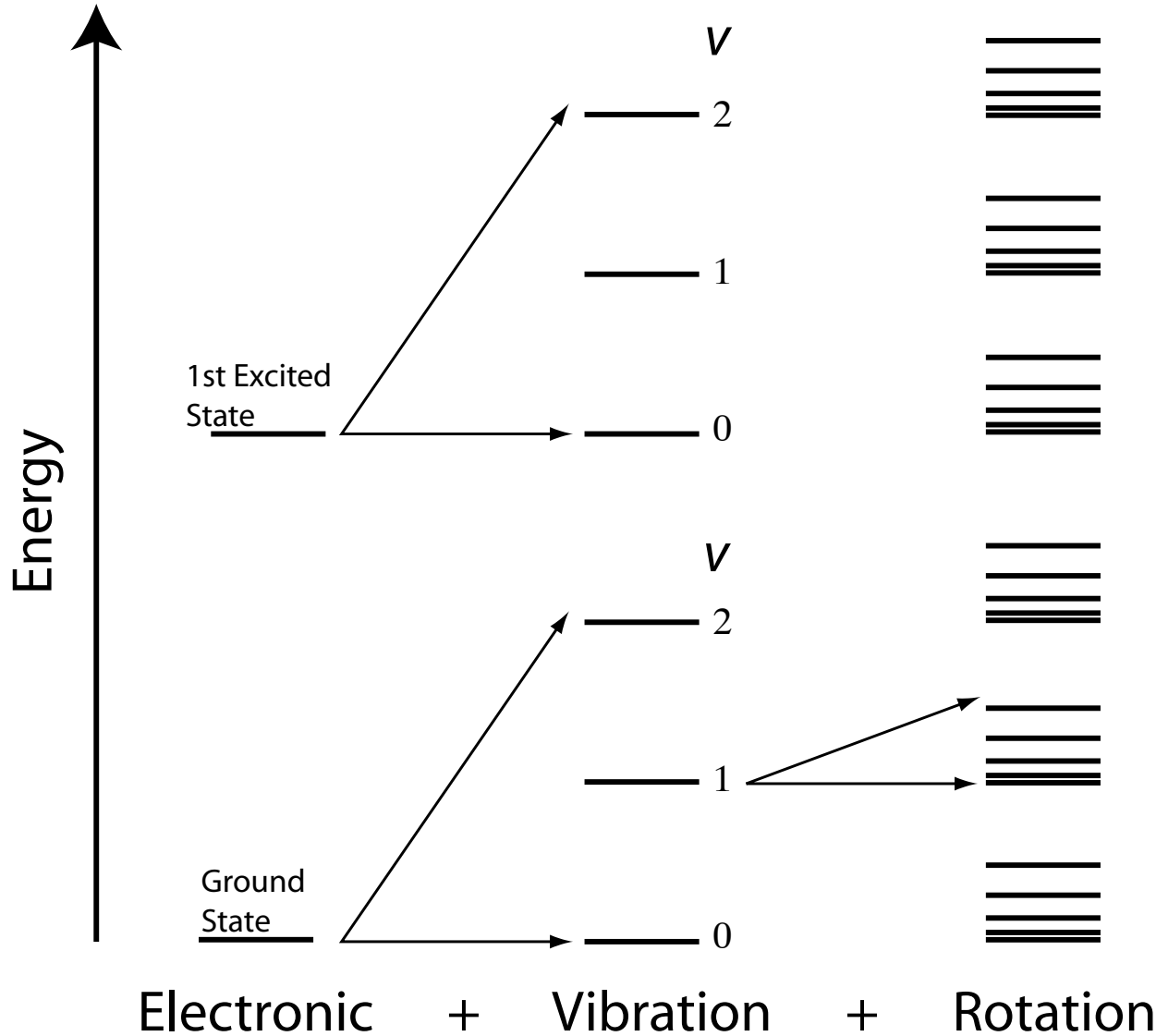
$\nu_3$

# Quantum Physics!

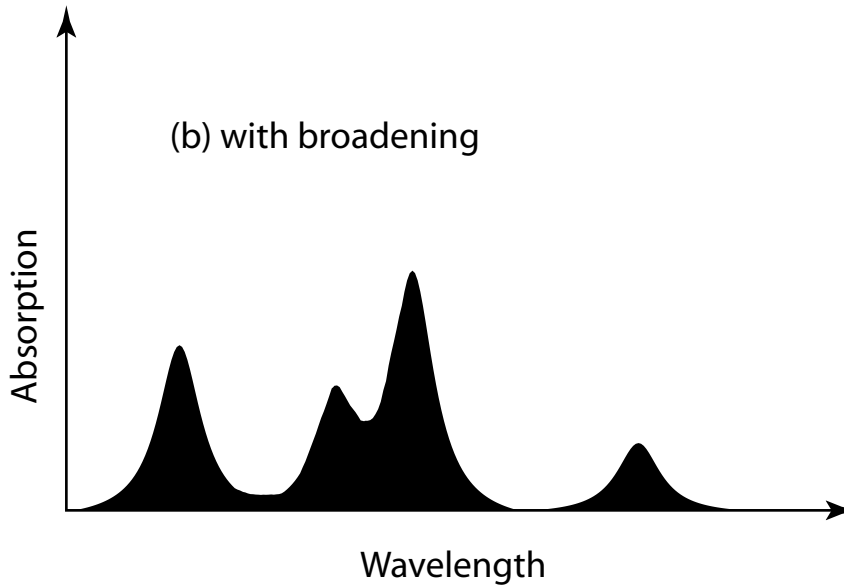
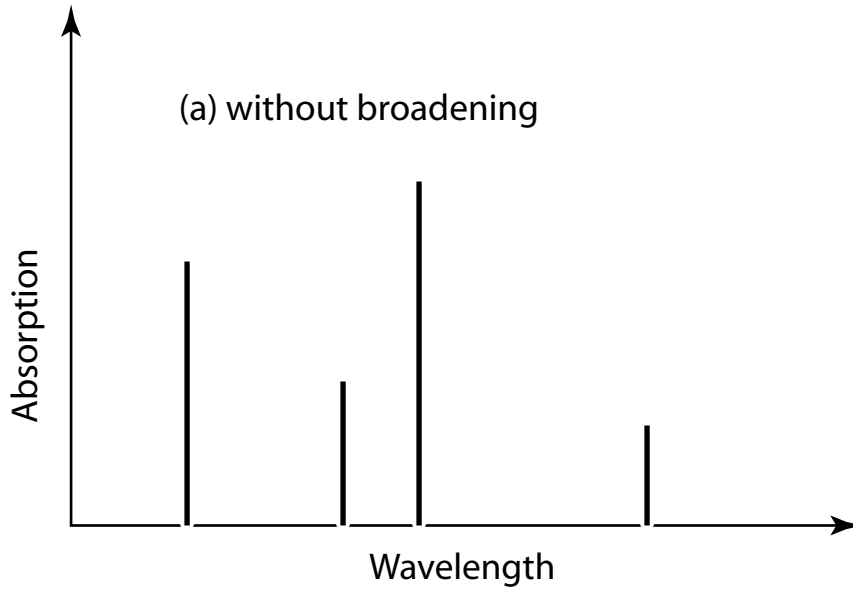
(Woo hoo!)

$$E = h \nu$$

Energy                  Planck's constant                  Frequency

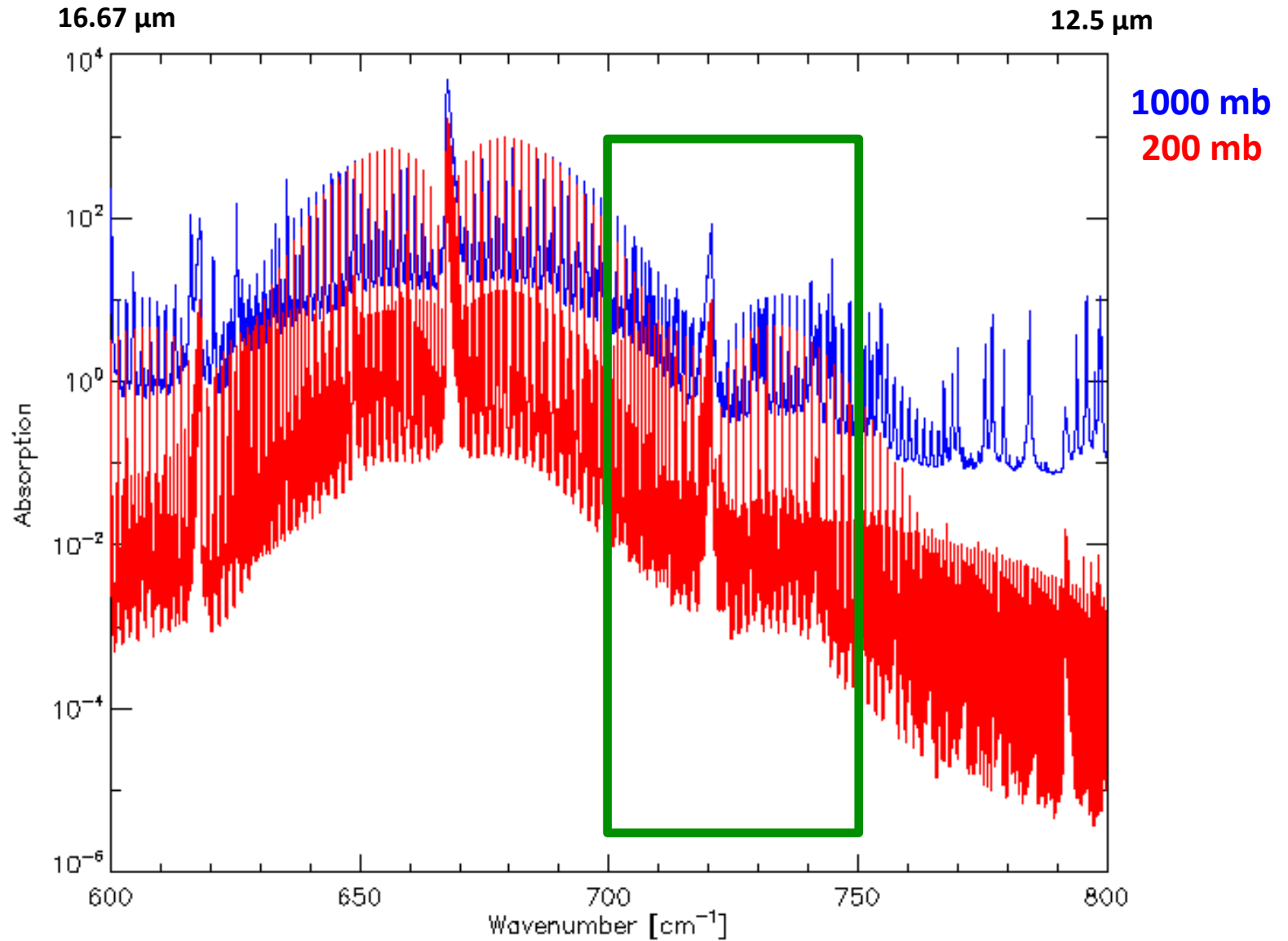


# Pressure Broadening



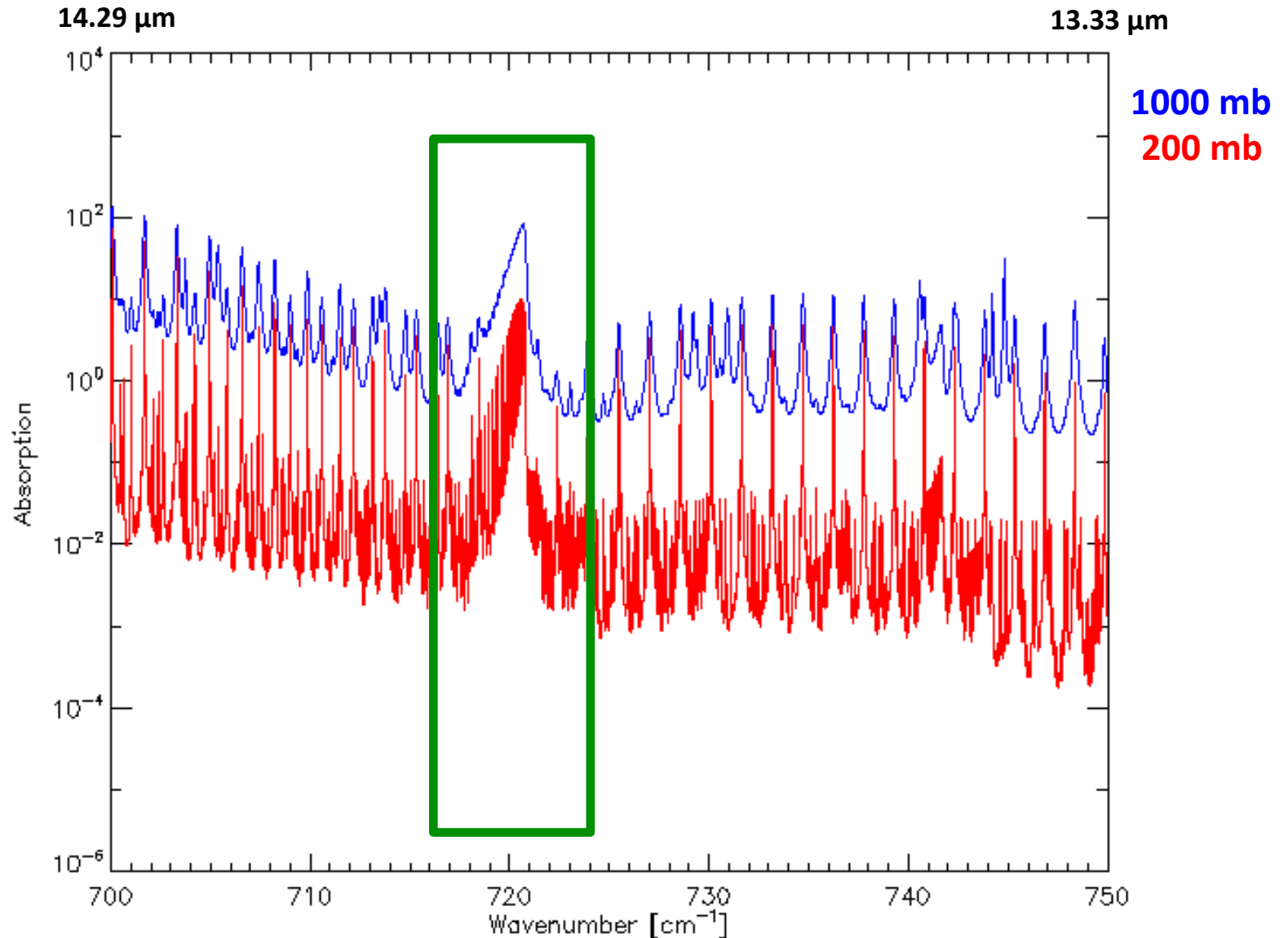
*There are other sources of absorption line broadening (e.g., Doppler broadening) but they are much less important in the troposphere*

# Carbon Dioxide Absorption

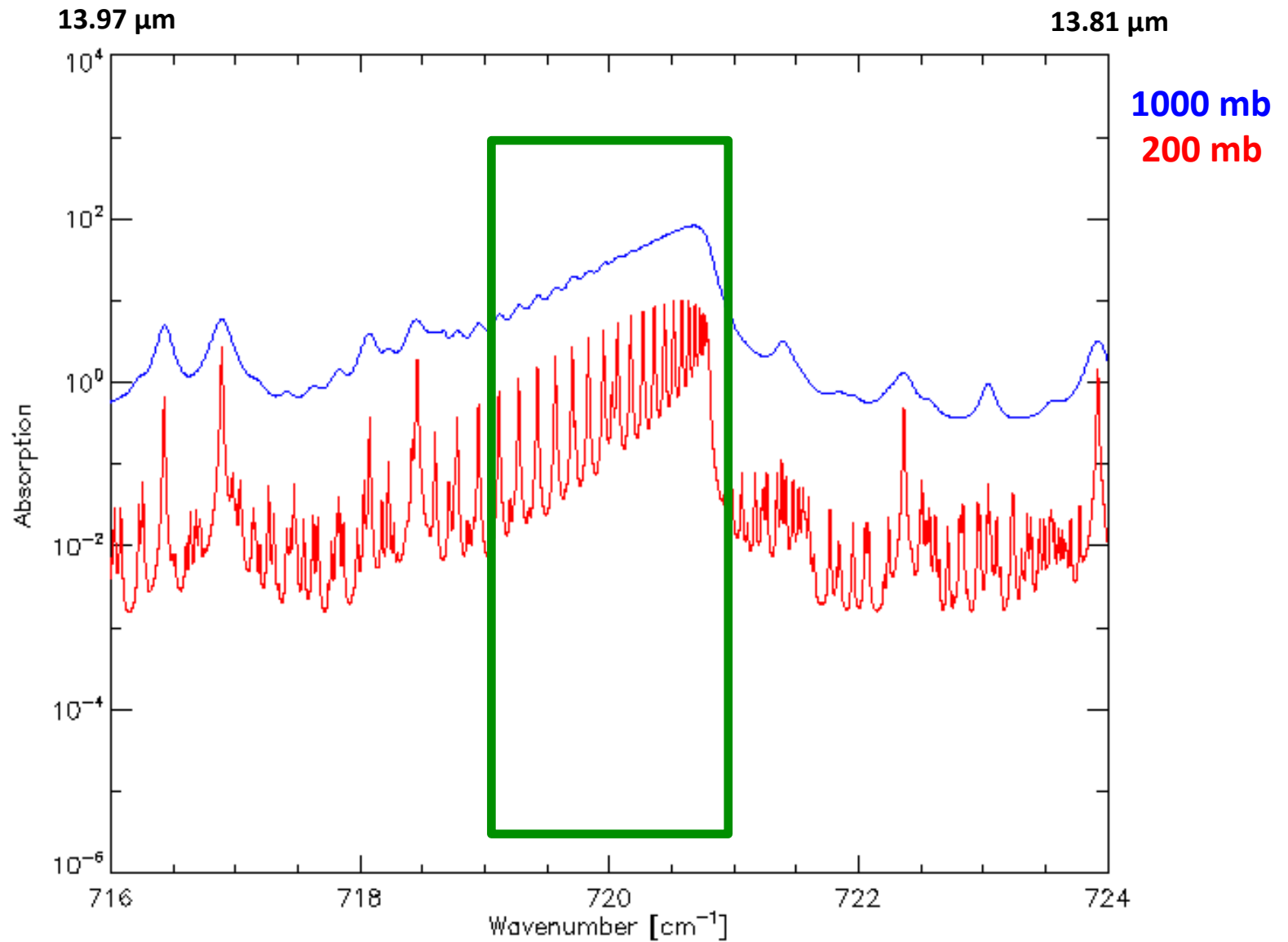




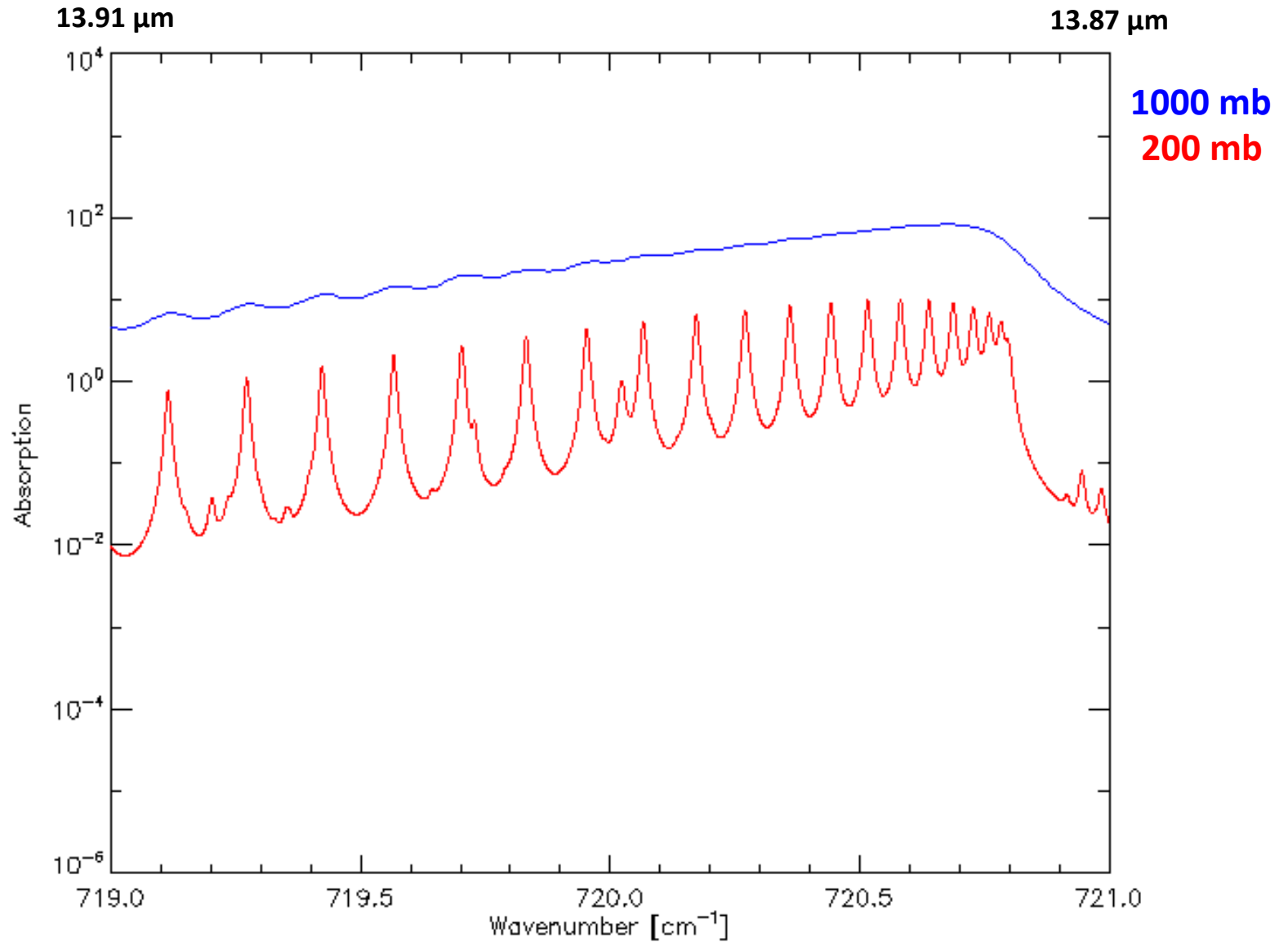
# Carbon Dioxide Absorption



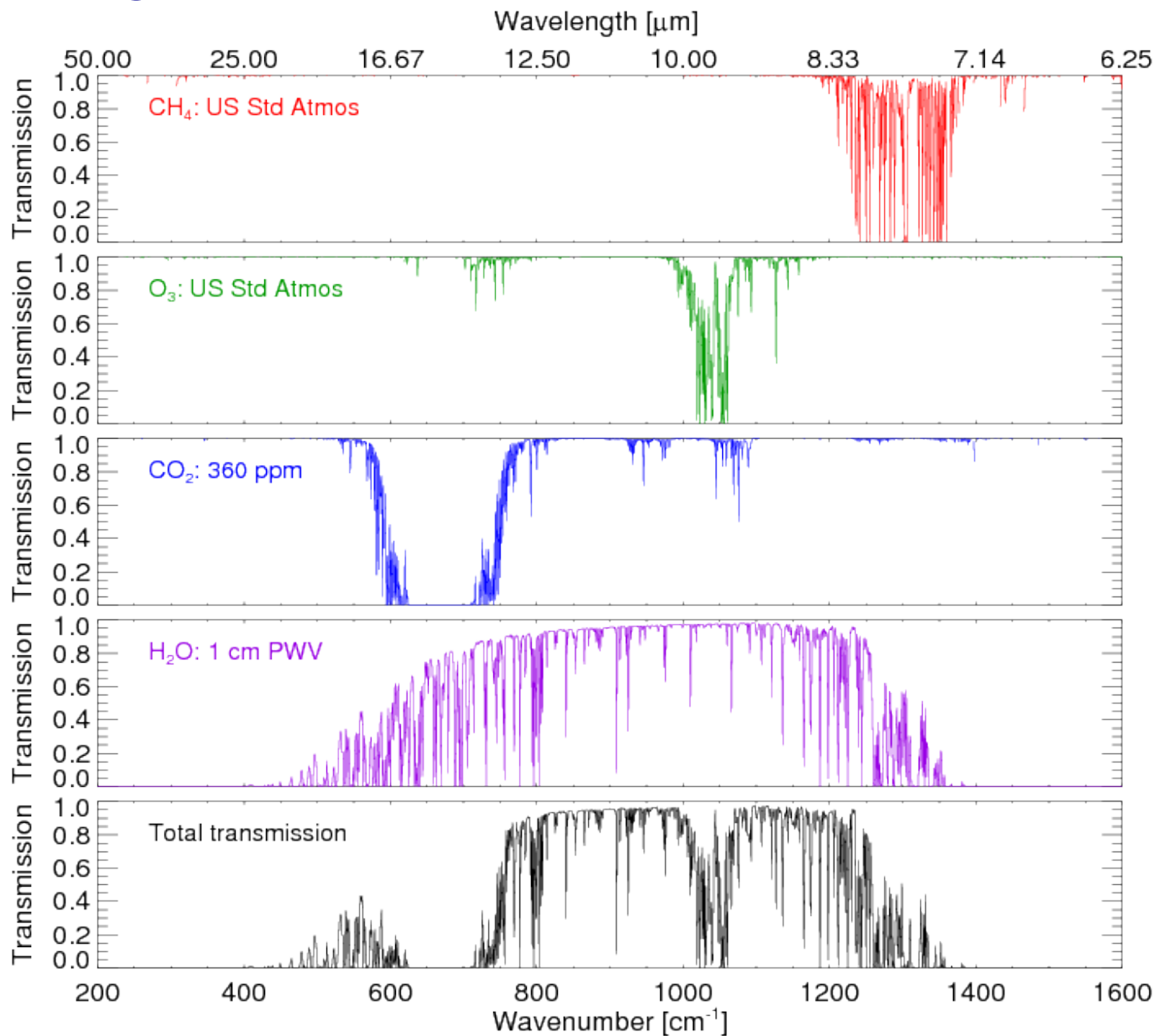
# Carbon Dioxide Absorption



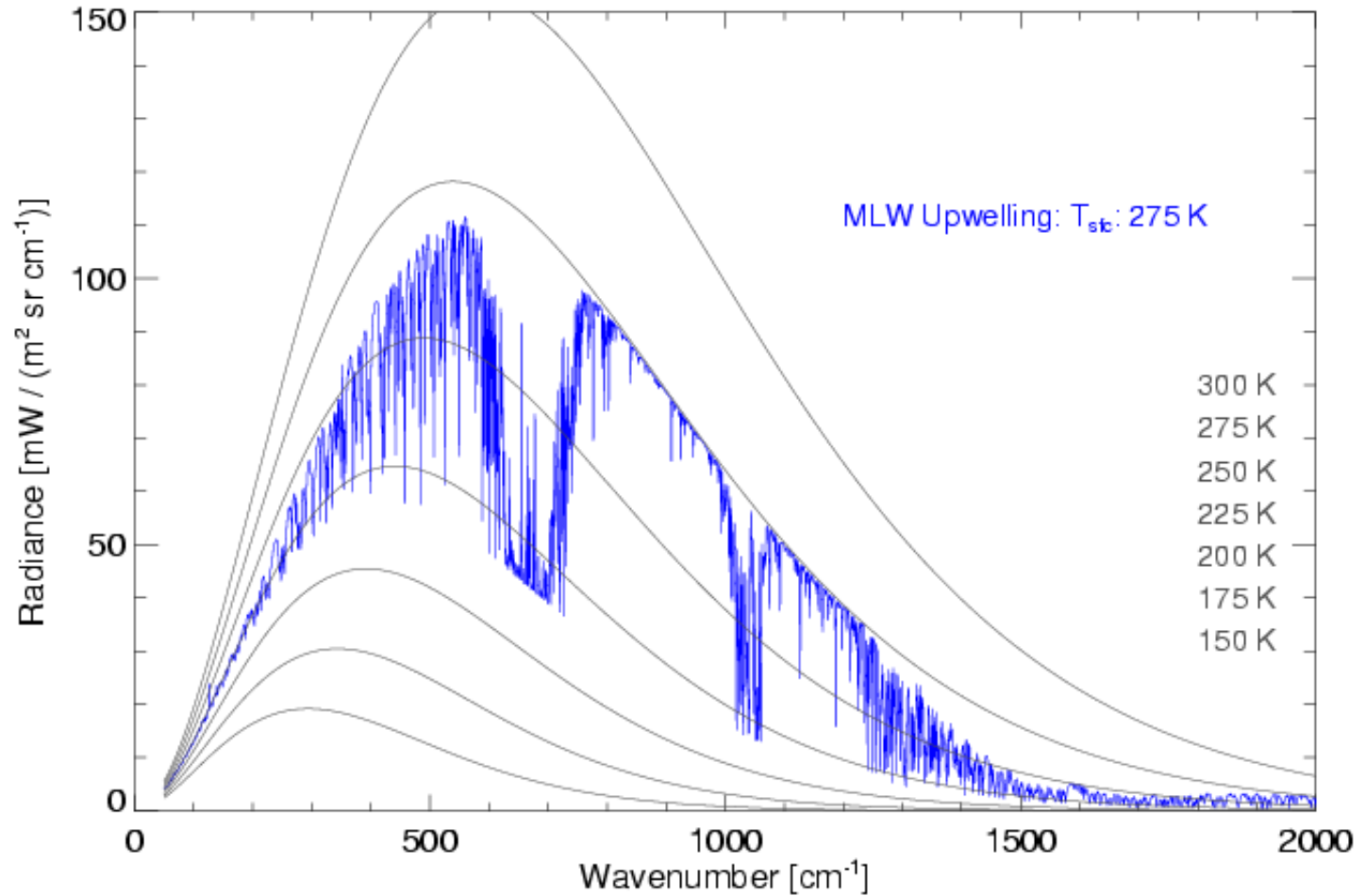
# Carbon Dioxide Absorption



# Primary Gas Absorption Bands in IR

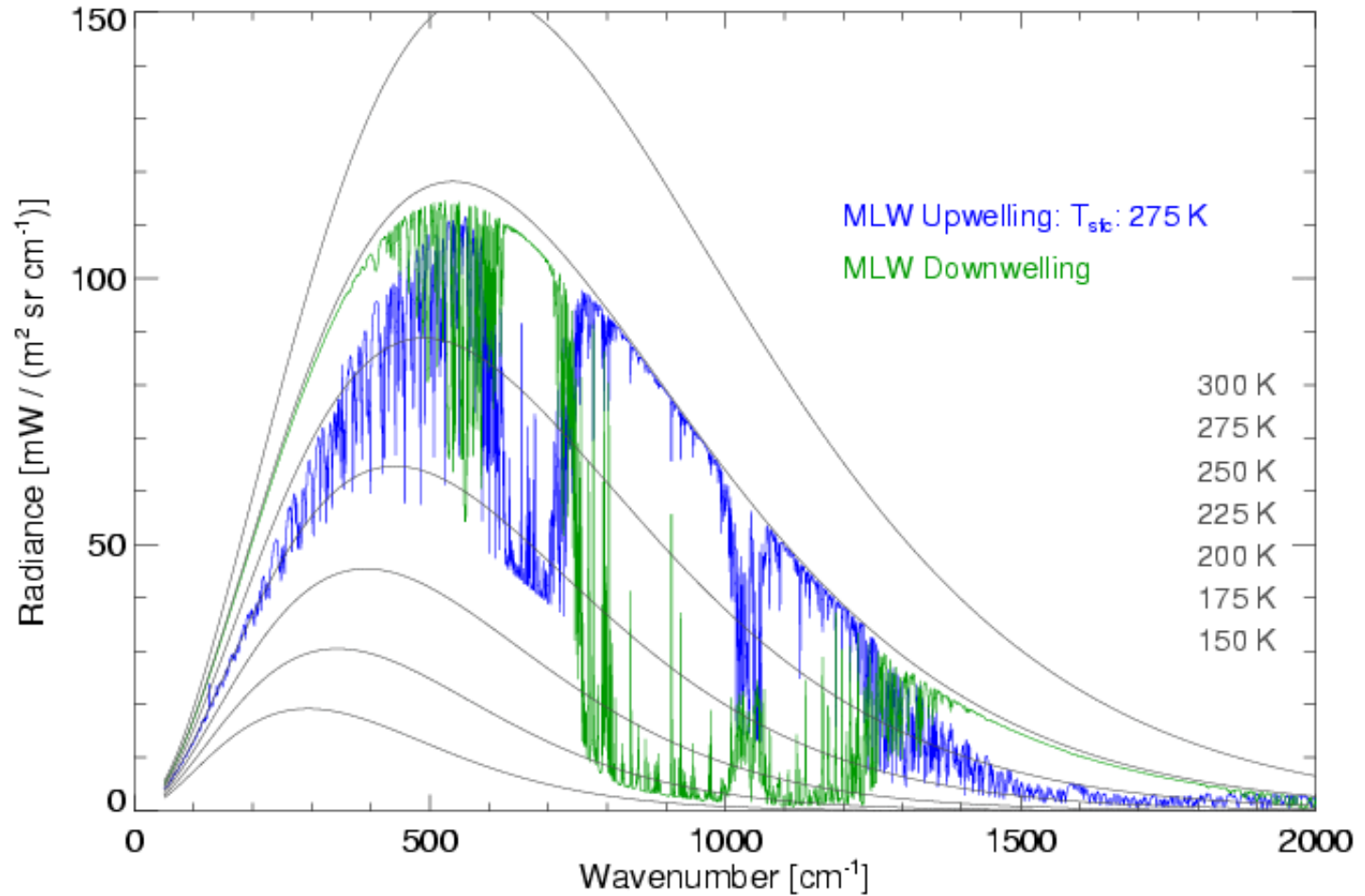


# Upwelling LW Radiance at Top of the Atmosphere



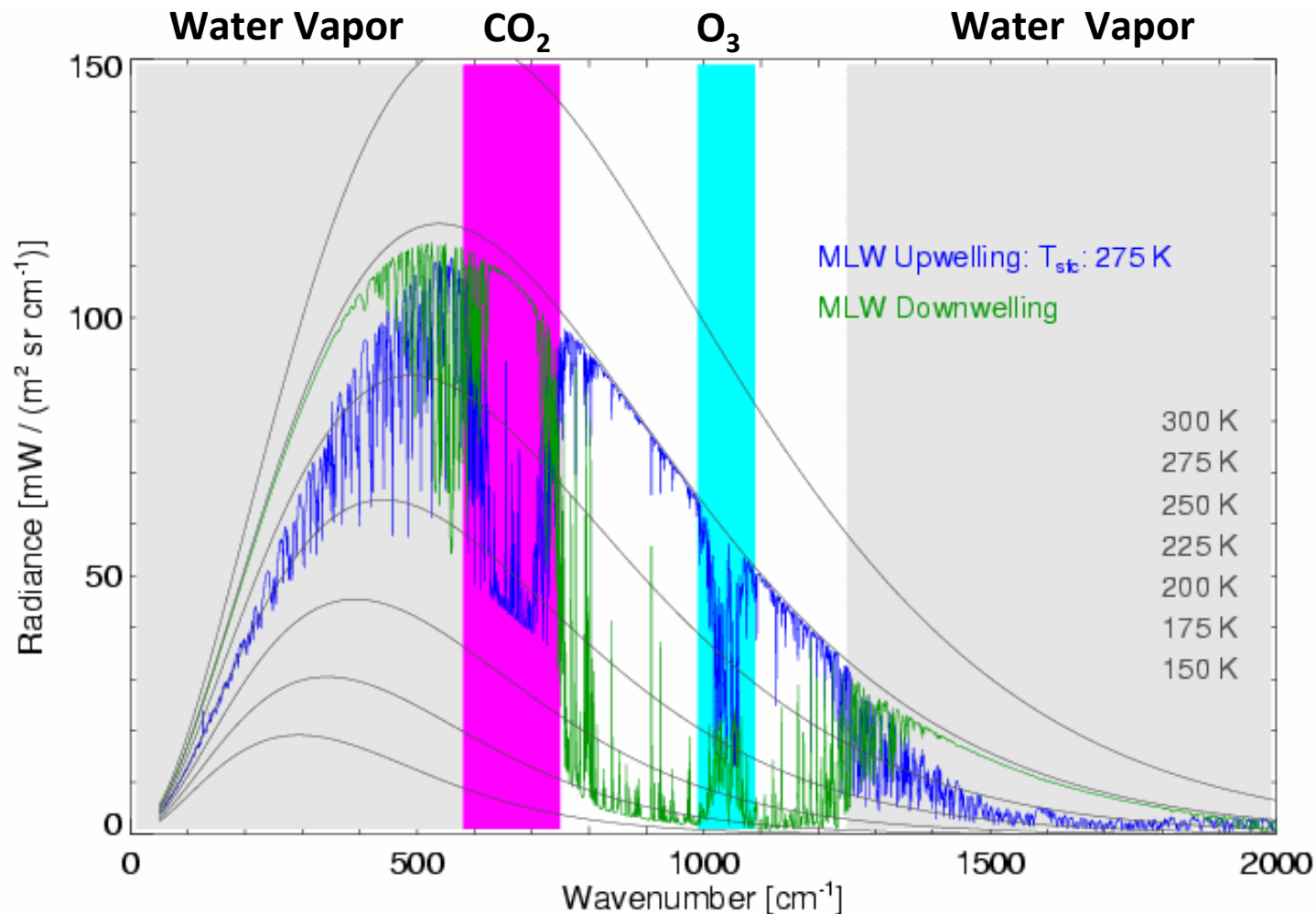
# Upwelling LW Radiance at Top of the Atmosphere

## Downwelling LW Radiance at the Surface



# Upwelling LW Radiance at Top of the Atmosphere

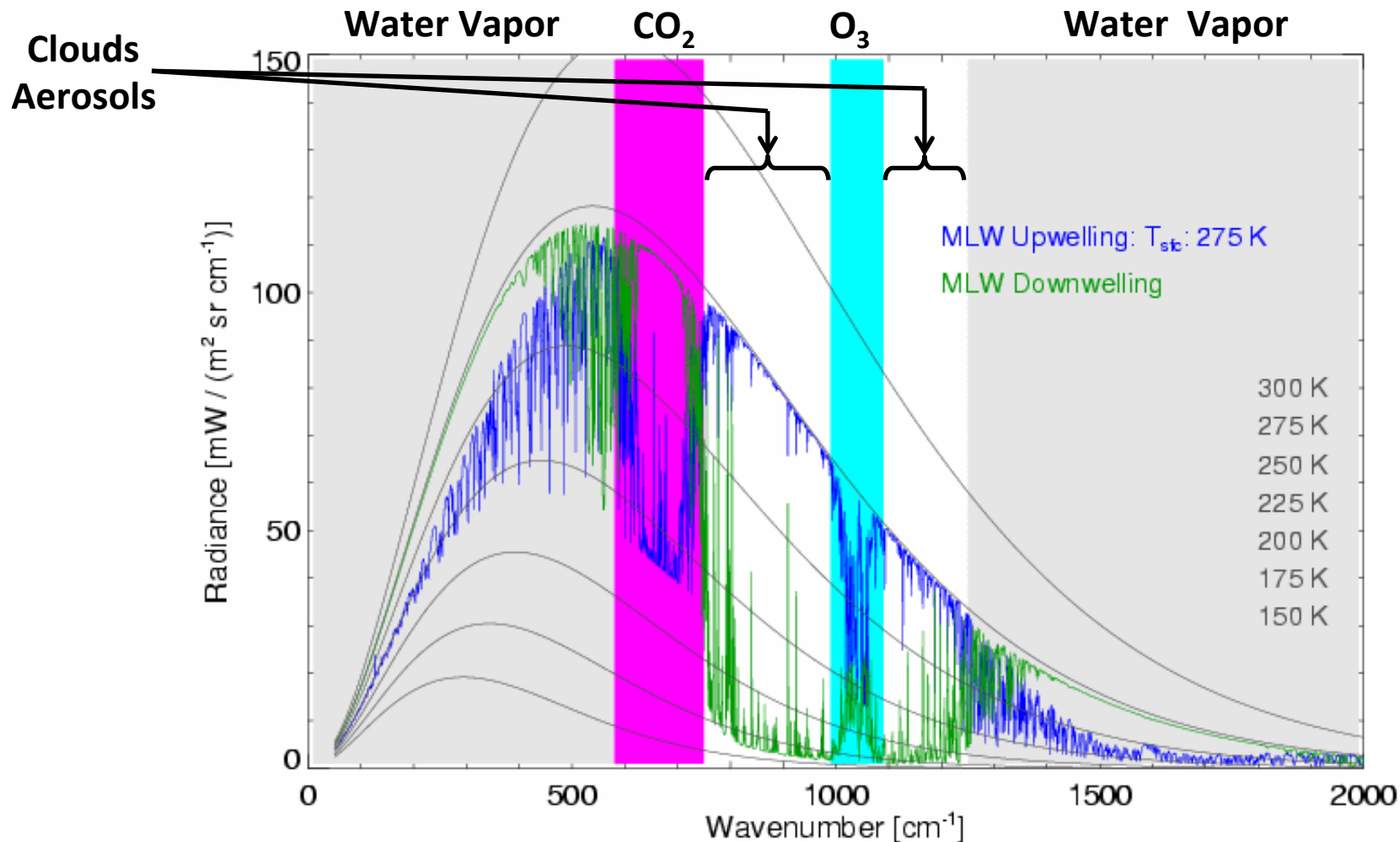
## Downwelling LW Radiance at the Surface



Trace gases (CFC,  $\text{CH}_4$ , etc) absorb in various regions

# Upwelling LW Radiance at Top of the Atmosphere

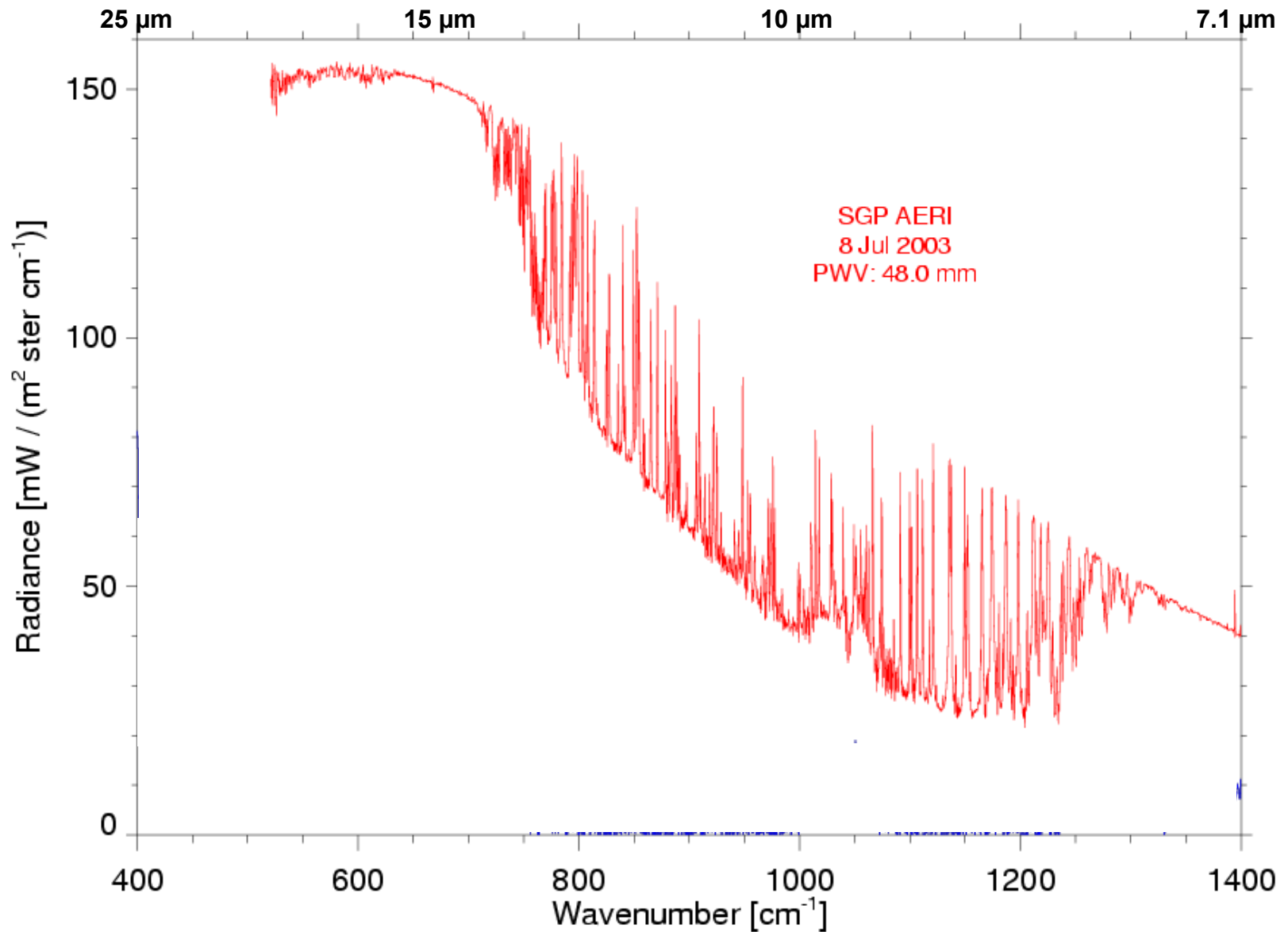
## Downwelling LW Radiance at the Surface



Trace gases (CFC, CH<sub>4</sub>, etc) absorb in various regions



# Clear Sky Downwelling IR Spectra



# Atmospheric Emitted Radiance Interferometer (AERI)



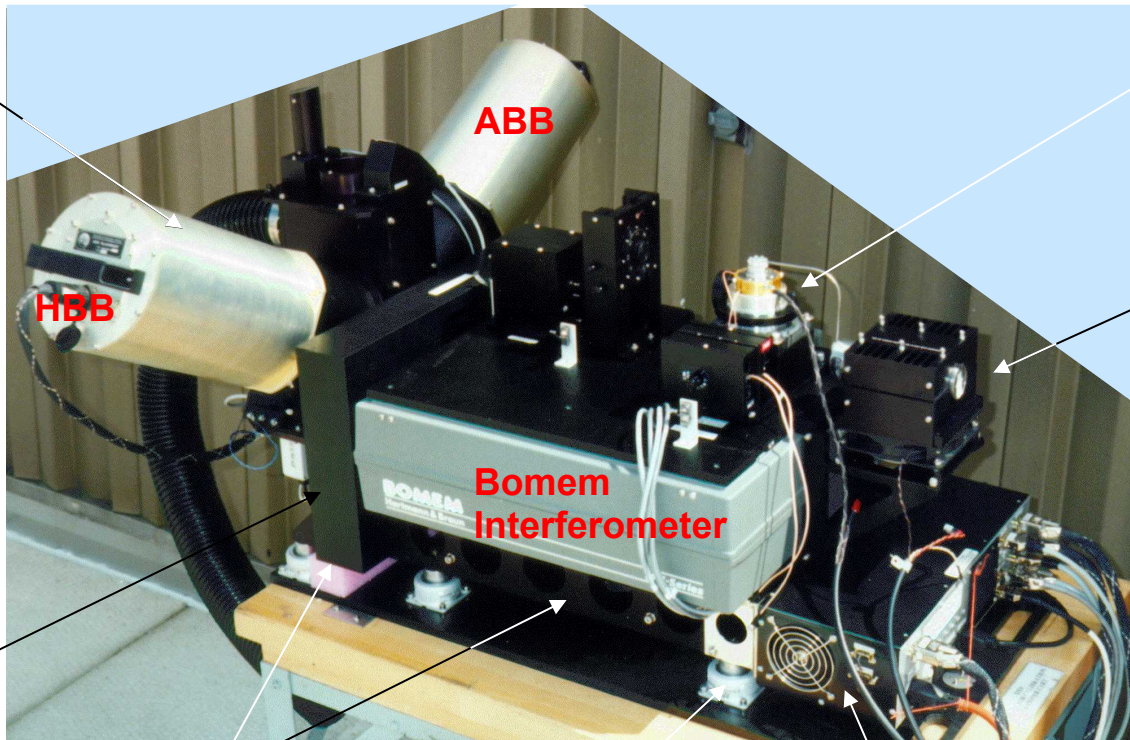
# AERI

- Measures downwelling infrared radiance at high spectral resolution
- Absolute accuracy is better than 1% of the ambient radiance ( $3\text{-}\sigma$ )
  - High emissivity blackbodies (0.9995)
  - BB temperature accuracy NIST-traceable and accurate to 30 mK
- Data used in wide range of research
  - RT model validation/improvement
  - Thermodynamic profiling
  - Cloud property retrievals
  - Aerosol optical depth / composition
  - Trace gas retrievals

# AERI Interferometer Assembly

## Front End Assembly

Blackbodies  
Scene Mirror Assembly  
Forced Air Inlet  
Rain Sensor  
Sun Sensor



IR Detector  
Dewar with  
Cooler Cold Finger

Stirling Cooler  
Compressor

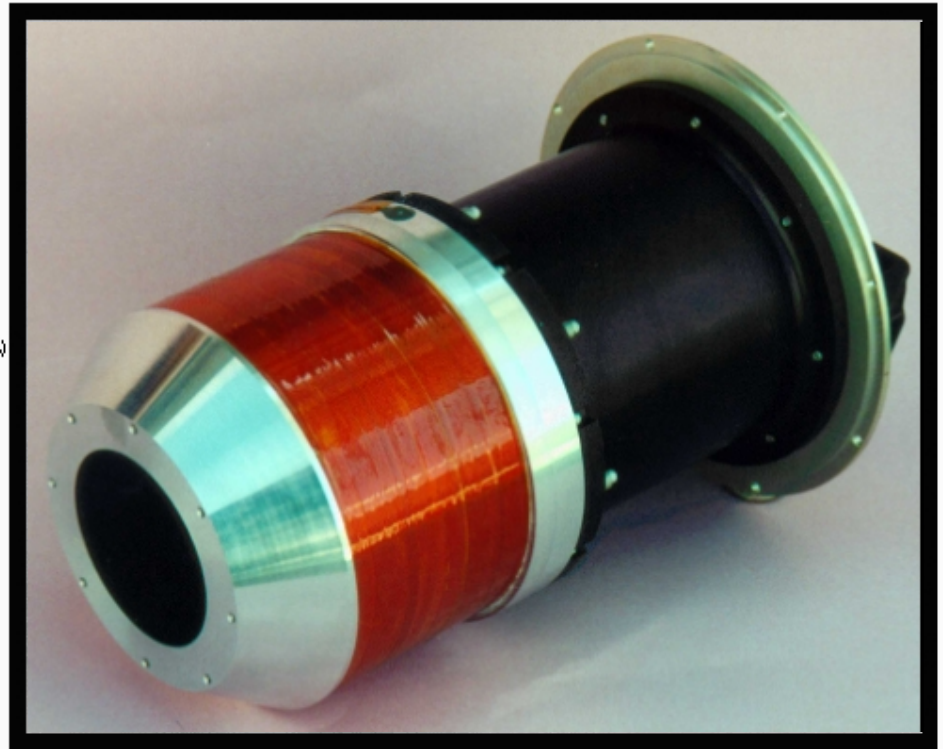
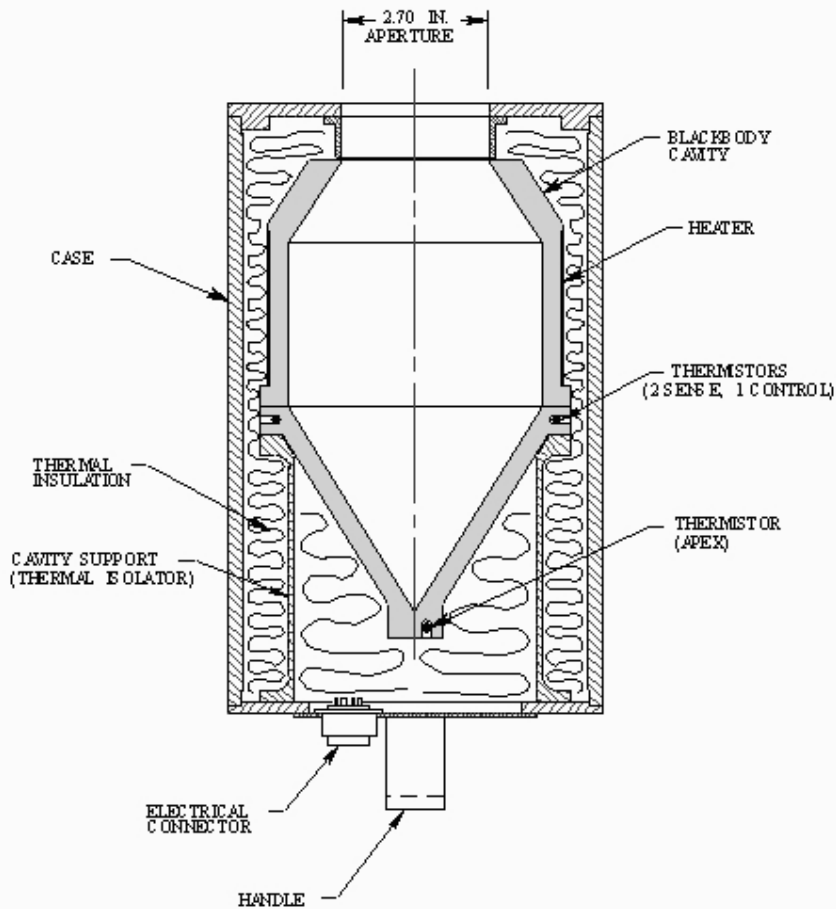
Front-end  
Closeout  
(thermal)

Optics  
Bench

Shock  
Mounts (4)

Interferometer / AERI  
Electronics Interface Box

# Calibration Targets (Blackbodies) are Key to Accurate Radiances



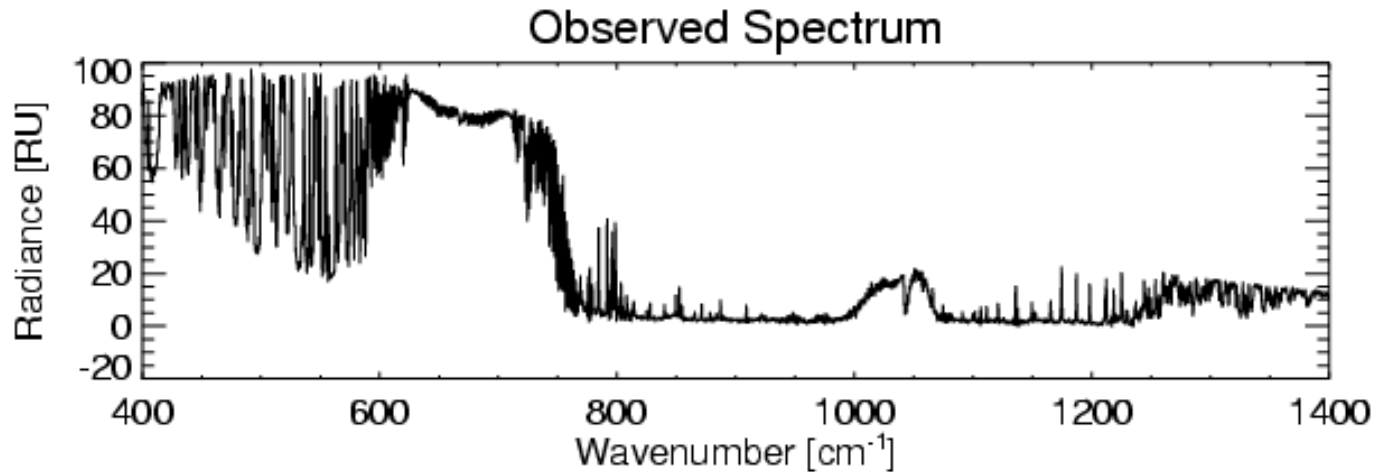
**Emissivity > 0.999**

# How an Interferometer Works

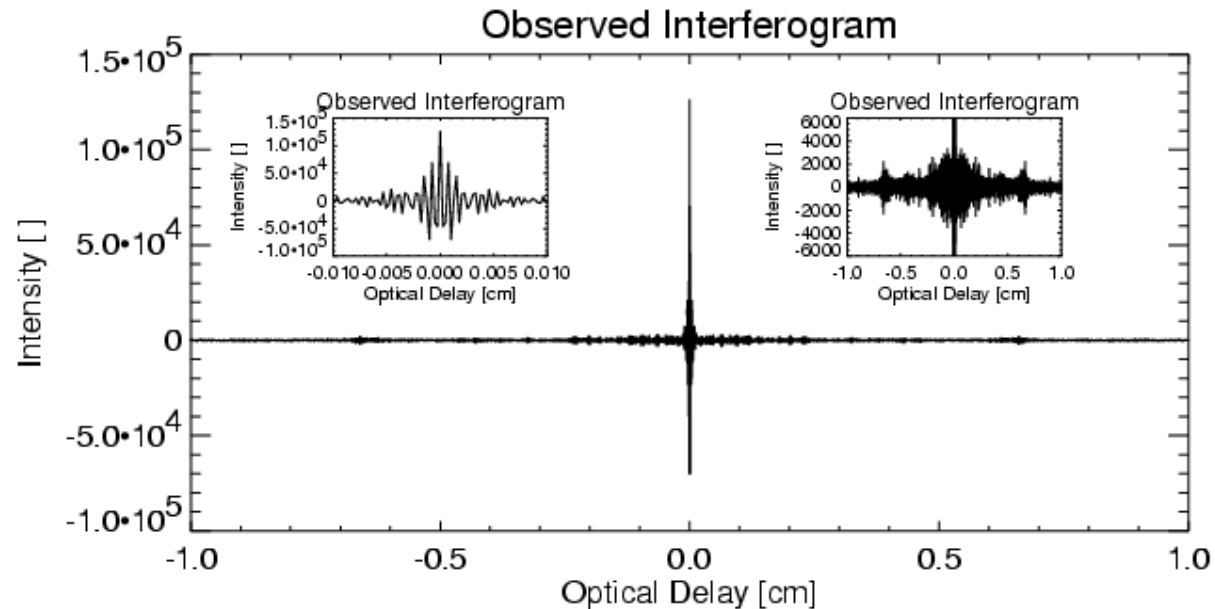
1. Move one mirror slowly back-and-

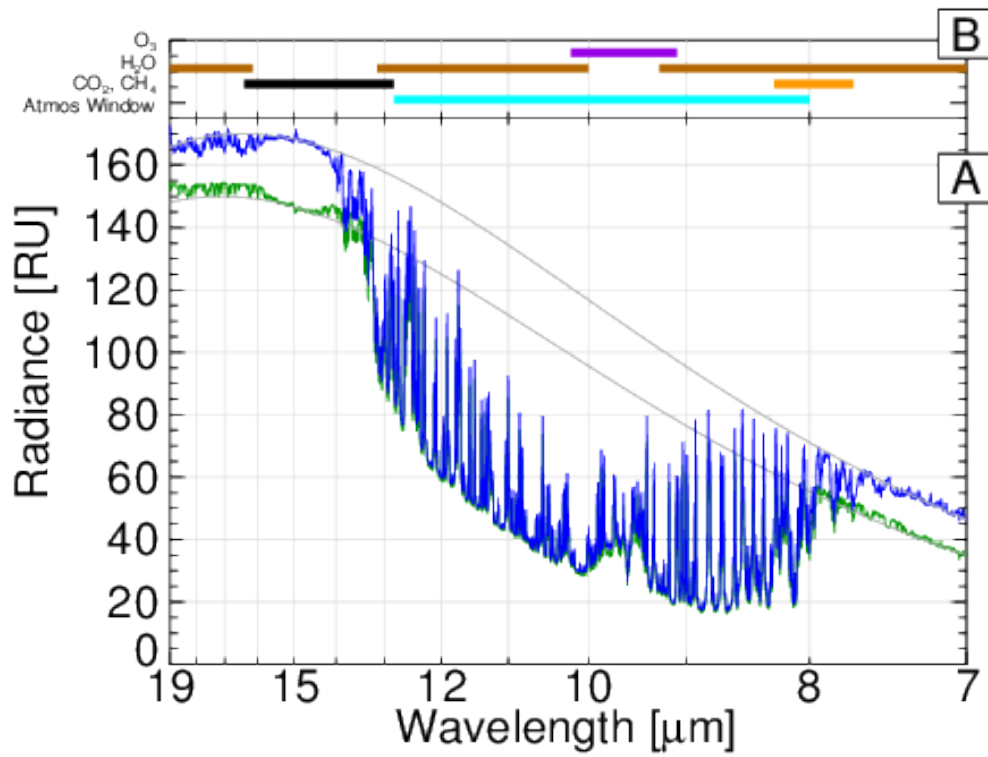
forth (interference  
pattern) at the

sample as a  
reference mirror



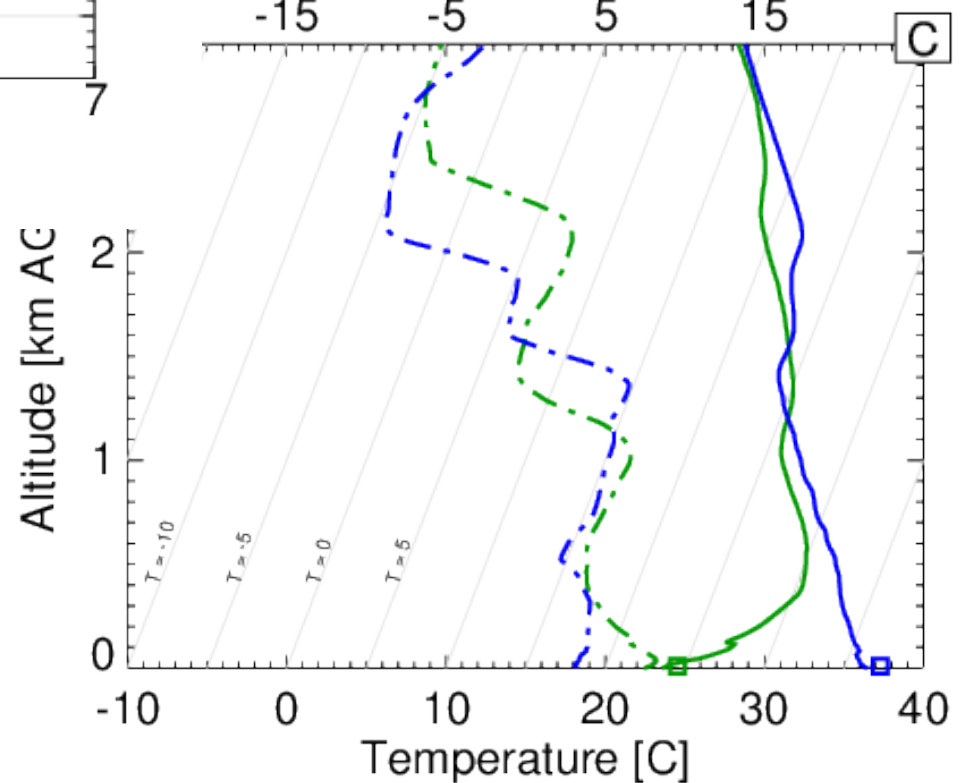
3. Apply a FFT to the  
interferogram to  
yield the spectrum

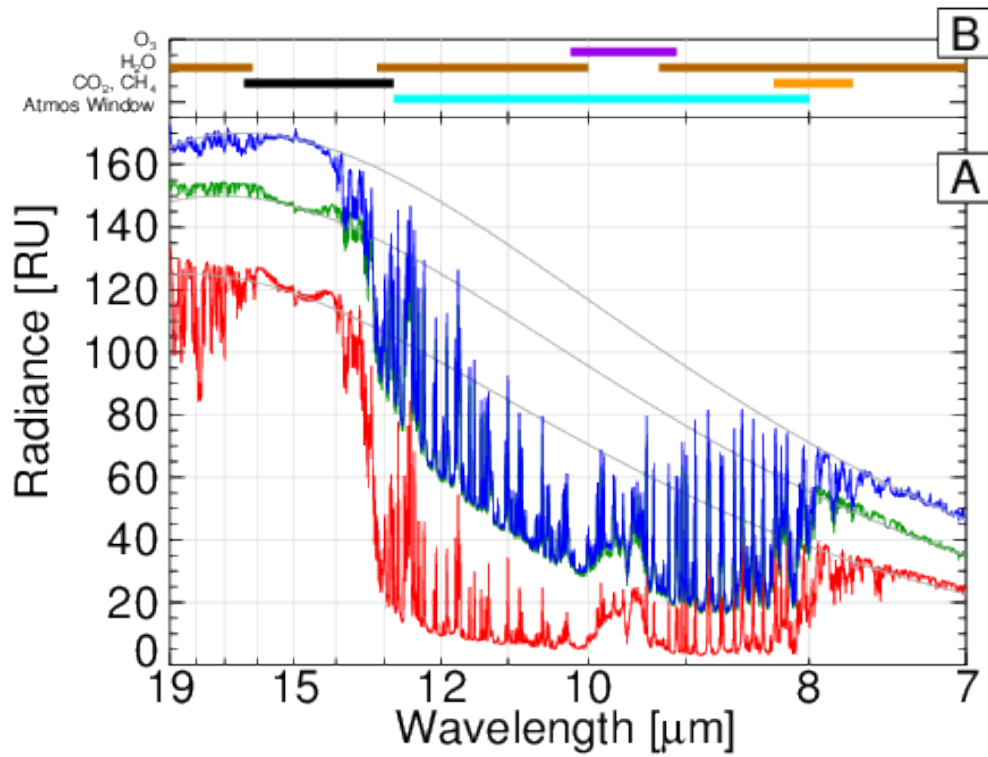




# Example Spectra to Retrieved Profiles

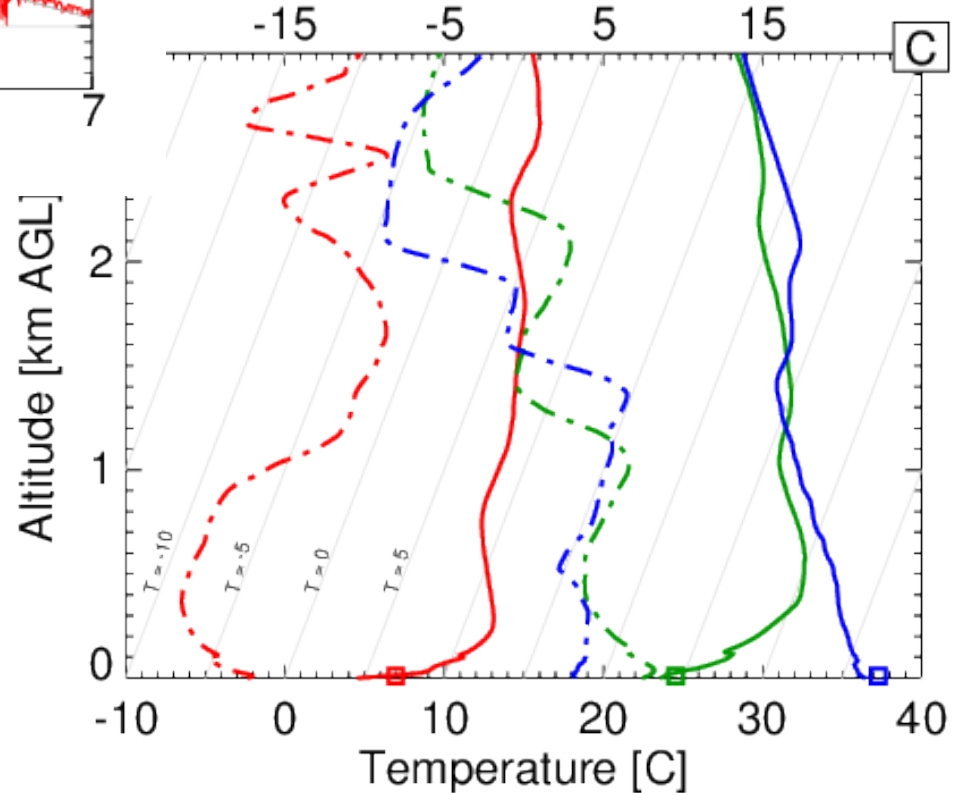
**Solid lines: temperature**  
**Dash/dot line: dew point**





# Example Spectra to Retrieved Profiles

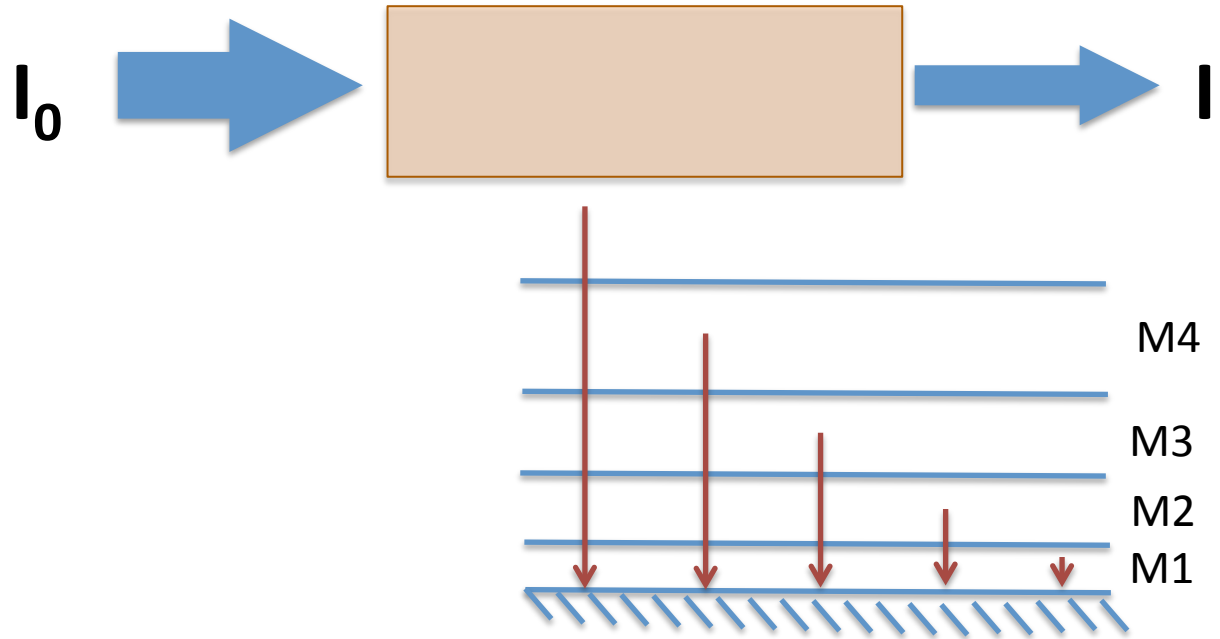
**Solid lines: temperature**  
**Dash/dot line: dew point**





# RT Basics

$$1 = J_\lambda + A_\lambda + \cancel{R_\lambda}$$

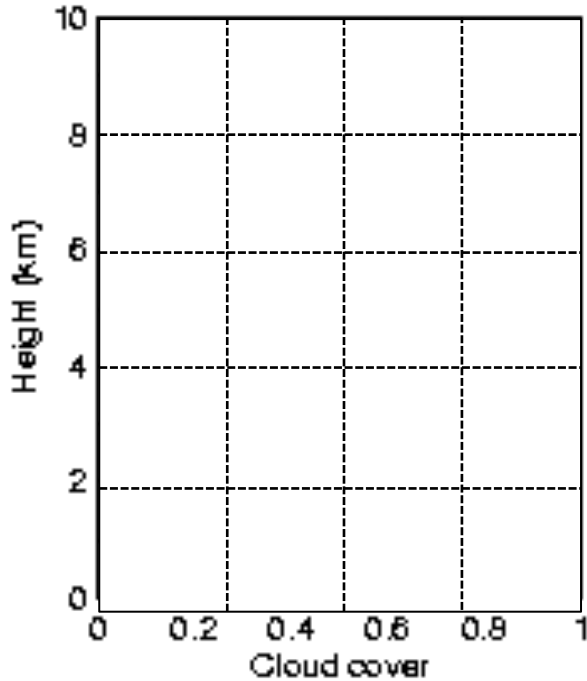


Local Thermodynamic Equilibrium  
Absorption = Emission

Emission  
from the layer

Transmission  
to the surface

# Downwelling Clear Sky Case (Example 1a)



$$T_{\text{gas5}} = 0.2$$

$$T_{\text{gas4}} = 0.8$$

$$T_{\text{gas3}} = 3.2$$

$$T_{\text{gas2}} = 12.5$$

$$T_{\text{gas1}} = 50.0$$

$$T_5 = 230 \text{ K}, B(T) = 41.2 \text{ RU}$$

$$T_4 = 244 \text{ K}, B(T) = 55.0 \text{ RU}$$

$$T_3 = 258 \text{ K}, B(T) = 71.2 \text{ RU}$$

$$T_2 = 272 \text{ K}, B(T) = 89.9 \text{ RU}$$

$$T_1 = 286 \text{ K}, B(T) = 111.0 \text{ RU}$$

$$T_0 = 300 \text{ K}, B(T) = 134.4 \text{ RU}$$

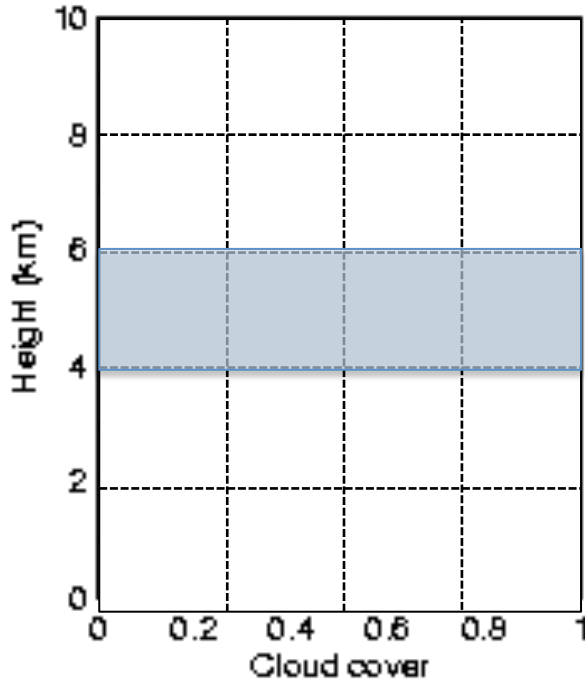
$$T_{\text{sfc}} = 310 \text{ K}, B(T_{\text{sfc}}) = 152.5 \text{ RU}, \text{Emissivity} = 1$$

Calculation at  $800 \text{ cm}^{-1}$   
which is  $12.5 \mu\text{m}$

$\text{RU} = 1 \text{ mW}/(\text{m}^2 \text{ sr cm}^{-1})$

Downwelling radiance:  $(1 - \exp(-0.2)) * (41.2 + 55.0) / 2 * \exp(-(0.8 + 3.2 + 12.5 + 50)) +$

# Downwelling Cloudy Sky Case (Example 1b)



$T_{\text{gas5}} = 0.2$        $T_5 = 230 \text{ K}, B(T) = 41.2 \text{ RU}$   
 $T_{\text{gas4}} = 0.8$        $T_4 = 244 \text{ K}, B(T) = 55.0 \text{ RU}$   
 $T_{\text{gas3}} = 3.2$        $T_3 = 258 \text{ K}, B(T) = 71.2 \text{ RU}$   
 $T_{\text{gas2}} = 12.5$        $T_2 = 272 \text{ K}, B(T) = 89.9 \text{ RU}$   
 $T_{\text{gas1}} = 50.0$        $T_1 = 286 \text{ K}, B(T) = 111.0 \text{ RU}$   
 $T_0 = 300 \text{ K}, B(T) = 134.4 \text{ RU}$   
 $T_{\text{sfc}} = 310 \text{ K}, B(T_{\text{sfc}}) = 152.5 \text{ RU}, \text{Emissivity} = 1$

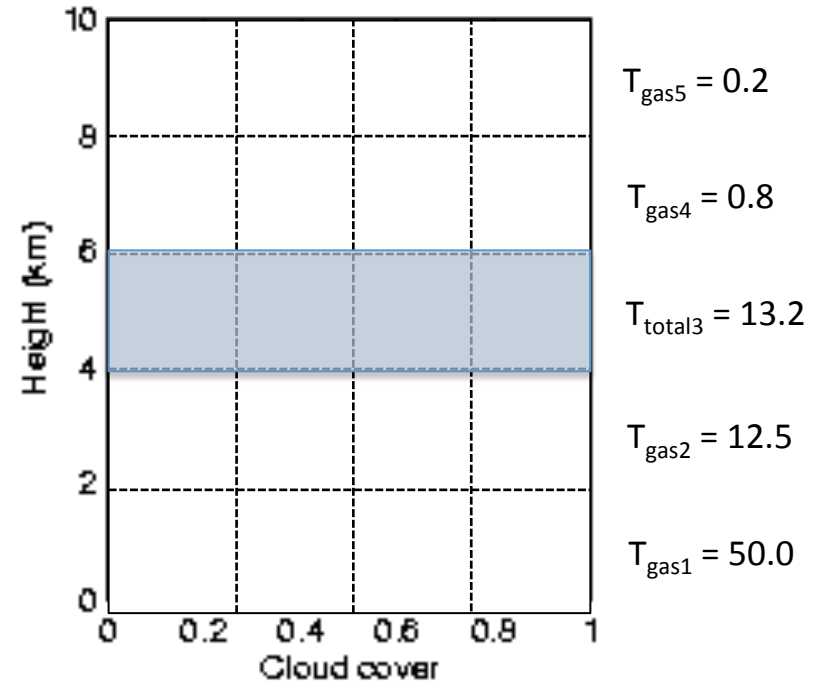
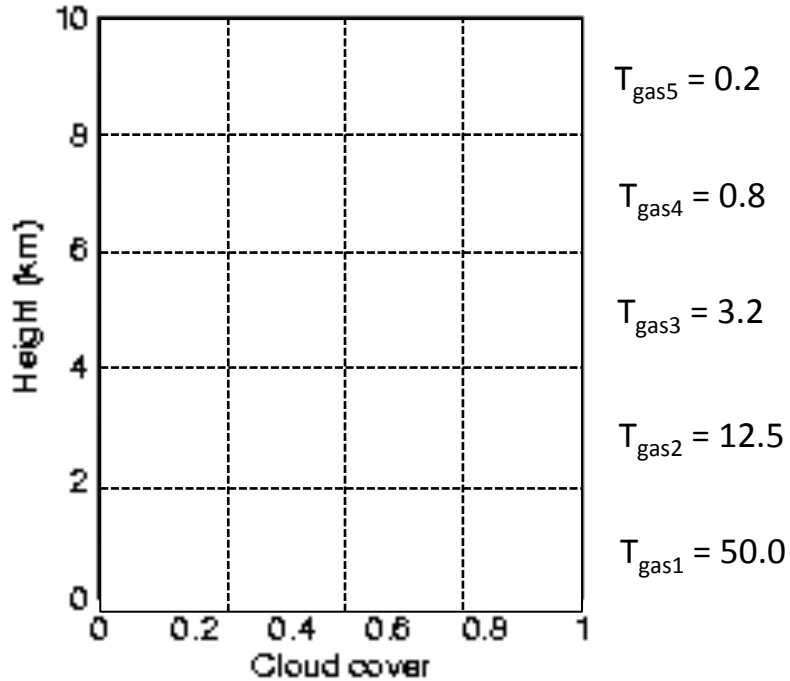
Calculation at  $800 \text{ cm}^{-1}$   
 which is  $12.5 \mu\text{m}$   
 $\text{RU} = 1 \text{ mW}/(\text{m}^2 \text{ sr cm}^{-1})$

$T_{\text{cloud3}} = 10, F_{\text{cld}} = 1.0$



Downwelling radiance:  $(1 - \exp(-0.2)) * (41.2 + 55.0) / 2 * \exp(- (0.8 + 13.2 + 12.5 + 50)) +$

# Example 1a vs Example 1b: Why ?

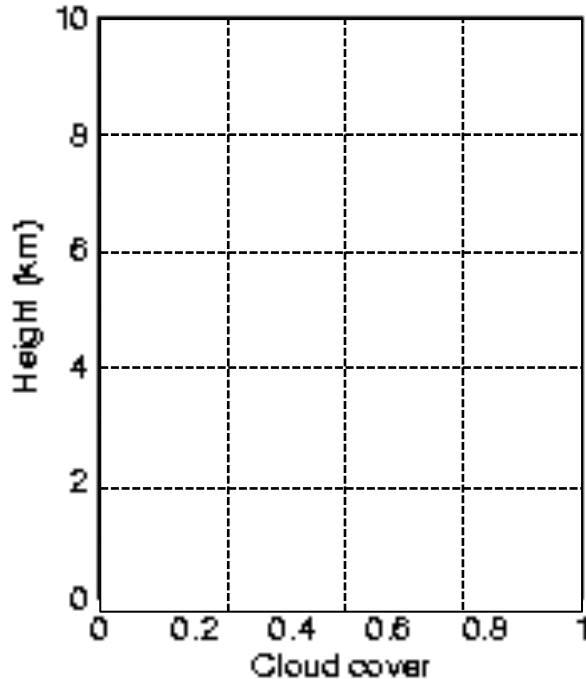


$T_{\text{sfc}}=310 \text{ K}$ ,  $B(T_{\text{sfc}})=152.5 \text{ RU}$ , Emissivity=1

Downwelling Radiance: 133.9 RU

Downwelling Radiance: 133.9 RU

# Downwelling Clear Sky Case (Example 1c)



$T_{\text{gas5}} = 0.2$	$T_5 = 230 \text{ K}, B(T) = 41.2 \text{ RU}$
$T_{\text{gas4}} = 0.8$	$T_4 = 244 \text{ K}, B(T) = 55.0 \text{ RU}$
$T_{\text{gas3}} = 3.2$	$T_3 = 258 \text{ K}, B(T) = 71.2 \text{ RU}$
$T_{\text{gas2}} = 12.5$	$T_2 = 270 \text{ K}, B(T) = 89.9 \text{ RU}$
$T_{\text{gas1}} = 50.0$	$T_1 = 286 \text{ K}, B(T) = 111.0 \text{ RU}$
	$T_0 = 300 \text{ K}, B(T) = 134.4 \text{ RU}$
	$T_{\text{sfc}} = 310 \text{ K}, B(T_{\text{sfc}}) = 152.5 \text{ RU}, \text{Emissivity} = 1$

Calculation at  $800 \text{ cm}^{-1}$   
which is  $12.5 \mu\text{m}$

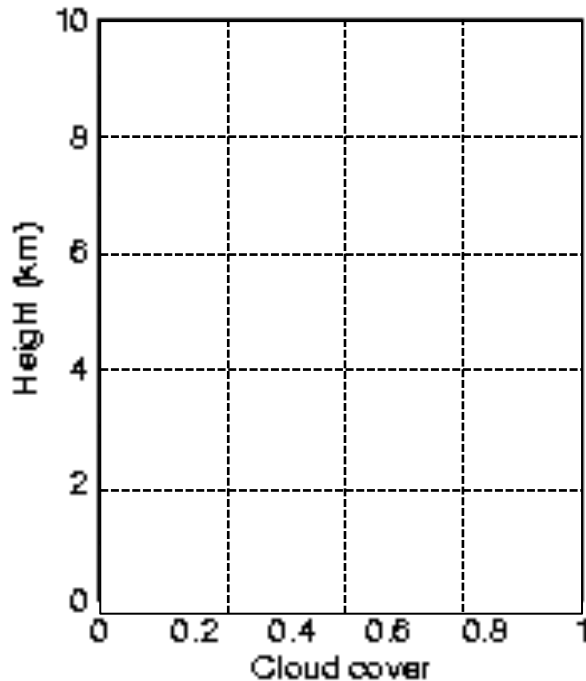
$\text{RU} = 1 \text{ mW}/(\text{m}^2 \text{ sr cm}^{-1})$

$T_2$  is 270 instead of 272 K

Example 1a ( $T_2 = 272 \text{ K}$ ): Downwelling Radiance: 133.9 RU

Example 1c ( $T_2 = 270 \text{ K}$ ): Downwelling Radiance: 133.9 RU

# Downwelling Clear Sky Case (Example 1d)



$$T_{\text{gas5}} = 0.2$$

$$T_{\text{gas4}} = 0.8$$

$$T_{\text{gas3}} = 3.2$$

$$T_{\text{gas2}} = 12.5$$

$$T_{\text{gas1}} = 50.0$$

$$T_5 = 230 \text{ K}, B(T) = 41.2 \text{ RU}$$

$$T_4 = 244 \text{ K}, B(T) = 55.0 \text{ RU}$$

$$T_3 = 258 \text{ K}, B(T) = 71.2 \text{ RU}$$

$$T_2 = 272 \text{ K}, B(T) = 89.9 \text{ RU}$$

$$T_1 = 286 \text{ K}, B(T) = 111.0 \text{ RU}$$

$$T_0 = 302 \text{ K}, B(T) = 137.9 \text{ RU}$$

Calculation at  $800 \text{ cm}^{-1}$   
which is  $12.5 \mu\text{m}$

$$\text{RU} = 1 \text{ mW}/(\text{m}^2 \text{ sr cm}^{-1})$$

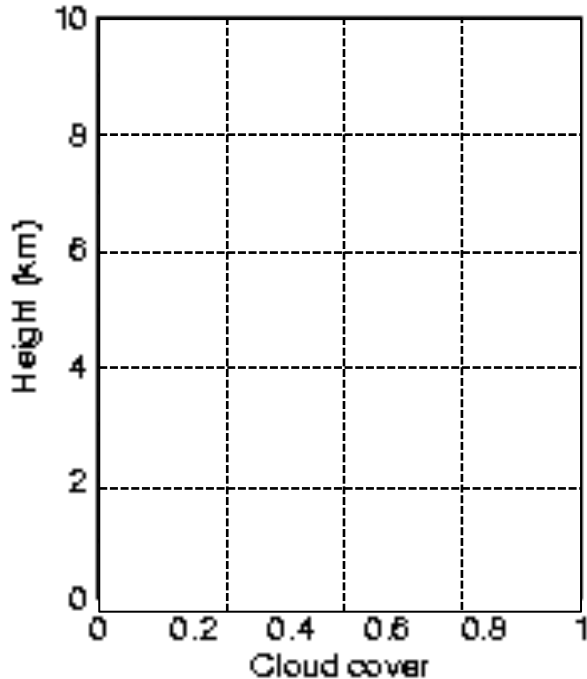
$$T_{\text{sfc}} = 310 \text{ K}, B(T_{\text{sfc}}) = 152.5 \text{ RU}, \text{Emissivity} = 1$$

$T_0$  is 302 instead of 300 K

**Example 1a ( $T_0=300\text{K}$ ): Downwelling Radiance: 133.9 RU**

**Example 1d ( $T_0=302\text{K}$ ): Downwelling Radiance: 137.4 RU**

# Downwelling Clear Sky Case (Example 1e)



$$T_{\text{gas5}} = 0.002$$

$$T_{\text{gas4}} = 0.008$$

$$T_{\text{gas3}} = 0.032$$

$$T_{\text{gas2}} = 0.125$$

$$T_{\text{gas1}} = 0.500$$

$$T_5 = 230 \text{ K}, B(T) = 41.2 \text{ RU}$$

$$T_4 = 244 \text{ K}, B(T) = 55.0 \text{ RU}$$

$$T_3 = 258 \text{ K}, B(T) = 71.2 \text{ RU}$$

$$T_2 = 272 \text{ K}, B(T) = 89.9 \text{ RU}$$

$$T_1 = 286 \text{ K}, B(T) = 111.0 \text{ RU}$$

$$T_0 = 300 \text{ K}, B(T) = 134.4 \text{ RU}$$

$$T_{\text{sfc}} = 310 \text{ K}, B(T_{\text{sfc}}) = 152.5 \text{ RU}, \text{Emissivity} = 1$$

Calculation at  $800 \text{ cm}^{-1}$   
which is  $12.5 \mu\text{m}$

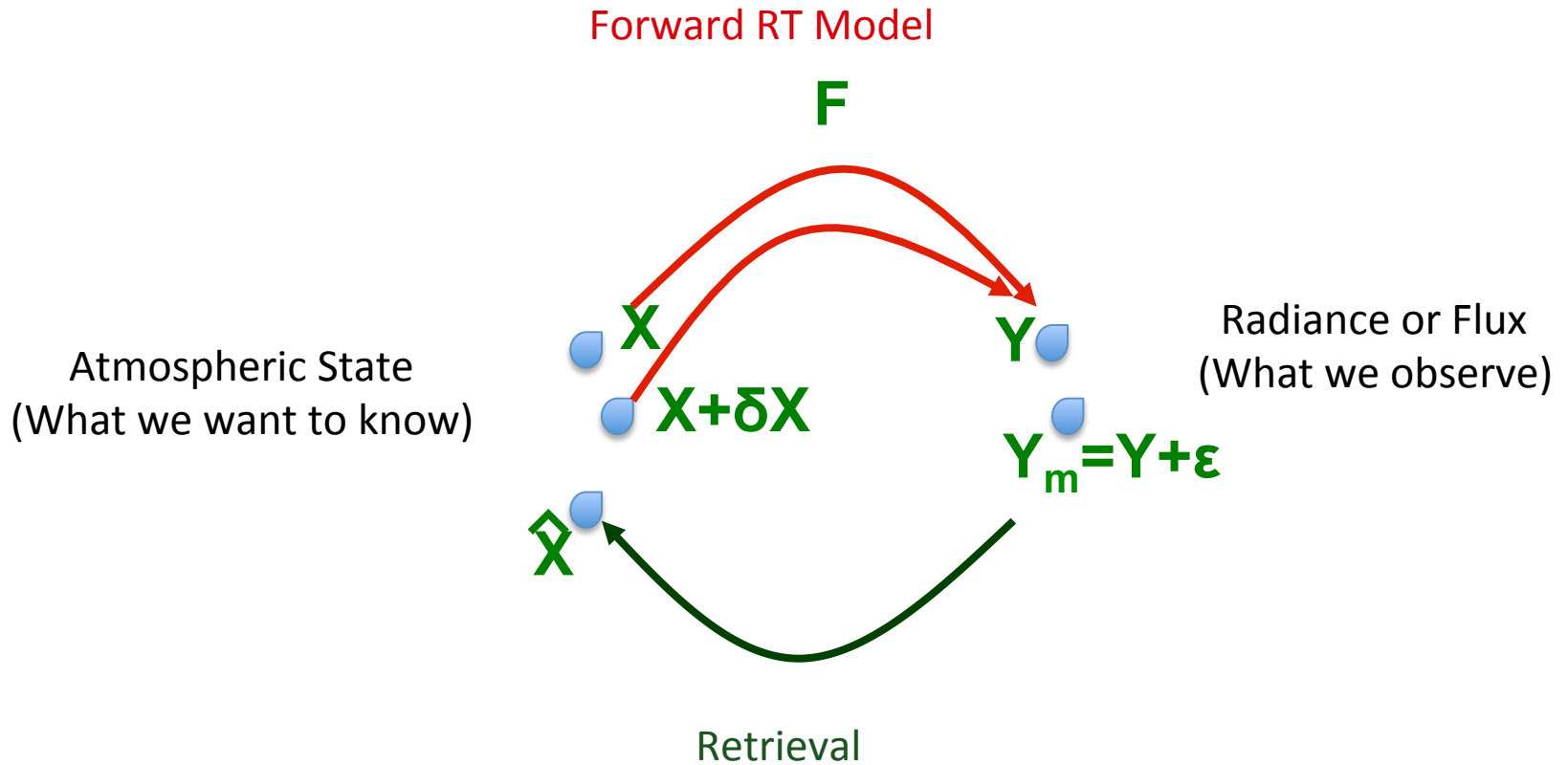
$$\text{RU} = 1 \text{ mW}/(\text{m}^2 \text{ sr cm}^{-1})$$

All optical depths  
are 100x smaller

Example 1a (large tau): Downwelling Radiance: 133.9 RU

Example 1e (small tau): Downwelling Radiance: 59.0 RU

# From Radiance to T/Q Profiles

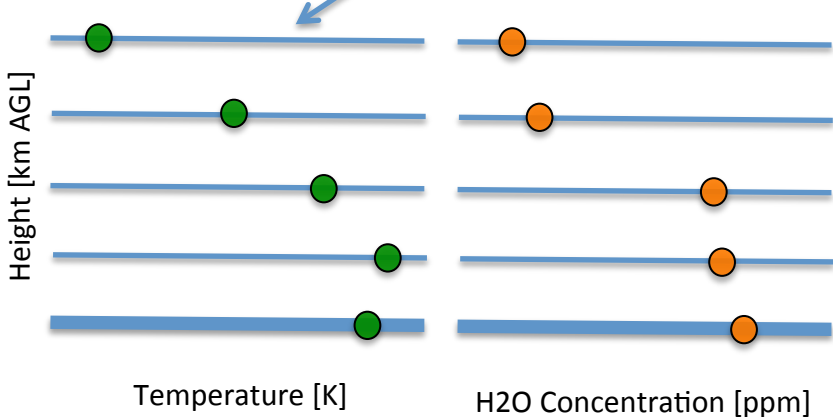
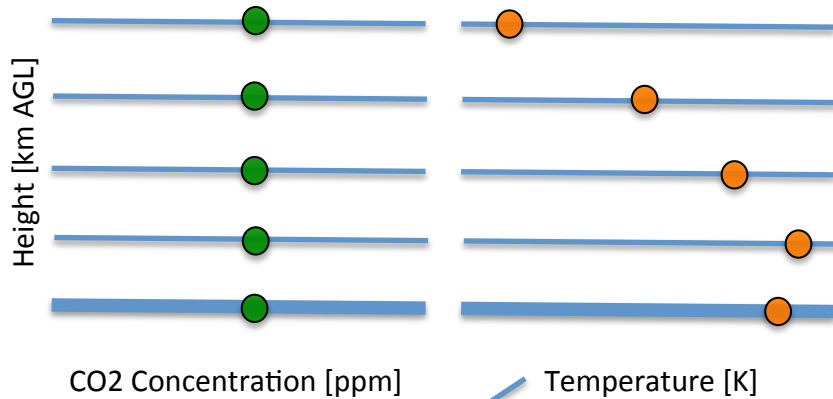




# Retrieval Algorithms

- Algorithm must be able to handle ill-conditioned problem with noise
- Two general approaches:
  - Statistical: use a priori data to generate relationships to relate radiance to  $T(z)$  and  $q(z)$  profile
    - Easy to develop
    - Handles noise well
    - Computationally fast
    - Examples: linear regressions, neural networks, PCA methods, etc
  - Physical: iterative approach whereby a forward RT model is used to derive  $T(z)$  and  $q(z)$  profile
    - Need a priori data to help constrain solution
    - Computationally slow
    - Provides error bars as part of the retrieval

# “Onion Peeling” Physical Retrieval



## Retrieving temperature

1. Assume the concentration of some well-mixed gas ( $\text{CO}_2$  in infrared,  $\text{O}_2$  in microwave)
2. Derive surface temperature using most opaque channel(s)
3. Derive temperature of next level using slightly less opaque channel(s)
4. Continue to get entire profile

## Retrieving water vapor

1. Assume the temperature retrieval from above is “accurate”
2. Derive surface WV concentration using most opaque channel(s)
3. Derive WV of next level using slightly less opaque channel(s)
4. Continue to get entire profile

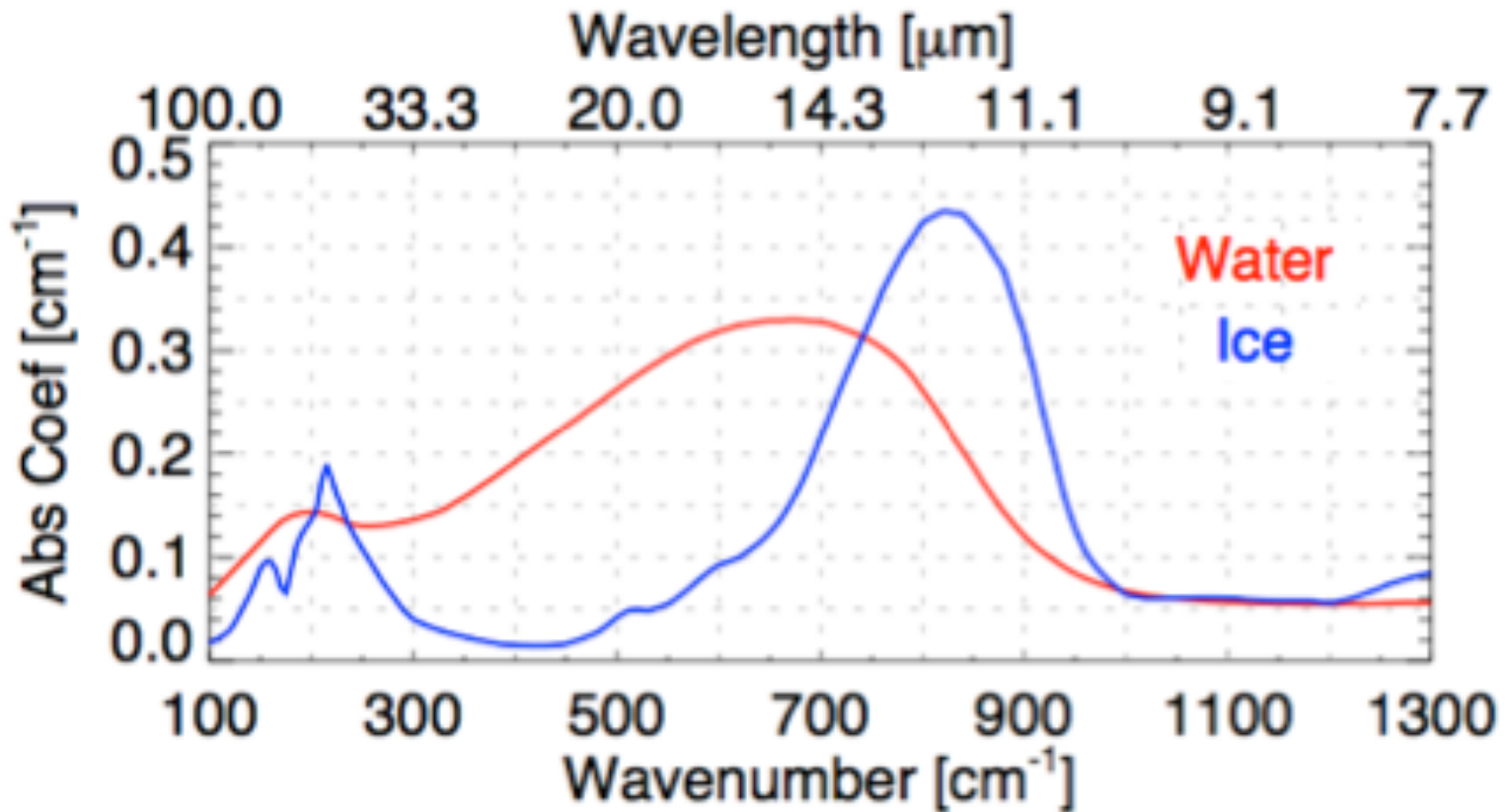
Solution will have correlated error!

# Clear skies are “simple”...

...clouds (and aerosols) greatly complicate radiative transfer calculations

- Different compositions (liquid, ice, soot, sulfate, etc) have different spectral absorption bands

# IR Absorption Coefficients of Ice and Water



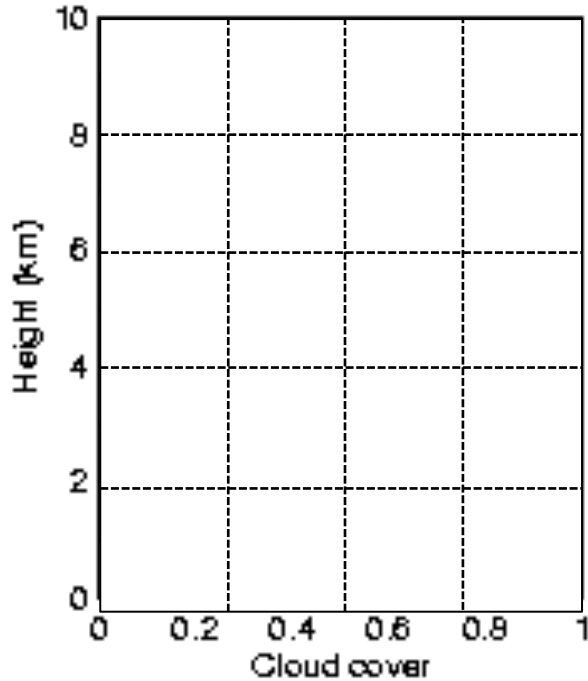
# Clear skies are “simple”...

...clouds (and aerosols) greatly complicate radiative transfer calculations

- Different compositions (liquid, ice, soot, sulfate, etc) have different spectral absorption bands
- Different size distributions (monomodal, bimodal, etc)
- Spherical and nonspherical particles
- Very inhomogeneous distribution
  - Within an atmospheric layer
  - Between different layers
- Absorption and scattering

**But we are going to leave scattering for another day**

# Downwelling Clear Sky Case (Example 2a)



$$T_{\text{gas5}} = 0.002$$

$$T_{\text{gas4}} = 0.008$$

$$T_{\text{gas3}} = 0.032$$

$$T_{\text{gas2}} = 0.125$$

$$T_{\text{gas1}} = 0.500$$

$$T_5 = 230 \text{ K}, B(T) = 41.2 \text{ RU}$$

$$T_4 = 244 \text{ K}, B(T) = 55.0 \text{ RU}$$

$$T_3 = 258 \text{ K}, B(T) = 71.2 \text{ RU}$$

$$T_2 = 272 \text{ K}, B(T) = 89.9 \text{ RU}$$

$$T_1 = 286 \text{ K}, B(T) = 111.0 \text{ RU}$$

$$T_0 = 300 \text{ K}, B(T) = 134.4 \text{ RU}$$

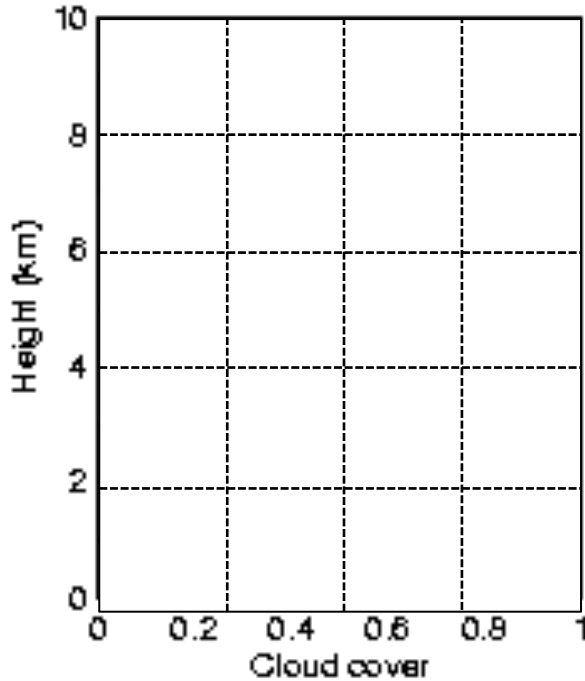
$$T_{\text{sfc}} = 310 \text{ K}, B(T_{\text{sfc}}) = 152.5 \text{ RU}, \text{Emissivity} = 1$$

Calculation at  $800 \text{ cm}^{-1}$   
which is  $12.5 \mu\text{m}$

RU =  $1 \text{ mW}/(\text{m}^2 \text{ sr cm}^{-1})$

Downwelling radiance:  $(1 - \exp(-0.002)) * (41.2 + 55.0) / 2 * \exp(- (0.008 + 0.032 + 0.125 + 0.5)) +$

# Upwelling Clear Sky Case (Example 2b)



$$T_{\text{gas5}} = 0.002$$

$$T_{\text{gas4}} = 0.008$$

$$T_{\text{gas3}} = 0.032$$

$$T_{\text{gas2}} = 0.125$$

$$T_{\text{gas1}} = 0.500$$

$$T_5 = 230 \text{ K}, B(T) = 41.2 \text{ RU}$$

$$T_4 = 244 \text{ K}, B(T) = 55.0 \text{ RU}$$

$$T_3 = 258 \text{ K}, B(T) = 71.2 \text{ RU}$$

$$T_2 = 272 \text{ K}, B(T) = 89.9 \text{ RU}$$

$$T_1 = 286 \text{ K}, B(T) = 111.0 \text{ RU}$$

$$T_0 = 300 \text{ K}, B(T) = 134.4 \text{ RU}$$

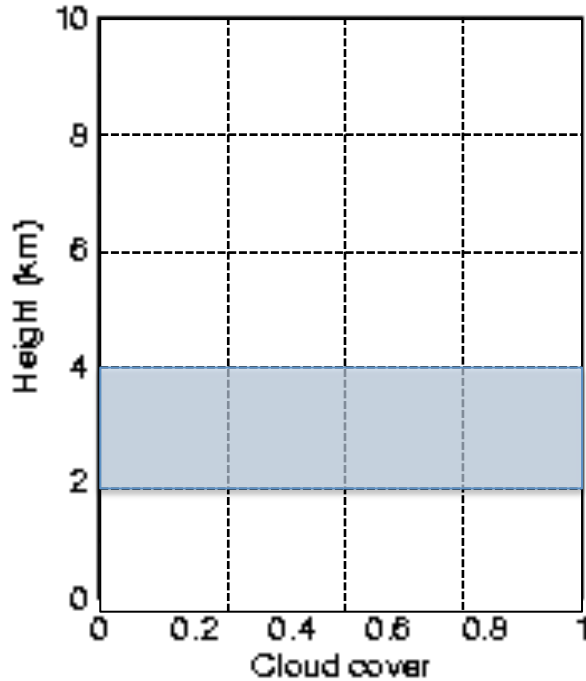
$$T_{\text{sfc}} = 310 \text{ K}, B(T_{\text{sfc}}) = 152.5 \text{ RU}, \text{Emissivity} = 1$$

Calculation at  $800 \text{ cm}^{-1}$   
which is  $12.5 \mu\text{m}$

$$\text{RU} = 1 \text{ mW}/(\text{m}^2 \text{ sr cm}^{-1})$$

Upwelling radiance:  $152.5 * 1.0 * \exp(-(0.5 + 0.125 + 0.032 + 0.008 + 0.002)) +$

# Down and Upwelling Cloudy Sky Case #1



$$T_{\text{gas5}} = 0.002$$

$$T_5 = 230 \text{ K}, B(T) = 41.2 \text{ RU}$$

$$T_{\text{gas4}} = 0.008$$

$$T_4 = 244 \text{ K}, B(T) = 55.0 \text{ RU}$$

$$T_{\text{gas3}} = 0.032$$

$$T_3 = 258 \text{ K}, B(T) = 71.2 \text{ RU}$$

$$T_{\text{gas2}} = 0.125$$

$$T_2 = 272 \text{ K}, B(T) = 89.9 \text{ RU}$$

$$T_{\text{cloud2}} = 4, F_{\text{cld}} = 1.0$$

$$T_{\text{gas1}} = 0.500$$

$$T_1 = 286 \text{ K}, B(T) = 111.0 \text{ RU}$$

$$T_0 = 300 \text{ K}, B(T) = 134.4 \text{ RU}$$

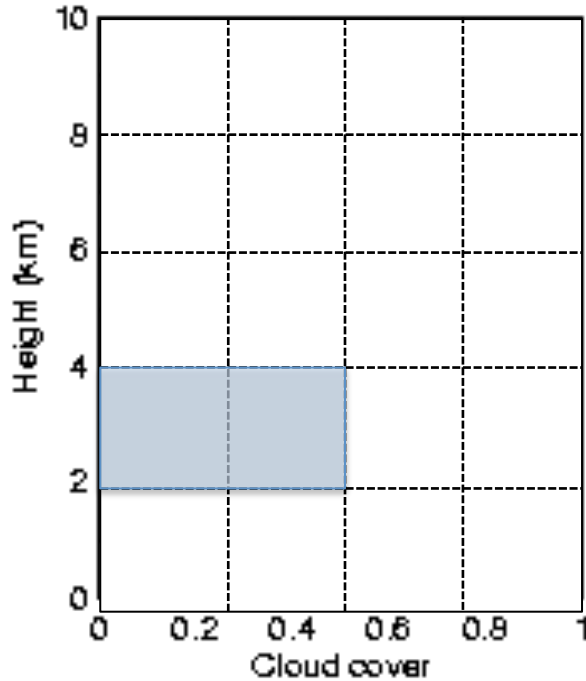
$$T_{\text{sfc}} = 310 \text{ K}, B(T_{\text{sfc}}) = 152.5 \text{ RU}, \text{Emissivity} = 1$$

$$R_{\uparrow} = ? \text{ RU}$$

$$R_{\downarrow} = ? \text{ RU}$$



# Down and Upwelling Cloudy Sky Case #2



$$T_{\text{gas5}} = 0.002$$

$$T_5 = 230 \text{ K}, B(T) = 41.2 \text{ RU}$$

$$T_{\text{gas4}} = 0.008$$

$$T_4 = 244 \text{ K}, B(T) = 55.0 \text{ RU}$$

$$T_{\text{gas3}} = 0.032$$

$$T_3 = 258 \text{ K}, B(T) = 71.2 \text{ RU}$$

$$T_{\text{gas2}} = 0.125$$

$$T_2 = 272 \text{ K}, B(T) = 89.9 \text{ RU}$$

$$T_{\text{gas1}} = 0.500$$

$$T_1 = 286 \text{ K}, B(T) = 111.0 \text{ RU}$$

$$T_0 = 300 \text{ K}, B(T) = 134.4 \text{ RU}$$

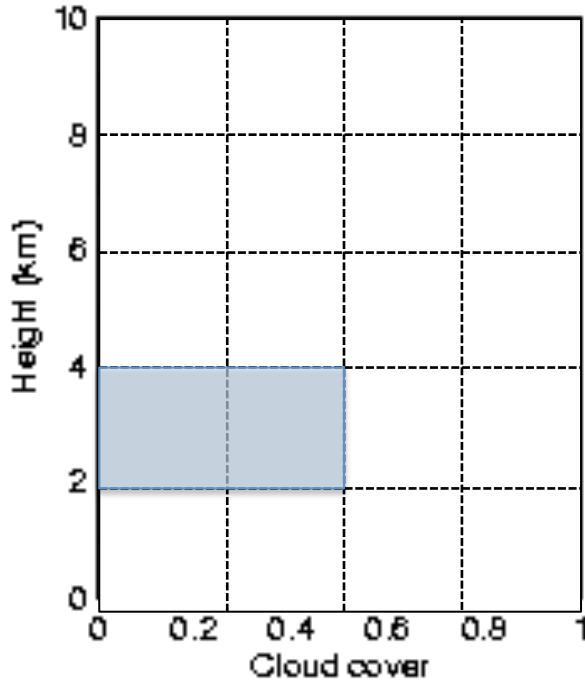
$$T_{\text{cloud2}} = 4, F_{\text{cld}} = 0.5$$

$$T_{\text{sfc}} = 310 \text{ K}, B(T_{\text{sfc}}) = 152.5 \text{ RU}, \text{Emissivity} = 1$$

$$R_{\uparrow} = ? \text{ RU}$$

$$R_{\downarrow} = ? \text{ RU}$$

# Down and Upwelling Cloudy Sky Case #3



$$T_{\text{gas5}} = 0.002$$

$$T_{\text{gas4}} = 0.008$$

$$T_{\text{gas3}} = 0.032$$

$$T_{\text{gas2}} = 0.125$$

$$T_{\text{gas1}} = 0.500$$

$$T_5 = 230 \text{ K}, B(T) = 41.2 \text{ RU}$$

$$T_4 = 244 \text{ K}, B(T) = 55.0 \text{ RU}$$

$$T_3 = 258 \text{ K}, B(T) = 71.2 \text{ RU}$$

$$T_2 = 272 \text{ K}, B(T) = 89.9 \text{ RU}$$

$$T_1 = 286 \text{ K}, B(T) = 111.0 \text{ RU}$$

$$T_0 = 300 \text{ K}, B(T) = 134.4 \text{ RU}$$

$$T_{\text{sfc}} = 310 \text{ K}, B(T_{\text{sfc}}) = 152.5 \text{ RU}, \text{Emissivity} = 1$$

$$T_{\text{cloud4}} = 1, F_{\text{cld}} = 0.25$$

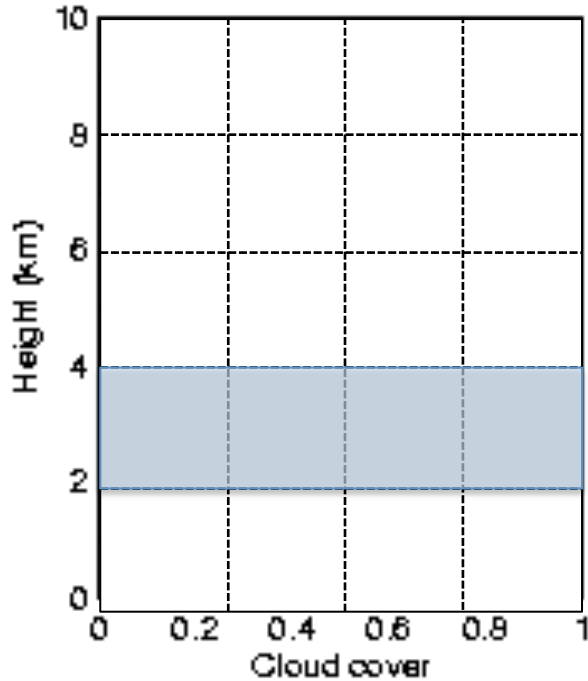
$$T_{\text{cloud2}} = 4, F_{\text{cld}} = 0.5$$

$$R_{\uparrow} = ? \text{ RU}$$

$$R_{\downarrow} = ? \text{ RU}$$

# Answers

# Down and Upwelling Cloudy Sky Case #1



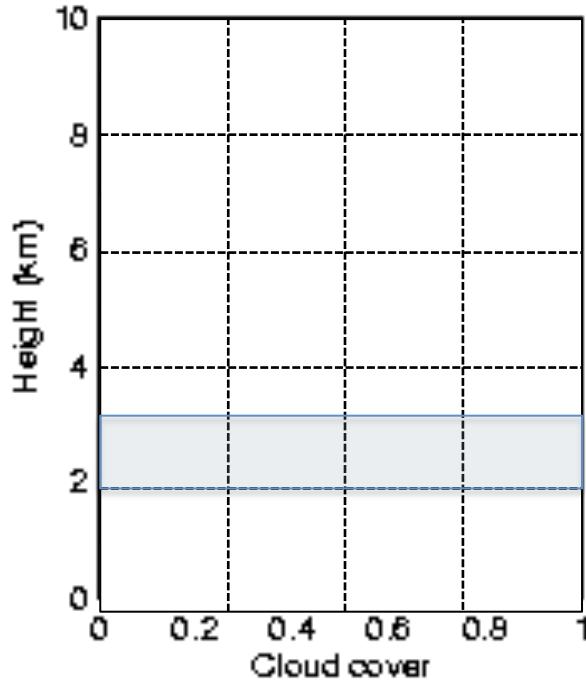
$T_{\text{gas5}} = 0.002$        $T_5 = 230 \text{ K}, B(T) = 41.2 \text{ RU}$   
 $T_{\text{gas4}} = 0.008$        $T_4 = 244 \text{ K}, B(T) = 55.0 \text{ RU}$   
 $T_{\text{gas3}} = 0.032$        $T_3 = 258 \text{ K}, B(T) = 71.2 \text{ RU}$   
 $T_{\text{gas2}} = 0.125$        $T_2 = 272 \text{ K}, B(T) = 89.9 \text{ RU}$   
 $T_{\text{gas1}} = 0.500$        $T_1 = 286 \text{ K}, B(T) = 111.0 \text{ RU}$   
 $T_0 = 300 \text{ K}, B(T) = 134.4 \text{ RU}$   
 $T_{\text{sfc}} = 310 \text{ K}, B(T_{\text{sfc}}) = 152.5 \text{ RU}, \text{Emissivity} = 1$

$T_{\text{cloud2}} = 4, F_{\text{cld}} = 1.0$

$R_{\uparrow} = 100.05 \text{ RU}$

$R_{\downarrow} = 108.03 \text{ RU}$

# Down and Upwelling Cloudy Sky Case #2



$$T_{\text{gas5}} = 0.002$$

$$T_5 = 230 \text{ K}, B(T) = 41.2 \text{ RU}$$

$$T_{\text{gas4}} = 0.008$$

$$T_4 = 244 \text{ K}, B(T) = 55.0 \text{ RU}$$

$$T_{\text{gas3}} = 0.032$$

$$T_3 = 258 \text{ K}, B(T) = 71.2 \text{ RU}$$

$$T_{\text{gas2}} = 0.125$$

$$T_2 = 272 \text{ K}, B(T) = 89.9 \text{ RU}$$

$$T_{\text{gas1}} = 0.500$$

$$T_1 = 286 \text{ K}, B(T) = 111.0 \text{ RU}$$

$$T_0 = 300 \text{ K}, B(T) = 134.4 \text{ RU}$$

$$T_{\text{cloud2}} = 4, F_{\text{cld}} = 0.5$$

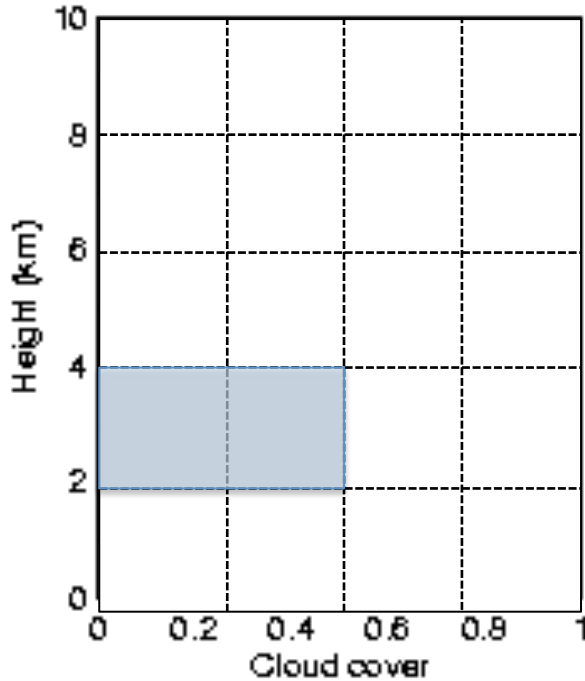
$$T_{\text{sfc}} = 310 \text{ K}, B(T_{\text{sfc}}) = 152.5 \text{ RU}, \text{Emissivity} = 1$$

$$R_{\uparrow} = 104.05 \text{ RU}$$

$$R_{\downarrow} = 101.95 \text{ RU}$$

**Averaging optical depth for clear and cloudy scenes**

# Down and Upwelling Cloudy Sky Case #2



$$T_{\text{gas5}} = 0.002$$

$$T_5 = 230 \text{ K}, B(T) = 41.2 \text{ RU}$$

$$T_{\text{gas4}} = 0.008$$

$$T_4 = 244 \text{ K}, B(T) = 55.0 \text{ RU}$$

$$T_{\text{gas3}} = 0.032$$

$$T_3 = 258 \text{ K}, B(T) = 71.2 \text{ RU}$$

$$T_{\text{gas2}} = 0.125$$

$$T_2 = 272 \text{ K}, B(T) = 89.9 \text{ RU}$$

$$T_{\text{gas1}} = 0.500$$

$$T_1 = 286 \text{ K}, B(T) = 111.0 \text{ RU}$$

$$T_0 = 300 \text{ K}, B(T) = 134.4 \text{ RU}$$

$$T_{\text{cloud2}} = 4, F_{\text{cld}} = 0.5$$

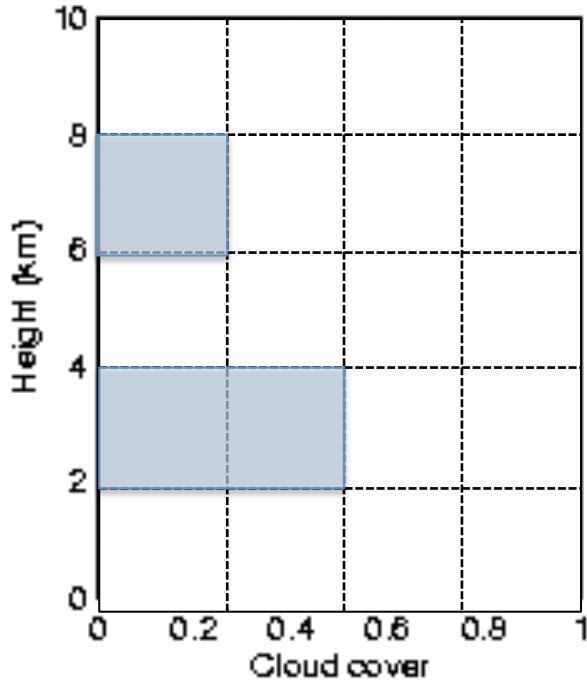
$$T_{\text{sfc}} = 310 \text{ K}, B(T_{\text{sfc}}) = 152.5 \text{ RU}, \text{Emissivity} = 1$$

$$R_{\uparrow} = 116.80 \text{ RU}$$

$$R_{\downarrow} = 82.51 \text{ RU}$$

**Independent Column Approximation (ICA)**  
 (This is much more accurate than the previous)

# Down and Upwelling Cloudy Sky Case #3



$$T_{\text{gas5}} = 0.002$$

$$T_{\text{gas4}} = 0.008$$

$$T_{\text{gas3}} = 0.032$$

$$T_{\text{gas2}} = 0.125$$

$$T_{\text{gas1}} = 0.500$$

$$T_5 = 230 \text{ K}, B(T) = 41.2 \text{ RU}$$

$$T_4 = 244 \text{ K}, B(T) = 55.0 \text{ RU}$$

$$T_3 = 258 \text{ K}, B(T) = 71.2 \text{ RU}$$

$$T_2 = 272 \text{ K}, B(T) = 89.9 \text{ RU}$$

$$T_1 = 286 \text{ K}, B(T) = 111.0 \text{ RU}$$

$$T_0 = 300 \text{ K}, B(T) = 134.4 \text{ RU}$$

$$T_{\text{cloud4}} = 1, F_{\text{cld}} = 0.25$$

$$T_{\text{cloud2}} = 4, F_{\text{cld}} = 0.5$$

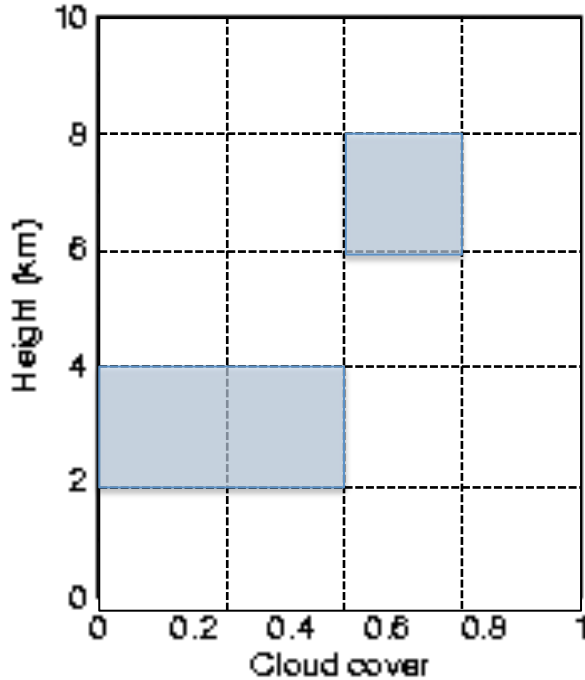
$$T_{\text{sfc}} = 310 \text{ K}, B(T_{\text{sfc}}) = 152.5 \text{ RU}, \text{Emissivity} = 1$$

$$R_{\uparrow} = 110.96 \text{ RU}$$

$$R_{\downarrow} = 82.61 \text{ RU}$$

**Maximum overlap**

# Down and Upwelling Cloudy Sky Case #3



$T_{\text{gas5}} = 0.002$   
 $T_{\text{gas4}} = 0.008$   
 $T_{\text{gas3}} = 0.032$   
 $T_{\text{gas2}} = 0.125$   
 $T_{\text{gas1}} = 0.500$   
 $T_{\text{sfc}} = 310 \text{ K}, B(T_{\text{sfc}}) = 152.5 \text{ RU}, \text{Emissivity} = 1$

$T_5 = 230 \text{ K}, B(T) = 41.2 \text{ RU}$

$T_4 = 244 \text{ K}, B(T) = 55.0 \text{ RU}$

$T_3 = 258 \text{ K}, B(T) = 71.2 \text{ RU}$

$T_2 = 272 \text{ K}, B(T) = 89.9 \text{ RU}$

$T_1 = 286 \text{ K}, B(T) = 111.0 \text{ RU}$

$T_0 = 300 \text{ K}, B(T) = 134.4 \text{ RU}$

$T_{\text{cloud4}} = 1, F_{\text{cld}} = 0.25$

$T_{\text{cloud2}} = 4, F_{\text{cld}} = 0.5$

$R_{\uparrow} = 105.66 \text{ RU}$

$R_{\downarrow} = 87.62 \text{ RU}$

**Minimum overlap**